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A SHORT TABLE OF
LANCHESTER-CLIFFORD-SCHLAFLI FUNCTIONS

by
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and
Gerald G. Brown

October 1977

NAVAL POSTGRADUATE SCHOOL
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report contains a reduced set of tables of Lanchester-Clifford-Schläfli (LCS) functions. A companion report contains a more extensive (and currently the most extensive available) set of tables of the LCS functions. These functions may be used to analyze Lanchester-type combat between two homogeneous forces modelled by power attrition-rate coefficients with "no effect." Theoretical background for the LCS functions is given, as well as a narrative description of the physical circumstances under which the associated		

20. Cont.

Lanchester-type combat model may be expected to be applicable. Numerical examples are given to illustrate the use of the LCS functions for analyzing "aimed-fire" combat modelled by the power attrition-rate coefficients with "no offset." Our results and these tabulations allow one to study this particular variable-coefficient combat model almost as easily and thoroughly as Lanchester's classic constant-coefficient model.

A SHORT TABLE OF LANCHESTER-CLIFFORD-SCHLÄFLI FUNCTIONS

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1. Introduction

Lanchester-type* differential-equation combat models are an important tool for analyzing many important problems of military operations research. In such a combat model, a so-called attrition-rate coefficient represents the fire effectiveness of a particular weapon-system type against a particular target type, i.e. the weapon-system type's effective firepower against such a target. Time-dependent attrition-rate coefficients are used to model temporal variations in firepower on the battlefield. Thus, we see that time-dependent attrition-rate coefficients are important (and, in fact, essential [4-6]) for the quantitative analysis of hypothetical combat.

Militarily realistic computer-based Lanchester-type models of quite complex military systems have been developed for almost the entire spectrum of combat operations, from combat between battalion-sized units to theater-level operations. Nevertheless, a simple combat model may yield a clearer understanding of significant interrelationships that are difficult to perceive in a more complex model, and such insights can subsequently provide valuable guidance for more detailed computerized investigations. In this report we consider such a simplified variable-coefficient Lanchester-type model of combat between two homogeneous forces.

For this variable-coefficient Lanchester-type model of combat between two homogeneous forces, different functional forms for the attrition-rate coefficients lead to different mathematical functions being involved in representing and computing the force-level trajectories. In a previous paper [5] we have discussed the plausibility of the hypothesis that except for the special case of a constant ratio of attrition-rate coefficients,

*So-called after pioneering work of F. W. Lanchester [3].

the solutions to such differential equations cannot be represented in term of "elementary" functions of analysis. Thus, new transcendental functions arise in the study of combat modelled with time-dependent attrition-rate coefficients. In particular, we have previously introduced [5-6] so-called Lanchester-Clifford-Schläfli (LCS) functions for analyzing combat modelled with power attrition-rate coefficients with "no offset" (see Section 3 below).

In the Appendix to this report is contained a reduced set of tables for the LCS functions: it contains tables of five-decimal-place values of the hyperbolic-like LCS functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ (see Section 4 below) for 11 fractional values of α (see Section 6 below). A companion report [8] contains the most extensive set of tables currently available. The main body of this report provides the theoretical and modelling background for the use of these tables. In particular, we examine a model of a constant-speed attack on a static defensive position and show how associated range-dependent kill rates give rise to time-dependent attrition-rate coefficients with "no offset." Numerical computations are presented to illustrate the use of the LCS functions for analyzing such "aimed-fire" combat. As a consequence of the availability of these tables, one can now study this variable-coefficient combat model almost as easily and thoroughly as Lanchester's classic constant-coefficient model.

2. Variable-Coefficient Lanchester-Type Equations of Modern Warfare.

We consider combat between two homogeneous forces modelled by the following variable-coefficient Lanchester-type [3] (see [4,5]) equations of modern warfare

$$\left\{ \begin{array}{ll} \frac{dx}{dt} = -a(t)y & \text{with } x(0) = x_0 , \\ \frac{dy}{dt} = -b(t)x & \text{with } y(0) = y_0 , \end{array} \right. \quad (2.1)$$

where $t = 0$ denotes the time at which the battle begins, $x(t)$ and $y(t)$ denote the numbers of X and Y at time t , and $a(t)$ and $b(t)$ denote time-dependent Lanchester attrition-rate coefficients, which represent the effectiveness of each side's fire. These coefficients depend on variables such as force separation, tactical posture of targets, rate of target acquisition, firing rate, etc. (see [4-7] for further details). Variable attrition-rate coefficients are used to model temporal variations in firepower on the battlefield. In any analysis of combat, moreover, we should use the above equations (2.1) only for x and $y > 0$ and, for example, set $dx/dt = 0$ when $x = 0$, since negative force levels have no physical meaning.

Mathematically, we assume that the attrition-rate coefficients $a(t)$ and $b(t)$ are defined, positive, and continuous for $t_0 < t < +\infty$ with $t_0 \leq 0$. We also assume that $a(t)$ and $b(t) \in L(t_0, T)$ for any finite $T \geq t_0$. We further take $a(t)$ and $b(t)$ to be given in the form

$$a(t) = k_a g(t) , \quad \text{and} \quad b(t) = k_b h(t) , \quad (2.2)$$

where k_a and k_b are positive constants chosen so that $a(t)/b(t) = k_a/k_b$ when $g(t) \equiv h(t)$. We introduce the combat-intensity parameter λ_I and the relative-fire-effectiveness parameter λ_R defined by

$$\lambda_I = \sqrt{k_a k_b}, \quad \text{and} \quad \lambda_R = k_a/k_b. \quad (2.3)$$

From our assumptions about $a(t)$ and $b(t)$, it follows that, for example, $a(t) \notin L(t_0, T)$ implies $\int_{t_0}^T a(t)dt = +\infty$.

The X force level as a function of time may be represented as [5,6]

$$x(t) = x_0 \{C_Y(0)C_X(t) - S_Y(0)S_X(t)\} - y_0 \sqrt{\lambda_R} \{C_X(0)S_X(t) - S_X(0)C_X(t)\}, \quad (2.4)$$

where the hyperbolic-like general Lanchester functions (GLF) $C_X(t)$ and $S_X(t)$ are linearly-independent solutions to the X force-level equation

$$\frac{d^2 x}{dt^2} - \left\{ \frac{1}{a(t)} \frac{da}{dt} \right\} \frac{dx}{dt} - a(t)b(t)x = 0, \quad (2.5)$$

with initial conditions

$$C_X(t_0) = 1, \quad S_X(t_0) = 0, \quad (2.6)$$

$$\{1/a(t_0)\} dC_X/dt(t_0) = 0, \quad \{1/a(t_0)\} dS_X/dt(t_0) = 1/\sqrt{\lambda_R}.$$

Here t_0 denotes the largest finite time at which $a(t)$ or $b(t)$ ceases to be defined, positive, or continuous. The Y force level as a function of time is given by a similar expression, with $C_Y(t)$ and $S_Y(t)$ being analogously defined for the corresponding Y force-level equation.

It is sometimes convenient to introduce the new independent variable τ defined by

$$\tau = \int_{t_0}^t \sqrt{a(s)b(s)} \, ds . \quad (2.7)$$

It is readily seen that the transformation $\tau = \tau(t)$ is well defined and invertible. Let us denote $\tau(0)$ as τ_0 . We observe that $t_0 \leq 0$ implies that $\tau_0 \geq 0$. If we denote the "average intensity of combat" as $\sqrt{a(t)b(t)}$, then

$$\sqrt{a(t)b(t)} \, t = \left\{ (1/t) \int_0^t \sqrt{a(s)b(s)} \, ds \right\} t = \tau - \tau_0 . \quad (2.8)$$

The substitution (2.7) transforms (2.5) into

$$\frac{d^2 x}{d\tau^2} - \left(\frac{1}{2}\right) \left\{ \frac{d}{d\tau} \ln R(\tau) \right\} \frac{dx}{d\tau} - x = 0 , \quad (2.9)$$

with initial conditions

$$x(\tau_0) = x_0 , \quad \text{and} \quad \{1/\sqrt{R(\tau_0)}\} \, dx/d\tau(\tau_0) = -y_0 ,$$

where $R(\tau) = a(t)/b(t)$.

3. Combat Modelled with Power Attrition-Rate Coefficients.

The above equations (2.1) basically apply to "aimed-fire" combat when target-acquisition times do not depend on the numbers of targets available (see [5,6] for further details). A large class of tactical situations of interest can be modelled with the following general power attrition-rate coefficients [5-7]

$$a(t) = k_a (t + C)^\mu, \quad \text{and} \quad b(t) = k_b (t + C + A)^\nu, \quad (3.1)$$

where A and $C \geq 0$. We will call A the offset parameter, since it allows us to model (with μ and $\nu \geq 0$) battles between opposing weapon systems with different maximum effective ranges (see [5,6]). We will call C the starting parameter, since it allows us to model (again, with μ and $\nu \geq 0$) battles that begin within the maximum effective ranges of the two opposing systems. We observe that for the general power attrition-rate coefficients (3.1) we have $t_0 = -C$, and μ and ν must be > -1 in order that $a(t)$ and $b(t) \in L(t_0, T)$.

The above nomenclature is motivated and possible applications of our work are indicated by considering S. Bonder's model of the constant-speed attack on a static defensive position (see [4-7] for further details)

$$\frac{dx}{dt} = -\alpha(r)y, \quad \text{and} \quad \frac{dy}{dt} = -\beta(r)x, \quad (3.2)$$

where r denotes the range between opposing forces, and $\alpha(r)$ and $\beta(r)$ denote range-dependent attrition-rate coefficients. Range is related to time by

$$r(t) = R_0 - vt, \quad (3.3)$$

where R_0 denotes the opening range of battle and $v > 0$ denotes the constant attack speed. For example, let us consider the constant-speed attack of a homogeneous Y force against the static defensive position of a homogeneous X force. Figure 1 diagrammatically portrays this situation.

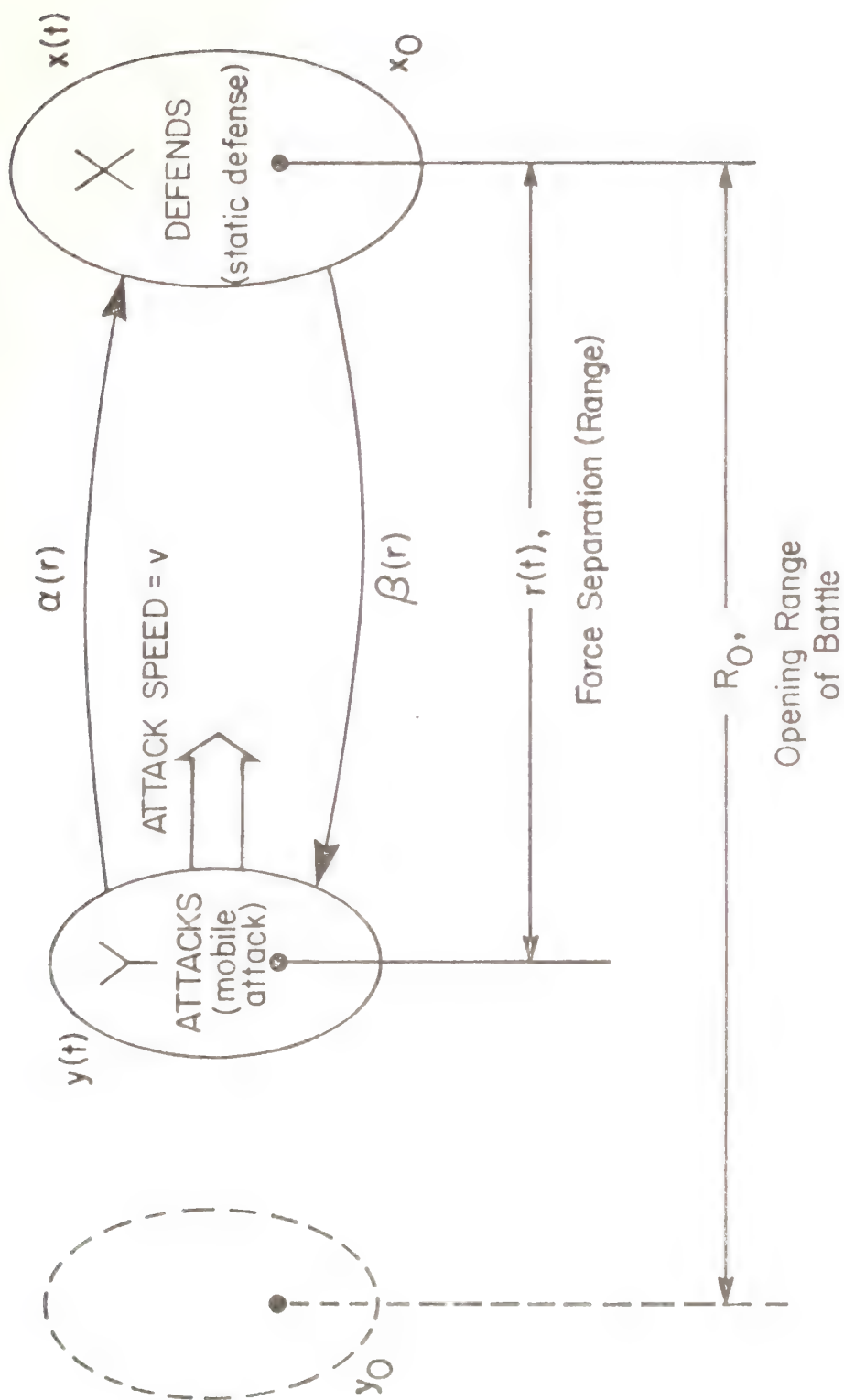


Figure 1. Diagram of Bonder's constant-speed attack model.

Force separation, $r(t)$, is given by $r(t) = R_0 - vt$.

The basic idea is that force separation, i.e. range between the opposing forces, changes over time, and the fire effectiveness of, for example, a single Y firer, denoted as $\alpha(r)$, depends on this force separation.

In many cases of tactical interest, we may model the fire effectiveness of, for example, the Y weapon system (as a function of range) with

$$\alpha(r) = \begin{cases} \alpha_0 \left(1 - \frac{r}{R_\alpha}\right)^\mu & \text{for } 0 \leq r \leq R_\alpha, \\ 0 & \text{for } R_\alpha \leq r, \end{cases} \quad (3.4)$$

where R_α denotes the maximum effective range of the Y weapon system and $\mu \geq 0$. Here μ is used to model the range dependency of Y's attrition-rate coefficient (see Figure 2). We model $\beta(r)$ similarly, with corresponding quantities R_β and ν being analogous to R_α and μ above.

If we use (3.3) to eliminate range r from (3.4), we obtain

$$\begin{cases} \frac{dx}{dt} = -a(t)y, \\ \frac{dy}{dt} = -b(t)x, \end{cases} \quad (3.5)$$

where the time-dependent attrition-rate coefficients $a(t)$ and $b(t)$ are given by (3.1). It follows that the offset and starting parameters are given by

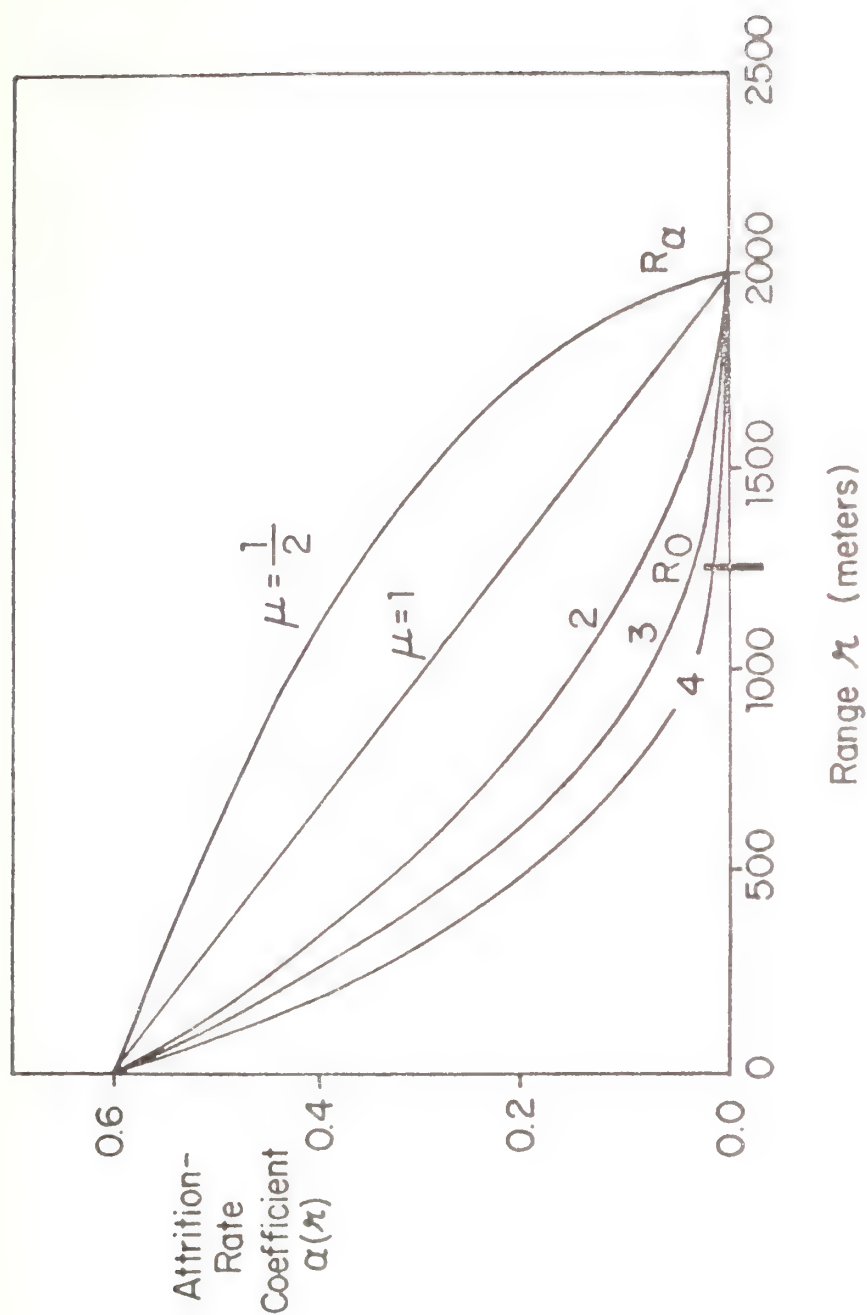


Figure 2. Dependence of Y's attrition-rate coefficient $\alpha(r)$ on the exponent μ with the maximum effective range of the weapon system and kill rate at zero range held constant. [NOTES: 1. The maximum effective range of the system is denoted as $R_\alpha = 2000$ meters. 2. $\alpha(0) = \alpha_0 = 0.6X$ casualties/(unit time \times number of Y firers) denotes the weapon-system kill rate for Y at zero force separation (range). 3. The opening range of battle is denoted as $R_0 = 1250$ meters and (as shown) $R_0 < R_\alpha$.]

$$A = \left(\frac{R_\beta - R_\alpha}{v} \right), \quad \text{and} \quad C = \left(\frac{R_\alpha - R_0}{v} \right), \quad (3.6)$$

and that

$$k_a = \alpha_0 \left(\frac{v}{R_\alpha} \right)^\mu, \quad \text{and} \quad k_b = \beta_0 \left(\frac{v}{R_\beta} \right)^\nu. \quad (3.7)$$

We observe that A and $C \geq 0$ if and only if $R_\beta \geq R_\alpha \geq R_0$. By considering (3.6) and Figure 3, the reader should have no trouble in understanding our terminology for A and C .

When the offset parameter is equal to zero (i.e. $A = 0$), then the coefficients (3.1) reduce to

$$a(t) = k_a (t+C)^\mu, \quad \text{and} \quad b(t) = k_b (t+C)^\nu. \quad (3.8)$$

We will refer to (3.8) as power attrition-rate coefficients with "no offset." As we have seen above in Bonder's constant-speed attack model, these coefficients model, for example, combat between weapon systems with the same maximum effective range so that there is no "offset" in the "reaching out" of the weapon systems against each other in combat (again, see Figure 3). For these coefficients (3.8), the transformed X force-level equation (2.9) becomes

$$\frac{d^2 x}{d\tau^2} + \left(\frac{2q-1}{\tau} \right) \frac{dx}{d\tau} - x = 0, \quad (3.9)$$

with initial conditions

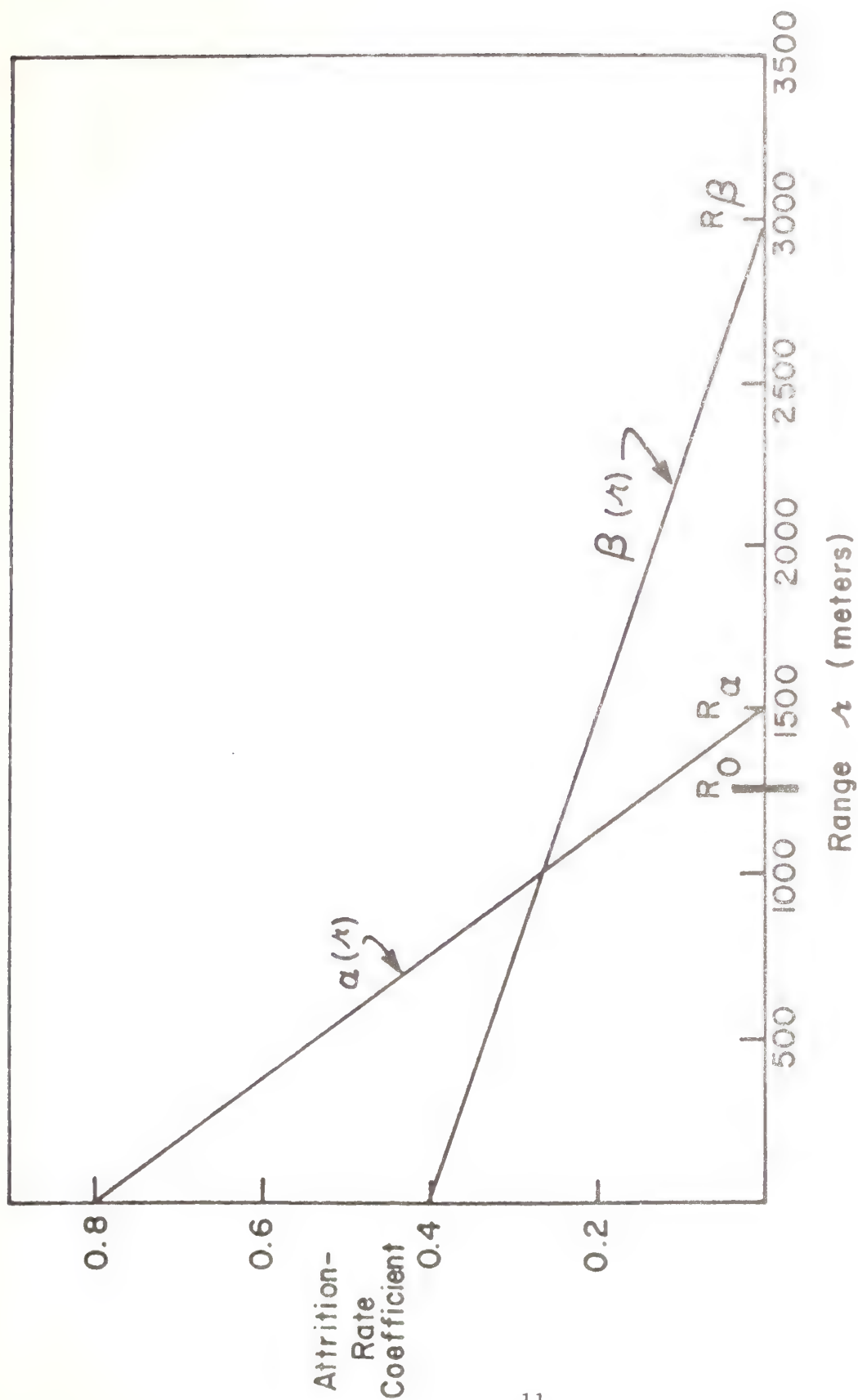


Figure 3. Explanation of the offset parameter A and the starting parameter C for power attrition-rate coefficients modelling constant-speed attack. [NOTES: 1. The maximum effective ranges of the X and Y weapon systems are denoted as R_α and R_β , respectively. 2. The opening range of battle is denoted as R_0 and (as shown) $R_0 < \min(R_\alpha, R_\beta)$. 3. The offset parameter is given by $A = (R_\beta - R_\alpha)/v$. 4. The starting parameter is given by $C = (R_\alpha - R_0)/v$.]

$$x(\tau_0) = x_0, \quad \text{and} \quad \left\{ \left(\frac{\tau}{2} \right)^{2q-1} \frac{dx}{d\tau} \right\}_{\tau=\tau_0} = -y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1}.$$

Here

$$q = \left(\frac{\nu + 1}{\mu + \nu + 2} \right), \quad (3.10)$$

$$\tau = \left(\frac{2\lambda_I}{\mu + \nu + 2} \right) (t + C)^{(\mu + \nu + 2)/2}, \quad (3.11)$$

and

$$\tau_0 = \left(\frac{2\lambda_I}{\mu + \nu + 2} \right) C^{(\mu + \nu + 2)/2}. \quad (3.12)$$

Let us observe that $0 < q < 1$ when μ and $\nu > -1$. Furthermore, $q > 1/2$ if and only if $dR/dt < 0$, i.e. $R(t)$ is a strictly decreasing function of time.

4. Lanchester-Clifford-Schläfli (LCS) Functions.

Consider the function $F_\alpha(x)$ defined by the power series

$$F_\alpha(x) = \Gamma(\alpha) \sum_{k=0}^{\infty} \frac{(x/2)^{2k}}{\{k! \Gamma(k + \alpha)\}}. \quad (4.1)$$

For $\alpha \neq 0, -1, -2, \dots$ the radius of convergence for $F_\alpha(x)$ is infinite by the ratio test for convergence of power series [2]. Hence, $F_\alpha(z)$ is an entire function of the complex variable $z = x + iy$, with an essential

singularity at the point at infinity. Now consider the function $H_\alpha(x)$ defined by the infinite series

$$H_\alpha(x) = \Gamma(\alpha) \sum_{k=0}^{\infty} \frac{(x/2)^{2(k+\alpha)}}{\{k! \Gamma(k+\alpha+1)\}} . \quad (4.2)$$

Observing that

$$H_\alpha(x) = (1/\alpha)(x/2)^{2\alpha} F_{\alpha+1}(x) , \quad (4.3)$$

we see that for $\alpha > 0$ the infinite series (4.2) is uniformly convergent on compact subsets of the complex plane. From (4.3) one can readily deduce the recursive relation

$$F_\alpha(x) = F_{\alpha+1}(x) + \left\{ \frac{(x/2)^2}{\alpha(\alpha+1)} \right\} F_{\alpha+2}(x) . \quad (4.4)$$

We will call the functions $F_\alpha(x)$ and $H_\alpha(x)$ Lanchester-Clifford-Schl fli (LCS) functions (see Note 10 on pp. 66-67 of [5]). Other properties are readily deduced and are given in Table I.

The function $F_\alpha(x)$ satisfies the linear second-order ordinary differential equation

$$\frac{d^2 F_\alpha}{dx^2} + \left(\frac{2\alpha-1}{x} \right) \frac{dF_\alpha}{dx} - F_\alpha = 0 , \quad (4.5)$$

with initial conditions

Table I. Properties of the LCS Functions $F_{\alpha}(x)$ and $H_{\alpha}(x)$.

1. $dF_{\alpha}/dx = (x/2)^{1-2\alpha} H_{\alpha}(x)$
2. $dH_{\alpha}/dx = (x/2)^{2\alpha-1} F_{\alpha}(x)$
3. $F_{\alpha}(x)F_{1-\alpha}(x) - H_{\alpha}(x)H_{1-\alpha}(x) = 1 \quad \forall x$
where α is not an integer (including zero)
4. $F_{\alpha}(x=0) = 1$
5. $H_{\alpha}(x=0) = 0 \quad \text{for } \alpha > 0$
6. $dF_{\alpha}/dx(x=0) = 0$
7. $\{(x/2)^{1-2\alpha} dH_{\alpha}/dx\}_{x=0} = 1$
8. $F_{1/2}(x) = \cosh x$
9. $H_{1/2}(x) = \sinh x$

$$F_{\alpha}(0) = 1, \quad \text{and} \quad \frac{dF_{\alpha}}{dx}(0) = 0,$$

while $H_{\alpha}(x)$ satisfies

$$\frac{d^2 H_{\alpha}}{dx^2} - \left(\frac{2\alpha-1}{x}\right) \frac{dH_{\alpha}}{dx} - H_{\alpha} = 0, \quad (4.6)$$

with initial conditions

$$H_{\alpha}(0) = 0, \quad \text{and} \quad \left\{ \left(\frac{x}{2}\right)^{1-2\alpha} \frac{dH_{\alpha}}{dx} \right\}_{x=0} = 1.$$

Thus, $\{F_{\alpha}, H_{1-\alpha}\}$ is a fundamental system of solutions to

$$\frac{d^2 F}{dx^2} + \left(\frac{2\alpha-1}{x}\right) \frac{dF}{dx} - F = 0, \quad (4.7)$$

with Wronskian $W(F_{\alpha}, H_{1-\alpha}) = (x/2)^{1-2\alpha}$. It follows that the GLF for the X and Y force-level equations for combat modelled with the attrition-rate coefficients (3.8) are given by

$$C_X(t) = F_q(\tau(t)), \quad S_X(t) = \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1} H_p(\tau(t)), \quad (4.8)$$

$$C_Y(t) = F_p(\tau(t)), \quad S_Y(t) = \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{1-2q} H_q(\tau(t)), \quad (4.9)$$

where $p = 1-q$. If we define

$$T_{\alpha}(x) = H_{1-\alpha}(x)/F_{\alpha}(x) , \quad (4.10)$$

then

$$T_X(t) = \frac{S_X(t)}{C_X(t)} = \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1} \frac{H_p(\tau(t))}{F_q(\tau(t))} , \quad (4.11)$$

or

$$T_X(t) = \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1} T_q(\tau(t)) , \quad (4.12)$$

where $T_X(t)$ denotes a hyperbolic-like GLF, which corresponds to the hyperbolic tangent. Observing that for $\mu, \nu > -1$, $\lim_{t \rightarrow +\infty} \tau(t) = +\infty$, we see that $T_{\alpha}(x)$ is a strictly increasing function of x on the interval $[0, +\infty)$ and

$$0 \leq T_{\alpha}(x) < \frac{\Gamma(1-\alpha)}{\Gamma(\alpha)} \quad \text{for } 0 \leq x < +\infty , \quad (4.13)$$

with

$$\lim_{x \rightarrow +\infty} T_{\alpha}(x) = \frac{\Gamma(1-\alpha)}{\Gamma(\alpha)} , \quad (4.14)$$

since by the results of Taylor and Comstock [7] the parity-condition parameter $Q^* = Q^*(\mu, \nu, C = 0)$ is given by

$$\lim_{t \rightarrow +\infty} T_X(t) = \frac{1}{Q^*(\mu, \nu, 0)} = \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1} \frac{\Gamma(p)}{\Gamma(q)} . \quad (4.15)$$

We recall that Taylor and Comstock [7] have introduced the so-called parity-condition parameter Q^* as the value (or range of such values) for the initial condition Q to the initial-value problem

$$\left\{ \begin{array}{l} \frac{dE_X^-}{dt} = - \frac{1}{\sqrt{\lambda_R}} a(t) E_Y^- \quad \text{with } E_X^-(t_0) = 1, \\ \frac{dE_Y^-}{dt} = - \sqrt{\lambda_R} b(t) E_X^- \quad \text{with } E_Y^-(t_0) = Q. \end{array} \right. \quad (4.16)$$

such that $E_X^-(t; Q^*)$ and $E_Y^-(t; Q^*) > 0$ for all $t \geq t_0$. In other words, Q^* is the value of Q in (4.16) above such that neither E_X^- nor E_Y^- ever become zero. In this case, both $E_X^-(t; Q^*)$ and $E_Y^-(t; Q^*)$ are positive, strictly decreasing functions, similar to decreasing exponentials. Thus, we may call Q^* "the Y equivalent of an X force of unit strength," since the forces are "at parity," with neither force being annihilated in finite time. Taylor and Comstock have shown that for either $a(t) \notin L(0, +\infty)$ or $b(t) \notin L(0, +\infty)$, then Q^* is unique and given by

$$\lim_{t \rightarrow +\infty} \frac{S_X(t)}{C_X(t)} = \frac{1}{Q^*}. \quad (4.17)$$

The significance of the parity-condition parameter Q^* is that it allows us to predict force annihilation as the following theorem shows.

THEOREM 1 (Taylor and Comstock [7]): Assume that either $a(t) \notin L(0, +\infty)$ or $b(t) \notin L(0, +\infty)$. Then the X force will be annihilated in finite time if and only if

$$\frac{x_0}{y_0} < \sqrt{\lambda_R} \left\{ \frac{C_X(0) - Q^* S_X(0)}{Q^* C_Y(0) - S_Y(0)} \right\}. \quad (4.18)$$

5. Use of LCS Functions for Analyzing Combat.

The Lanchester-Clifford-Schläfli (LCS) functions $F_\alpha(x)$ and $H_\alpha(x)$ are useful for analyzing "aimed-fire" combat (see Section 3 above) modelled with the power attrition-rate coefficients with "no offset" (3.8), which we rewrite here as

$$a(t) = k_a (t + C)^\mu, \quad \text{and} \quad b(t) = k_b (t + C)^\nu. \quad (5.1)$$

In other words, the LCS functions arise in solving the differential combat model (2.1) with attrition-rate coefficients (5.1). In order that both $a(t)$ and $b(t) \in L(t_0, T)$, we must have μ and $\nu > -1$. Military situations modelled by these equations have been discussed in Section 3 above, e.g. combat between two weapon systems with the same maximum effective range. For such combat, the LCS functions may be used to

- (1) compute force-level declines,
- (2) predict force annihilation,
- and (3) predict the time of force annihilation.

Let us now see how the LCS functions may be used to obtain the above information about force-level declines and force-annihilation prediction. According to (2.4), (4.8), and (4.9) above, the X force level is given by

$$x(t) = x_0 \{ F_p(\tau_0) F_q(\tau(t)) - H_q(\tau_0) H_p(\tau(t)) \} \\ - y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{2q-1} \{ F_q(\tau_0) H_p(\tau(t)) - H_p(\tau_0) F_q(\tau(t)) \}, \quad (5.2)$$

where q is given by (3.10), $p = 1-q$, and $\tau(t)$ is given by (3.11), which we rewrite as

$$\tau(t) = \left(\frac{2\lambda_I}{\mu + \nu + 2} \right) (t + C)^{(\mu+\nu+2)/2}, \quad (5.3)$$

The time to annihilate the X force* is determined by $x(t_a^X) = 0$, and it follows that

$$T_q(\tau(t_a^X)) = \frac{x_0 F_p(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} H_p(\tau_0)}{x_0 H_q(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} F_q(\tau_0)}, \quad (5.4)$$

where from (4.10)

$$T_q(\tau(t)) = H_p(\tau(t))/F_q(\tau(t)), \quad (5.5)$$

and we recall that $p + q = 1$. It follows that the time to annihilate X , t_a^X , is given by

* If we multiply the first equation of (2.1) by y , the second by x , add, and integrate, we obtain

$$x(t) y(t) = x_0 y_0 - \int_0^t \{a(s) y^2(s) + b(s) x^2(s)\} ds,$$

which shows that $x(t)$ and $y(t)$ can have at most one finite zero. Hence, if $x(t_a^X) = 0$, then we know that $y(t) > 0$ for all $t \geq 0$.

$$t_a^X = \tau^{-1} \left\{ T_q^{-1} \left[\frac{x_0 F_p(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} H_p(\tau_0)}{x_0 H_q(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} F_q(\tau_0)} \right] \right\}. \quad (5.6)$$

Taylor and Comstock [7] have shown that $T_q(\tau)$ is strictly increasing and satisfies (see also (4.12) above)

$$0 \leq T_q(\tau) < \Gamma(p)/\Gamma(q), \quad (5.7)$$

where $p = 1-q$. It follows that in order for X to be annihilated in finite time, the right-hand side of (5.4) must be less than $\Gamma(p)/\Gamma(q)$. Let us observe that for $t_0 = -C = 0$, (5.4) simplifies to

$$T_q(\tau(t_a^X)) = \frac{x_0}{y_0 \sqrt{\lambda_R}} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{p-q}. \quad (5.8)$$

Thus, we have proved the following theorem concerning force-annihilation prediction.

THEOREM 2: Consider combat between two homogeneous forces modelled by (2.1) with power attrition-rate coefficients (5.1). Assume that μ and $\nu > -1$ and that the above equations hold for all time. Then the X force will be annihilated in finite time if and only if

$$\Gamma(q) \left\{ x_0 F_p(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} H_p(\tau_0) \right\} \\ < \Gamma(p) \left\{ x_0 H_q(\tau_0) + y_0 \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} F_q(\tau_0) \right\}, \quad (5.9)$$

where $q = (\nu + 1)/(\mu + \nu + 2)$ and $p = 1 - q$. For $\tau_0 = 0$ (i.e. $C = 0$ so that $\tau_0 = 0$), X will be annihilated in finite time if and only if

$$\frac{x_0}{y_0} < \frac{\Gamma(p)}{\Gamma(q)} \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p}. \quad (5.10)$$

6. Tabulation of LCS Functions.

This report contains a reduced set of tables of the Lanchester-Clifford-Schläfli functions. The Appendix contains tables of five-decimal-place values of the hyperbolic-like LCS functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ for various values of the argument x , namely $x = 0.00$ (0.01) 2.00 (0.1) 10.0, and $\alpha = 1/2, 1/3, 2/3, 1/4, 3/4, 1/5, 2/5, 3/5, 4/5, 3/7$, and $4/7$. These values of the index α correspond to $\mu, \nu = 0, 1, 2$, and 3 in (3.8) and allow one to analyze, for example, a basic spectrum of range capabilities for weapon systems in the constant-speed-attack model of Section 3. These tables have been calculated by the recursive means given in Section 8 of [5]. A more extensive tabulation (namely, for $\alpha = 1/2, 1/3, 2/3, 1/4, 3/4, 1/5, 2/5, 3/5, 4/5, 2/7, 3/7, 4/7, 5/7, 4/9, 5/9, 3/11, 5/11, 6/11, 8/11, 5/13, 8/13, 5/17, 12/17, 5/21$, and $16/21$ corresponding to $\mu, \nu = 0, 1/4, 1/2, 1, 1\frac{1}{2}, 2, 3$)

is to be found in a companion report [8]. This companion report contains the most extensive set of tables of the Lanchester-Clifford-Schläfli functions currently available.

A representative tabulation of the hyperbolic-like LCS functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ is given in, for example, Tables 8A and 8B of the Appendix for $\alpha = 3/5$. The values of the argument x are the same as those used for the tabulation of the hyperbolic functions by Abramowitz and Stegun [1]. We observe from Table 8B and (4.13) that the limiting value of $T_\alpha(x)$ as $x \rightarrow +\infty$ (here $\alpha = 3/5$) is quickly reached, with three-decimal-place accuracy already attained for $x = 4.5$. Moreover, the use of these tables (specifically, Tables 8A and 8B of the Appendix) for combat analysis is illustrated in the next section.

7. Numerical Examples

In this section we examine a couple of numerical examples to show some of the insights that may be gained into the dynamics of combat between two homogeneous forces from our results (see also [6]). These examples illustrate the use of the LCS functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ for analyzing "aimed-fire" combat modelled with the power attrition-rate coefficients with "no offset" (5.1). As in [4-7], we consider S. Bonder's model (3.2) for the constant-speed attack against a static defensive position. We will focus on the use of the LCS functions for predicting force annihilation, since the computing of force-level trajectories with Lanchester functions is adequately handled elsewhere (see [4-5]).

Let us accordingly consider the constant-speed attack of a homogeneous Y force against the static defensive position of a homogeneous X force (see Section 3 above for further modelling details, especially Figure 1). For our numerical computations, we assume that the fire effectiveness of the Y weapon system varies linearly with range, i.e.

$$\alpha(r) = \begin{cases} \alpha_0 \left(1 - \frac{r}{R_\alpha}\right) & \text{for } 0 \leq r \leq R_\alpha, \\ 0 & \text{for } R_\alpha \leq r, \end{cases} \quad (7.1)$$

and that the fire effectiveness of the X weapon system varies quadratically with range, i.e.

$$\beta(r) = \begin{cases} \beta_0 \left(1 - \frac{r}{R_\beta}\right)^2 & \text{for } 0 \leq r \leq R_\beta, \\ 0 & \text{for } R_\beta \leq r, \end{cases} \quad (7.2)$$

with $R_\alpha = R_\beta$, i.e. both weapon systems have the same maximum effective range. In other words, $\mu = 1$ in (3.4) and $\nu = 2$ for $\beta(r)$. We consider a battle modelled by the input data given in Table II. In terms of time as the independent variable, the attrition-rate coefficients (7.1) and (7.2) become via (3.3)

$$a(t) = k_a(t + C) \quad \text{and} \quad b(t) = k_b(t + C)^2, \quad (7.3)$$

Table II. Input Data for Numerical Examples

$$\mu = 1, \quad \nu = 2$$

$$\alpha_0 = 0.06 \text{ X casualties/minute/Y firer}$$

$$\beta_0 = 0.6 \text{ Y casualties/minute/X firer}$$

$$R_\alpha = R_\beta = 2000 \text{ meters}$$

$$v = 5 \text{ miles/hour}$$

where $R_\alpha = R_\beta$,

$$C = \frac{R_\alpha - R_0}{v}, \quad k_a = \frac{\alpha_0 v}{R_\alpha}, \quad \text{and} \quad k_b = \beta_0 \left(\frac{v}{R_\beta} \right)^2. \quad (7.4)$$

From the input data given in Table II, we compute the parameter values shown in Table III, since the transformed X force-level equation is given by (3.9) with $q = (v + 1)/(\mu + v + 2)$, $p = 1 - q$, $\mu = 1$, and $v = 2$. Thus, the X force level may be computed with $F_\alpha(\tau)$ and $H_{1-\alpha}(\tau)$ with $\alpha = q = 3/5$. Force-annihilation prediction involves the limiting value of $T_\alpha(\tau) = H_{1-\alpha}(\tau)/F_\alpha(\tau)$ as $\tau \rightarrow +\infty$. From Table 8B of the Appendix and Table III, we note the predicted agreement between $\Gamma(1-\alpha)/\Gamma(\alpha)$ and the limiting value of $T_\alpha(x)$ as $x \rightarrow +\infty$ [recall (4.13)] for $\alpha = q = 3/5$. We now consider two cases: (I) $R_0 = 2000$ meters, and (II) $R_0 = 1250$ meters.

When $R_0 = 2000$ meters (see Figure 3 of [4]), we have $C = 0$ and $\tau_0 = 0$. The maximum time that the battle can last is $t_{\max} = R_0/v = 14.91$ minutes, since at this time the attackers reach their final objective, i.e. the defender's position (again, see Figure 1). We now consider the qualitative behavior of the $\mu = 1$, $v = 2$ force-level trajectory shown in Figure 3 of [4]. Theorem 2 tells us that the X force can be annihilated in finite time if and only if

$$\frac{x_0}{y_0} < \frac{\Gamma(p)}{\Gamma(q)} \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + v + 2} \right)^{q-p}, \quad (7.3)$$

where $q = 3/5$ and $p = 1 - q$. Using the numerical values in Table III, we compute from (7.3) that the X force can be annihilated in finite time if and only if

Table III. Parameter Values for Numerical Examples

$$k_a = 4.0233 \times 10^{-3} \text{ X casualties/minute}^\mu/\text{Y firer}$$

$$k_b = 2.6979 \times 10^{-3} \text{ Y casualties/minute}^\nu/\text{X firer}$$

$$p = 2/5, \quad q = 3/5$$

$$\Gamma(p)/\Gamma(q) = 1.48951$$

$$A = 0$$

$$\frac{x_0}{y_0} < 0.420 . \quad (7.4)$$

When the X force can be annihilated, its annihilation time is given by (5.8), which we rewrite here as

$$T_q(\tau(t_a^X)) = \frac{x_0}{y_0 \sqrt{\lambda_R}} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{p-q} , \quad (7.5)$$

where

$$\tau(t) = \left(\frac{2\lambda_I}{\mu + \nu + 2} \right) t^{(\mu+\nu+2)/2} . \quad (7.6)$$

Thus, for the numerical values given in Table III, the time of annihilation of the X force is given by

$$T_q(\tau(t_a^X)) = 3.544 \frac{x_0}{y_0} , \quad (7.7)$$

with $q = 3/5$. We will now illustrate further computations for $x_0 = 10$ and $y_0 = 30$. From (7.4) we see that the X force can be annihilated in finite time (but we must verify that $t_a^X \leq t_{\max}$). In this case (7.7) becomes

$$T_q(\tau(t_a^X)) = 1.18122 . \quad (7.8)$$

We must now determine $\tau(t_a^X)$ such that $\tau(t_a^X) = T_q^{-1}(1.18122)$ by using interpolation methods and Tables 8A and 8B. From Table 8A, we find

$$\begin{array}{ll} T_q(\tau) = 1.18172 & \text{for } \tau = 1.01 \\ T_q(\tau) = 1.17630 & \text{for } \tau = 1.00 \end{array}$$

so that using linear interpolation, we obtain

$$\tau(t_a^X) = 1.009, \quad (7.9)$$

whence use of (7.6) yields

$$t_a^X = 14.24 \text{ minutes}, \quad (7.10)$$

which is less than $t_{\max} = 14.91$ minutes so that the defending X force is indeed annihilated before the attacking Y force reaches its final objective. Since $r(t) = R_0 - vt$, we find that force separation at the instant of annihilation of the X force is

$$r_a^X = 89.8 \text{ meters}. \quad (7.11)$$

Further results may be computed in a similar fashion and are given in Table IV.

When $R_0 = 1250$ meters (see Figure 3 of [5]), we have $C = 5.5923$ minutes, $\tau_0 = 0.0975$, and $t_{\max} = R_0/v = 9.32$ minutes. In this case Theorem 2 tells us that the X force can be annihilated in finite time if and only if

Table IV. Annihilation of the X Force as a Function
of the Initial Force Ratio for $R_0 = 2000$ meters

(x_0/y_0)	t_a^X (minutes)	r_a^X (meters)
0.333	14.24	89.8
0.250	11.61	443.2
0.200	10.19	633.2

$$\frac{x_0}{y_0} < \sqrt{\lambda_R} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{q-p} \frac{\Gamma(p)}{\Gamma(q)} \frac{\left\{ F_q(\tau_0) - \frac{\Gamma(q)}{\Gamma(p)} H_p(\tau_0) \right\}}{\left\{ F_p(\tau_0) - \frac{\Gamma(p)}{\Gamma(q)} H_q(\tau_0) \right\}}, \quad (7.12)$$

with $q = 3/5$ and $p = 1-q$. Using linear interpolation, we obtain from Tables 7A and 8A of the Appendix that for the numerical values of Table III

$$F_p(\tau_0) = 1.006, \quad H_q(\tau_0) = 0.044, \quad (7.13)$$

$$F_q(\tau_0) = 1.004, \quad H_p(\tau_0) = 0.223,$$

so that (7.12) says that the X force can be annihilated if and only if

$$\frac{x_0}{y_0} < 0.382. \quad (7.14)$$

When the X force can be annihilated, its annihilation time is given by (5.4), which we rewrite here as

$$T_q(\tau(t_a^X)) = \frac{\left\{ \frac{x_0}{y_0 \sqrt{\lambda_R}} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{p-q} F_p(\tau_0) + H_p(\tau_0) \right\}}{\left\{ F_q(\tau_0) + \frac{x_0}{y_0 \sqrt{\lambda_R}} \left(\frac{\lambda_I}{\mu + \nu + 2} \right)^{p-q} H_q(\tau_0) \right\}}, \quad (7.15)$$

whence for the data of Table III

$$T_a(\tau(t_a^X)) = \frac{3.565u_0 + 0.223}{0.156u_0 + 1.004}, \quad (7.16)$$

where $u_0 = x_0/y_0$. Let us also record here that (3.11) yields

$$t = \left(\frac{\{\mu + \nu + 2\}\tau}{2\lambda_I} \right)^{2/(\mu+\nu+2)} - C . \quad (7.17)$$

We will again illustrate further computations for $x_0 = 10$ and $y_0 = 30$.

From (7.14) we see that the X force can be annihilated in finite time (but again we must investigate whether or not $t_a^X \leq t_{\max}$). In this case (7.16) becomes

$$T_q(\tau(t_a^X)) = 1.33651 , \quad (7.18)$$

whence Table 8A of the Appendix and linear interpolation yield

$$\tau(t_a^X) = 1.397 , \quad (7.19)$$

so that by (7.17)

$$t_a^X = 10.63 \text{ minutes} . \quad (7.20)$$

Since $t_{\max} = R_0/\nu = 9.32$ minutes $< t_a^X$, we see that the attacking Y force overruns the defender's position before annihilation of the X force occurs. Thus, the battle ends with $x_f = x(t_f) > 0$ and $y_f > 0$ at $t_f = t_{\max} = 9.32$ minutes. Corresponding to $t_f = 9.32$ minutes is $\tau_f = 1.1318$, and then Table 8A of the Appendix yields

$$F_q(\tau_f = 1.1318) = 1.589 , \quad H_p(1.1318) = 1.973 , \quad (7.21)$$

whence via (2.4), (4.8), (4.9), and (7.13) we obtain

$$x_f = x(t_f) = x(r = 0) = 1.35 . \quad (7.22)$$

Some further numerical results are given in Table V. Again, these parametric results should be contrasted with the single $\mu = 1$, $\nu = 2$ force-level trajectory shown in Figure 3 of [5].

8. Final Remarks

In the previous section above, we have seen how the LCS functions allow one to conveniently obtain much valuable information about the model (2.1) with power attrition-rate coefficients (3.8) without having to explicitly compute the entire force-level trajectories. Previously we were limited to computing only force-level trajectories (see [4-5]). With the availability of these tabulations of LCS functions (see the Appendix of this report and [8]), we can now tell who is going to be annihilated and when this event will happen without having to compute the trajectories. Not only did we answer questions about the qualitative behavior of the model (e.g. force annihilation) for specific values of, for example, initial force levels but also for a range of values of the initial force ratio (i.e. parametric analysis of model behavior).

Table V. Annihilation of the X Force as a Function
of the Initial Force Ratio for $R_0 = 1250$ meters

(x_0/y_0)	t_a^X (minutes)	r_a^X (meters)
0.333	10.63	----- [†]
0.250	7.56	235.9
0.200	6.17	422.8

[†] $t_{\max} = 9.32$ minutes and $x_f = x(r=0) = 1.35$.

The results of this report may be used for other parametric analyses, e.g. parametric dependence of battle outcome on attrition-rate coefficients. Thus, the contents of this report allow one to develop important insights into the dynamics of combat between two homogeneous forces with temporal variations in fire effectiveness. With the availability of tabulations of the LCS functions, one can now analyze such combat modelled by the power attrition-rate coefficients (3.8) with somewhat the same facility as he can for the constant-coefficient case and thus aid in parametric analyses. For further discussions of the significance of such results for military operations research, the reader is directed to [6] and [7].

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APPENDIX: Tabulation of the LCS Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for
 $\alpha = 1/2, 1/3, 2/3, 1/4, 3/4, 1/5, 2/5, 3/5, 4/5, 3/7$, and $4/7$.

x	$F_{1/2}(x)$	$H_{1/2}(x)$	$T_{1/2}(x)$	x	$F_{1/2}(x)$	$H_{1/2}(x)$	$T_{1/2}(x)$	x	$F_{1/2}(x)$	$H_{1/2}(x)$	$T_{1/2}(x)$
0.0	1.0000	0.0	0.0	0.50	1.2763	0.5210	0.4621	1.00	1.54308	1.1750	0.76159
0.01	1.0005	0.02000	0.02000	0.51	1.2827	0.5275	0.4719	1.01	1.5491	1.1806	0.76516
0.02	1.0010	0.04000	0.04000	0.52	1.2891	0.5340	0.4817	1.02	1.5552	1.1862	0.76873
0.03	1.0015	0.06000	0.06000	0.53	1.2955	0.5405	0.4915	1.03	1.5613	1.1918	0.77230
0.04	1.0020	0.08000	0.08000	0.54	1.3019	0.5470	0.5013	1.04	1.5674	1.1974	0.77587
0.05	1.0025	0.10000	0.10000	0.55	1.3083	0.5535	0.5111	1.05	1.5735	1.2030	0.77944
0.06	1.0030	0.12000	0.12000	0.56	1.3147	0.5600	0.5209	1.06	1.5796	1.2086	0.78301
0.07	1.0035	0.14000	0.14000	0.57	1.3211	0.5665	0.5307	1.07	1.5857	1.2142	0.78658
0.08	1.0040	0.16000	0.16000	0.58	1.3275	0.5730	0.5405	1.08	1.5918	1.2198	0.79015
0.09	1.0045	0.18000	0.18000	0.59	1.3339	0.5795	0.5503	1.09	1.5979	1.2254	0.79372
0.10	1.0050	0.20000	0.20000	0.60	1.3403	0.5860	0.5601	1.10	1.6040	1.2310	0.79729
0.11	1.0055	0.22000	0.22000	0.61	1.3467	0.5925	0.5699	1.11	1.6101	1.2366	0.80086
0.12	1.0060	0.24000	0.24000	0.62	1.3531	0.5990	0.5797	1.12	1.6162	1.2422	0.80443
0.13	1.0065	0.26000	0.26000	0.63	1.3595	0.6055	0.5895	1.13	1.6223	1.2478	0.80800
0.14	1.0070	0.28000	0.28000	0.64	1.3659	0.6120	0.5993	1.14	1.6284	1.2534	0.81157
0.15	1.0075	0.30000	0.30000	0.65	1.3723	0.6185	0.6091	1.15	1.6345	1.2590	0.81514
0.16	1.0080	0.32000	0.32000	0.66	1.3787	0.6250	0.6189	1.16	1.6406	1.2646	0.81871
0.17	1.0085	0.34000	0.34000	0.67	1.3851	0.6315	0.6287	1.17	1.6467	1.2702	0.82228
0.18	1.0090	0.36000	0.36000	0.68	1.3915	0.6380	0.6385	1.18	1.6528	1.2758	0.82585
0.19	1.0095	0.38000	0.38000	0.69	1.3979	0.6445	0.6483	1.19	1.6589	1.2814	0.82942
0.20	1.0100	0.40000	0.40000	0.70	1.4043	0.6510	0.6581	1.20	1.6650	1.2870	0.83299
0.21	1.0105	0.42000	0.42000	0.71	1.4107	0.6575	0.6679	1.21	1.6711	1.2926	0.83656
0.22	1.0110	0.44000	0.44000	0.72	1.4171	0.6640	0.6777	1.22	1.6772	1.2982	0.84013
0.23	1.0115	0.46000	0.46000	0.73	1.4235	0.6705	0.6875	1.23	1.6833	1.3038	0.84370
0.24	1.0120	0.48000	0.48000	0.74	1.4299	0.6770	0.6973	1.24	1.6894	1.3094	0.84727
0.25	1.0125	0.50000	0.50000	0.75	1.4363	0.6835	0.7071	1.25	1.6955	1.3150	0.85084
0.26	1.0130	0.52000	0.52000	0.76	1.4427	0.6900	0.7169	1.26	1.7016	1.3206	0.85441
0.27	1.0135	0.54000	0.54000	0.77	1.4491	0.6965	0.7267	1.27	1.7077	1.3262	0.85798
0.28	1.0140	0.56000	0.56000	0.78	1.4555	0.7030	0.7365	1.28	1.7138	1.3318	0.86155
0.29	1.0145	0.58000	0.58000	0.79	1.4619	0.7095	0.7463	1.29	1.7199	1.3374	0.86512
0.30	1.0150	0.60000	0.60000	0.80	1.4683	0.7160	0.7561	1.30	1.7260	1.3430	0.86869
0.31	1.0155	0.62000	0.62000	0.81	1.4747	0.7225	0.7659	1.31	1.7321	1.3486	0.87226
0.32	1.0160	0.64000	0.64000	0.82	1.4811	0.7290	0.7757	1.32	1.7382	1.3542	0.87583
0.33	1.0165	0.66000	0.66000	0.83	1.4875	0.7355	0.7855	1.33	1.7443	1.3598	0.87940
0.34	1.0170	0.68000	0.68000	0.84	1.4939	0.7420	0.7953	1.34	1.7504	1.3654	0.88297
0.35	1.0175	0.70000	0.70000	0.85	1.5003	0.7485	0.8051	1.35	1.7565	1.3710	0.88654
0.36	1.0180	0.72000	0.72000	0.86	1.5067	0.7550	0.8149	1.36	1.7626	1.3766	0.89011
0.37	1.0185	0.74000	0.74000	0.87	1.5131	0.7615	0.8247	1.37	1.7687	1.3822	0.89368
0.38	1.0190	0.76000	0.76000	0.88	1.5195	0.7680	0.8345	1.38	1.7748	1.3878	0.89725
0.39	1.0195	0.78000	0.78000	0.89	1.5259	0.7745	0.8443	1.39	1.7809	1.3934	0.90082
0.40	1.0200	0.80000	0.80000	0.90	1.5323	0.7810	0.8541	1.40	1.7870	1.3990	0.90439
0.41	1.0205	0.82000	0.82000	0.91	1.5387	0.7875	0.8639	1.41	1.7931	1.4046	0.90796
0.42	1.0210	0.84000	0.84000	0.92	1.5451	0.7940	0.8737	1.42	1.7992	1.4102	0.91153
0.43	1.0215	0.86000	0.86000	0.93	1.5515	0.8005	0.8835	1.43	1.8053	1.4158	0.91510
0.44	1.0220	0.88000	0.88000	0.94	1.5579	0.8070	0.8933	1.44	1.8114	1.4214	0.91867
0.45	1.0225	0.90000	0.90000	0.95	1.5643	0.8135	0.9031	1.45	1.8175	1.4270	0.92224
0.46	1.0230	0.92000	0.92000	0.96	1.5707	0.8200	0.9129	1.46	1.8236	1.4326	0.92581
0.47	1.0235	0.94000	0.94000	0.97	1.5771	0.8265	0.9227	1.47	1.8297	1.4382	0.92938
0.48	1.0240	0.96000	0.96000	0.98	1.5835	0.8330	0.9325	1.48	1.8358	1.4438	0.93295
0.49	1.0245	0.98000	0.98000	0.99	1.5899	0.8395	0.9423	1.49	1.8419	1.4494	0.93652
0.50	1.0250	1.00000	1.00000	1.00	1.5963	0.8460	0.9521	1.50	1.8480	1.4550	0.94009

TABLE 1A. Lanchester-Clifford-Schlafli Functions $F_\alpha(x)$, $H_\alpha(x)$, and $T_\alpha(x)$ for $\alpha = 1/2$ and x from 0.00 to 1.50.

α	$F_{1/2}(\alpha)$	$H_{1/2}(\alpha)$	$T_{1/2}(\alpha)$	α	$F_{1/2}(\alpha)$	$H_{1/2}(\alpha)$	$T_{1/2}(\alpha)$	α	$F_{1/2}(\alpha)$	$H_{1/2}(\alpha)$	$T_{1/2}(\alpha)$
1.50	2.33231	2.1928	0.90515	2.0	3.76220	3.62686	0.86403	6.0	201.71564	201.71316	0.99999
1.51	2.33330	2.1930	0.90594	2.1	3.76220	3.62686	0.86403	6.1	201.71564	201.71316	0.99999
1.52	2.33429	2.1931	0.90673	2.2	3.76220	3.62686	0.86403	6.2	201.71564	201.71316	0.99999
1.53	2.33528	2.1932	0.90752	2.3	3.76220	3.62686	0.86403	6.3	201.71564	201.71316	0.99999
1.54	2.33627	2.1933	0.90831	2.4	3.76220	3.62686	0.86403	6.4	201.71564	201.71316	0.99999
1.55	2.33726	2.1934	0.90910	2.5	3.76220	3.62686	0.86403	6.5	201.71564	201.71316	0.99999
1.56	2.33825	2.1935	0.90989	2.6	3.76220	3.62686	0.86403	6.6	201.71564	201.71316	0.99999
1.57	2.33924	2.1936	0.91068	2.7	3.76220	3.62686	0.86403	6.7	201.71564	201.71316	0.99999
1.58	2.34023	2.1937	0.91147	2.8	3.76220	3.62686	0.86403	6.8	201.71564	201.71316	0.99999
1.59	2.34122	2.1938	0.91226	2.9	3.76220	3.62686	0.86403	6.9	201.71564	201.71316	0.99999
1.60	2.34221	2.1939	0.91305	3.0	3.76220	3.62686	0.86403	7.0	201.71564	201.71316	0.99999
1.61	2.34320	2.1940	0.91384	3.1	3.76220	3.62686	0.86403	7.1	201.71564	201.71316	0.99999
1.62	2.34419	2.1941	0.91463	3.2	3.76220	3.62686	0.86403	7.2	201.71564	201.71316	0.99999
1.63	2.34518	2.1942	0.91542	3.3	3.76220	3.62686	0.86403	7.3	201.71564	201.71316	0.99999
1.64	2.34617	2.1943	0.91621	3.4	3.76220	3.62686	0.86403	7.4	201.71564	201.71316	0.99999
1.65	2.34716	2.1944	0.91700	3.5	3.76220	3.62686	0.86403	7.5	201.71564	201.71316	0.99999
1.66	2.34815	2.1945	0.91779	3.6	3.76220	3.62686	0.86403	7.6	201.71564	201.71316	0.99999
1.67	2.34914	2.1946	0.91858	3.7	3.76220	3.62686	0.86403	7.7	201.71564	201.71316	0.99999
1.68	2.35013	2.1947	0.91937	3.8	3.76220	3.62686	0.86403	7.8	201.71564	201.71316	0.99999
1.69	2.35112	2.1948	0.92016	3.9	3.76220	3.62686	0.86403	7.9	201.71564	201.71316	0.99999
1.70	2.35211	2.1949	0.92095	4.0	3.76220	3.62686	0.86403	8.0	201.71564	201.71316	0.99999
1.71	2.35310	2.1950	0.92174	4.1	3.76220	3.62686	0.86403	8.1	201.71564	201.71316	0.99999
1.72	2.35409	2.1951	0.92253	4.2	3.76220	3.62686	0.86403	8.2	201.71564	201.71316	0.99999
1.73	2.35508	2.1952	0.92332	4.3	3.76220	3.62686	0.86403	8.3	201.71564	201.71316	0.99999
1.74	2.35607	2.1953	0.92411	4.4	3.76220	3.62686	0.86403	8.4	201.71564	201.71316	0.99999
1.75	2.35706	2.1954	0.92490	4.5	3.76220	3.62686	0.86403	8.5	201.71564	201.71316	0.99999
1.76	2.35805	2.1955	0.92569	4.6	3.76220	3.62686	0.86403	8.6	201.71564	201.71316	0.99999
1.77	2.35904	2.1956	0.92648	4.7	3.76220	3.62686	0.86403	8.7	201.71564	201.71316	0.99999
1.78	2.36003	2.1957	0.92727	4.8	3.76220	3.62686	0.86403	8.8	201.71564	201.71316	0.99999
1.79	2.36102	2.1958	0.92806	4.9	3.76220	3.62686	0.86403	8.9	201.71564	201.71316	0.99999
1.80	2.36201	2.1959	0.92885	5.0	3.76220	3.62686	0.86403	9.0	201.71564	201.71316	0.99999
1.81	2.36300	2.1960	0.92964	5.1	3.76220	3.62686	0.86403	9.1	201.71564	201.71316	0.99999
1.82	2.36399	2.1961	0.93043	5.2	3.76220	3.62686	0.86403	9.2	201.71564	201.71316	0.99999
1.83	2.36498	2.1962	0.93122	5.3	3.76220	3.62686	0.86403	9.3	201.71564	201.71316	0.99999
1.84	2.36597	2.1963	0.93201	5.4	3.76220	3.62686	0.86403	9.4	201.71564	201.71316	0.99999
1.85	2.36696	2.1964	0.93280	5.5	3.76220	3.62686	0.86403	9.5	201.71564	201.71316	0.99999
1.86	2.36795	2.1965	0.93359	5.6	3.76220	3.62686	0.86403	9.6	201.71564	201.71316	0.99999
1.87	2.36894	2.1966	0.93438	5.7	3.76220	3.62686	0.86403	9.7	201.71564	201.71316	0.99999
1.88	2.36993	2.1967	0.93517	5.8	3.76220	3.62686	0.86403	9.8	201.71564	201.71316	0.99999
1.89	2.37092	2.1968	0.93596	5.9	3.76220	3.62686	0.86403	9.9	201.71564	201.71316	0.99999
1.90	2.37191	2.1969	0.93675	6.0	3.76220	3.62686	0.86403	10.0	201.71564	201.71316	0.99999
1.91	2.37290	2.1970	0.93754								
1.92	2.37389	2.1971	0.93833								
1.93	2.37488	2.1972	0.93912								
1.94	2.37587	2.1973	0.93991								
1.95	2.37686	2.1974	0.94070								
1.96	2.37785	2.1975	0.94149								
1.97	2.37884	2.1976	0.94228								
1.98	2.37983	2.1977	0.94307								
1.99	2.38082	2.1978	0.94386								
2.00	2.38181	2.1979	0.94465								

TABLE 1B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 1/2$ and x from 1.50 to 10.0.

x	$F_{1/3}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$	x	$F_{1/3}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$	x	$F_{1/3}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$
0.0	1.00000	0.0	0.0	1.0	1.19193	0.2420	0.20511	1.0	1.8267	0.6885	0.37769
0.01	1.00008	0.00128	0.00128	1.01	1.19988	0.23514	0.21033	1.01	1.8096	0.68025	0.38009
0.02	1.00016	0.00323	0.00323	1.02	1.20799	0.22819	0.21498	1.02	1.7927	0.67175	0.38249
0.03	1.00028	0.00555	0.00555	1.03	1.21628	0.22127	0.21971	1.03	1.7760	0.66328	0.38484
0.04	1.00120	0.00815	0.00815	1.04	1.22474	0.21437	0.22441	1.04	1.7595	0.65478	0.38714
0.05	1.00198	0.01097	0.01095	1.05	1.23338	0.20749	0.22904	1.05	1.7431	0.64626	0.38945
0.06	1.00270	0.01399	0.01395	1.06	1.24219	0.20063	0.23367	1.06	1.7267	0.63772	0.39176
0.07	1.00338	0.01719	0.01712	1.07	1.25118	0.19379	0.23829	1.07	1.7104	0.62917	0.39407
0.08	1.00408	0.02055	0.02049	1.08	1.26035	0.18697	0.24291	1.08	1.6941	0.62061	0.39638
0.09	1.00481	0.02405	0.02399	1.09	1.26969	0.18017	0.24753	1.09	1.6778	0.61205	0.39869
0.1	1.00557	0.02767	0.02759	1.1	1.27923	0.17339	0.25215	1.1	1.6615	0.60349	0.40100
0.11	1.00635	0.03143	0.03135	1.11	1.28893	0.16663	0.25677	1.11	1.6452	0.59493	0.40331
0.12	1.00715	0.03531	0.03523	1.12	1.29881	0.15989	0.26139	1.12	1.6289	0.58637	0.40562
0.13	1.00797	0.03930	0.03922	1.13	1.30891	0.15317	0.26601	1.13	1.6126	0.57781	0.40793
0.14	1.00881	0.04340	0.04332	1.14	1.31917	0.14647	0.27063	1.14	1.5963	0.56925	0.41024
0.15	1.00967	0.04760	0.04752	1.15	1.32957	0.13979	0.27525	1.15	1.5799	0.56069	0.41255
0.16	1.01055	0.05190	0.05182	1.16	1.34011	0.13313	0.27987	1.16	1.5636	0.55213	0.41486
0.17	1.01145	0.05630	0.05622	1.17	1.35079	0.12649	0.28449	1.17	1.5472	0.54357	0.41717
0.18	1.01237	0.06079	0.06071	1.18	1.36161	0.11987	0.28911	1.18	1.5309	0.53501	0.41948
0.19	1.01331	0.06537	0.06529	1.19	1.37257	0.11327	0.29373	1.19	1.5145	0.52645	0.42179
0.2	1.01427	0.07004	0.06996	1.2	1.38367	0.10669	0.29835	1.2	1.4981	0.51789	0.42410
0.21	1.01525	0.07480	0.07472	1.21	1.39491	0.10013	0.30297	1.21	1.4817	0.50933	0.42641
0.22	1.01625	0.07965	0.07957	1.22	1.40629	0.09359	0.30759	1.22	1.4653	0.50077	0.42872
0.23	1.01727	0.08459	0.08451	1.23	1.41781	0.08707	0.31221	1.23	1.4489	0.49221	0.43103
0.24	1.01831	0.08962	0.08954	1.24	1.42947	0.08057	0.31683	1.24	1.4325	0.48365	0.43334
0.25	1.01937	0.09474	0.09466	1.25	1.44127	0.07409	0.32145	1.25	1.4161	0.47509	0.43565
0.26	1.02045	0.09995	0.09987	1.26	1.45321	0.06763	0.32607	1.26	1.3997	0.46653	0.43796
0.27	1.02155	0.10525	0.10517	1.27	1.46529	0.06119	0.33069	1.27	1.3833	0.45797	0.44027
0.28	1.02267	0.11064	0.11056	1.28	1.47751	0.05477	0.33531	1.28	1.3669	0.44941	0.44258
0.29	1.02381	0.11612	0.11604	1.29	1.48987	0.04837	0.33993	1.29	1.3505	0.44085	0.44489
0.3	1.02497	0.12169	0.12161	1.3	1.50237	0.04199	0.34455	1.3	1.3341	0.43229	0.44720
0.31	1.02615	0.12735	0.12727	1.31	1.51501	0.03563	0.34917	1.31	1.3177	0.42373	0.44951
0.32	1.02735	0.13310	0.13302	1.32	1.52779	0.02929	0.35379	1.32	1.3013	0.41517	0.45182
0.33	1.02857	0.13893	0.13885	1.33	1.54071	0.02297	0.35841	1.33	1.2849	0.40661	0.45413
0.34	1.02981	0.14484	0.14476	1.34	1.55377	0.01667	0.36303	1.34	1.2685	0.39805	0.45644
0.35	1.03107	0.15083	0.15075	1.35	1.56697	0.01039	0.36765	1.35	1.2521	0.38949	0.45875
0.36	1.03235	0.15690	0.15682	1.36	1.58031	0.00413	0.37227	1.36	1.2357	0.38093	0.46106
0.37	1.03365	0.16304	0.16296	1.37	1.59379	0.00000	0.37689	1.37	1.2193	0.37237	0.46337
0.38	1.03497	0.16925	0.16917	1.38	1.60741	0.00000	0.38151	1.38	1.2029	0.36381	0.46568
0.39	1.03631	0.17554	0.17546	1.39	1.62117	0.00000	0.38613	1.39	1.1865	0.35525	0.46799
0.4	1.03767	0.18191	0.18183	1.4	1.63507	0.00000	0.39075	1.4	1.1701	0.34669	0.47030
0.41	1.03905	0.18836	0.18828	1.41	1.64911	0.00000	0.39537	1.41	1.1537	0.33813	0.47261
0.42	1.04045	0.19488	0.19480	1.42	1.66329	0.00000	0.39999	1.42	1.1373	0.32957	0.47492
0.43	1.04187	0.20147	0.20139	1.43	1.67761	0.00000	0.40461	1.43	1.1209	0.32101	0.47723
0.44	1.04331	0.20813	0.20805	1.44	1.69207	0.00000	0.40923	1.44	1.1045	0.31245	0.47954
0.45	1.04477	0.21486	0.21478	1.45	1.70667	0.00000	0.41385	1.45	1.0881	0.30389	0.48185
0.46	1.04625	0.22166	0.22158	1.46	1.72141	0.00000	0.41847	1.46	1.0717	0.29533	0.48416
0.47	1.04775	0.22852	0.22844	1.47	1.73629	0.00000	0.42309	1.47	1.0553	0.28677	0.48647
0.48	1.04927	0.23544	0.23536	1.48	1.75131	0.00000	0.42771	1.48	1.0389	0.27821	0.48878
0.49	1.05081	0.24242	0.24234	1.49	1.76647	0.00000	0.43233	1.49	1.0225	0.26965	0.49109
0.5	1.05237	0.24946	0.24938	1.5	1.78177	0.00000	0.43695	1.5	1.0061	0.26109	0.49340
0.50	1.05395	0.25656	0.25648	1.50	1.79721	0.00000	0.44157	1.50	0.9897	0.25253	0.49571

TABLE 2A. Lanchester-Clifford-Schlöfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 1/3$ and x from 0.00 to 1.50.

x	$F_{1/3}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$	x	$F_{1-\alpha}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$	x	$F_{1-\alpha}(x)$	$H_{2/3}(x)$	$T_{1/3}(x)$
1.0	3.07330	1.40540	0.45729	2.0	5.29834	2.58494	0.48788	6.0	359.67982	181.79456	0.50546
1.1	3.10669	1.42263	0.45825	2.2	5.39006	2.59135	0.48910	6.2	346.91522	180.53471	0.50546
1.2	3.14047	1.44004	0.45918	2.4	5.48009	2.60280	0.49059	6.4	334.91515	179.27493	0.50547
1.3	3.17464	1.46064	0.46010	2.6	5.57009	2.61426	0.49165	6.6	322.91515	178.01493	0.50547
1.4	3.20920	1.47943	0.46100	2.8	5.66009	2.62572	0.49265	6.8	310.91515	176.75493	0.50547
1.5	3.24410	1.49590	0.46188	3.0	5.75009	2.63718	0.49365	7.0	298.91515	175.49493	0.50547
1.6	3.27957	1.51127	0.46274	3.2	5.84009	2.64864	0.49465	7.2	286.91515	174.23493	0.50547
1.7	3.31544	1.52652	0.46359	3.4	5.93009	2.66010	0.49565	7.4	274.91515	172.97493	0.50547
1.8	3.35180	1.54169	0.46442	3.6	6.02009	2.67156	0.49665	7.6	262.91515	171.71493	0.50547
1.9	3.38862	1.55678	0.46524	3.8	6.11009	2.68302	0.49765	7.8	250.91515	170.45493	0.50547
2.0	3.42501	1.57179	0.46603	4.0	6.20009	2.69448	0.49865	8.0	238.91515	169.19493	0.50547
2.1	3.46193	1.58672	0.46682	4.2	6.29009	2.70594	0.49965	8.2	226.91515	167.93493	0.50547
2.2	3.49938	1.60157	0.46759	4.4	6.38009	2.71740	0.50065	8.4	214.91515	166.67493	0.50547
2.3	3.53737	1.61634	0.46834	4.6	6.47009	2.72886	0.50165	8.6	202.91515	165.41493	0.50547
2.4	3.57582	1.63103	0.46908	4.8	6.56009	2.74032	0.50265	8.8	190.91515	164.15493	0.50547
2.5	3.61474	1.64564	0.46979	5.0	6.65009	2.75178	0.50365	9.0	178.91515	162.89493	0.50547
2.6	3.65413	1.66017	0.47049	5.2	6.74009	2.76324	0.50465	9.2	166.91515	161.63493	0.50547
2.7	3.69400	1.67462	0.47119	5.4	6.83009	2.77470	0.50565	9.4	154.91515	160.37493	0.50547
2.8	3.73435	1.68900	0.47189	5.6	6.92009	2.78616	0.50665	9.6	142.91515	159.11493	0.50547
2.9	3.77519	1.70331	0.47259	5.8	7.01009	2.79762	0.50765	9.8	130.91515	157.85493	0.50547
3.0	3.81653	1.71756	0.47329	6.0	7.10009	2.80908	0.50865	10.0	118.91515	156.59493	0.50547
3.1	3.85837	1.73174	0.47399								
3.2	3.90071	1.74585	0.47469								
3.3	3.94355	1.75989	0.47539								
3.4	3.98689	1.77386	0.47609								
3.5	4.03073	1.78776	0.47679								
3.6	4.07507	1.80159	0.47749								
3.7	4.11991	1.81535	0.47819								
3.8	4.16525	1.82904	0.47889								
3.9	4.21109	1.84266	0.47959								
4.0	4.25743	1.85621	0.48029								
4.1	4.30427	1.86969	0.48099								
4.2	4.35161	1.88310	0.48169								
4.3	4.39945	1.89644	0.48239								
4.4	4.44779	1.90971	0.48309								
4.5	4.49663	1.92291	0.48379								
4.6	4.54597	1.93604	0.48449								
4.7	4.59581	1.94910	0.48519								
4.8	4.64615	1.96209	0.48589								
4.9	4.69700	1.97501	0.48659								
5.0	4.74834	1.98786	0.48729								
5.1	4.79918	2.00064	0.48799								
5.2	4.85052	2.01335	0.48869								
5.3	4.90236	2.02600	0.48939								
5.4	4.95470	2.03859	0.49009								
5.5	5.00754	2.05112	0.49079								
5.6	5.06088	2.06359	0.49149								
5.7	5.11472	2.07600	0.49219								
5.8	5.16906	2.08835	0.49289								
5.9	5.22390	2.10064	0.49359								
6.0	5.27924	2.11287	0.49429								
6.1	5.33508	2.12504	0.49499								
6.2	5.39142	2.13715	0.49569								
6.3	5.44826	2.14920	0.49639								
6.4	5.50560	2.16119	0.49709								
6.5	5.56344	2.17312	0.49779								
6.6	5.62178	2.18500	0.49849								
6.7	5.68062	2.19683	0.49919								
6.8	5.73996	2.20861	0.49989								
6.9	5.79980	2.22034	0.50059								
7.0	5.86014	2.23202	0.50129								
7.1	5.92098	2.24365	0.50199								
7.2	5.98232	2.25523	0.50269								
7.3	6.04416	2.26676	0.50339								
7.4	6.10650	2.27824	0.50409								
7.5	6.16934	2.28967	0.50479								
7.6	6.23268	2.30105	0.50549								
7.7	6.29652	2.31238	0.50619								
7.8	6.36086	2.32366	0.50689								
7.9	6.42570	2.33489	0.50759								
8.0	6.49104	2.34607	0.50829								
8.1	6.55688	2.35720	0.50899								
8.2	6.62322	2.36828	0.50969								
8.3	6.68906	2.37931	0.51039								
8.4	6.75540	2.39029	0.51109								
8.5	6.82224	2.40122	0.51179								
8.6	6.88958	2.41210	0.51249								
8.7	6.95742	2.42293	0.51319								
8.8	7.02576	2.43371	0.51389								
8.9	7.09460	2.44444	0.51459								
9.0	7.16394	2.45512	0.51529								
9.1	7.23378	2.46575	0.51599								
9.2	7.30412	2.47633	0.51669								
9.3	7.37496	2.48686	0.51739								
9.4	7.44630	2.49734	0.51809								
9.5	7.51814	2.50777	0.51879								
9.6	7.59048	2.51815	0.51949								
9.7	7.66332	2.52848	0.52019								
9.8	7.73666	2.53876	0.52089								
9.9	7.81050	2.54900	0.52159								
10.0	7.88484	2.55919	0.52229								
10.1	7.95968	2.56934	0.52299								
10.2	8.03502	2.57944	0.52369								
10.3	8.11086	2.58949	0.52439								
10.4	8.18720	2.59949	0.52509								
10.5	8.26404	2.60944	0.52579								
10.6	8.34138	2.61934	0.52649								
10.7	8.41922	2.62919	0.52719								
10.8	8.49756	2.63899	0.52789								
10.9	8.57640	2.64874	0.52859								
11.0	8.65574	2.65844	0.52929								
11.1	8.73558	2.66809	0.52999								
11.2	8.81592	2.67769	0.53069								
11.3	8.89676	2.68724	0.53139								
11.4	8.97810	2.69674	0.53209								
11.5	9.05994	2.70619	0.53279								
11.6	9.14228	2.71559	0.53349								
11.7	9.22512	2.72494	0.53419								
11.8	9.30846	2.73424	0.53489								
11.9	9.39230	2.74349	0.53559								
12.0	9.47664	2.75269	0.53629								
12.1	9.56148	2.76184	0.53699								
12.2	9.64682	2.77094	0.53769								
12.3	9.73266	2.78000	0.53839								
12.4	9.81900	2.78901	0.53909								
12.5	9.90584	2.79797	0.53979								
12.6	9.99318	2.80689	0.54049								
12.7	10.08092	2.81576	0.54119								
12.8	10.16916	2.82459	0.54189								
12.9	10.25790	2.83337	0.54259								
13.0	10.34714	2.84210	0.54329								
13.1	10.43688	2.85079	0.54399								
13.2	10.52712	2.85944	0.54469								
13.3	10.61786	2.86804	0.54539								
13.4	10.70910	2.87659	0.54609								
13.5	10.80084	2.88509	0.54679								
13.6	10.89308	2.89354	0.54749								
13.7	10.98582	2.90194	0.54819								
13.8	11.07906	2.91029	0.54889								
13.9	11.17280	2.91859	0.54959								
14.0	11.26704	2.92684	0.55029								
14.1	11.36178	2.93504	0.55099								
14.2	11.45702	2.94319	0.55169								
14.3	11.55276	2.95129	0.55239								
14.4	11.64900	2.95934	0.55309								
14.5	11.74574	2.96734	0.55379								
14.6											

TABLE 2B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for $\alpha = 1/3$ and x from 1.50 to 10.0.

x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$	x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$	x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$
0.0	1.00000	0.08772	0.0	0.50	1.09552	1.2711	1.19317	1.00	1.40402	2.26870	1.61230
0.01	1.00004	0.08772	0.08772	0.51	1.09996	1.27603	1.19514	1.01	1.41270	2.26974	1.61664
0.02	1.00015	0.13326	0.13326	0.52	1.10337	1.28095	1.19746	1.02	1.42160	2.27078	1.62093
0.03	1.00034	0.18220	0.18220	0.53	1.11176	1.28589	1.19985	1.03	1.43069	2.27182	1.62518
0.04	1.00060	0.22211	0.22038	0.54	1.11716	1.29083	1.19885	1.04	1.43964	2.27286	1.62938
0.05	1.00094	0.25662	0.25333	0.55	1.12049	1.29577	1.20049	1.05	1.44853	2.27390	1.63355
0.06	1.00135	0.28946	0.28374	0.56	1.12283	1.30071	1.20213	1.06	1.45735	2.27494	1.63769
0.07	1.00180	0.32110	0.31737	0.57	1.12518	1.30565	1.20377	1.07	1.46610	2.27598	1.64181
0.08	1.00230	0.35073	0.34903	0.58	1.12753	1.31059	1.20541	1.08	1.47479	2.27702	1.64591
0.09	1.00284	0.37846	0.37455	0.59	1.12989	1.31553	1.20705	1.09	1.48341	2.27806	1.65001
0.1	1.00341	0.40413	0.40166	0.6	1.13225	1.32047	1.20869	1.1	1.49196	2.27910	1.65410
0.11	1.00401	0.42789	0.42442	0.61	1.13461	1.32541	1.21033	1.11	1.50053	2.28014	1.65819
0.12	1.00464	0.44963	0.44514	0.62	1.13697	1.33035	1.21207	1.12	1.50911	2.28118	1.66226
0.13	1.00530	0.46937	0.46389	0.63	1.13933	1.33529	1.21381	1.13	1.51770	2.28222	1.66631
0.14	1.00598	0.48712	0.48064	0.64	1.14169	1.34023	1.21555	1.14	1.52630	2.28326	1.67035
0.15	1.00668	0.50287	0.49439	0.65	1.14405	1.34517	1.21729	1.15	1.53491	2.28430	1.67438
0.16	1.00739	0.51662	0.50614	0.66	1.14641	1.35011	1.21903	1.16	1.54353	2.28534	1.67840
0.17	1.00812	0.52837	0.51589	0.67	1.14877	1.35505	1.22077	1.17	1.55216	2.28638	1.68241
0.18	1.00886	0.53811	0.52363	0.68	1.15113	1.35999	1.22251	1.18	1.56080	2.28742	1.68641
0.19	1.00961	0.54684	0.52937	0.69	1.15349	1.36493	1.22425	1.19	1.56945	2.28846	1.69039
0.2	1.01037	0.55457	0.53310	0.7	1.15585	1.36987	1.22600	1.2	1.57811	2.28950	1.69436
0.21	1.01114	0.56130	0.53583	0.71	1.15821	1.37481	1.22774	1.21	1.58678	2.29054	1.69831
0.22	1.01192	0.56703	0.53856	0.72	1.16057	1.37975	1.22948	1.22	1.59546	2.29158	1.70225
0.23	1.01270	0.57176	0.54129	0.73	1.16293	1.38469	1.23122	1.23	1.60414	2.29262	1.70618
0.24	1.01349	0.57549	0.54402	0.74	1.16529	1.38963	1.23296	1.24	1.61283	2.29366	1.71010
0.25	1.01428	0.57822	0.54675	0.75	1.16765	1.39457	1.23470	1.25	1.62153	2.29470	1.71401
0.26	1.01507	0.58095	0.54948	0.76	1.16999	1.39951	1.23644	1.26	1.63024	2.29574	1.71791
0.27	1.01586	0.58368	0.55221	0.77	1.17235	1.40445	1.23818	1.27	1.63896	2.29678	1.72180
0.28	1.01665	0.58641	0.55494	0.78	1.17471	1.40939	1.23992	1.28	1.64769	2.29782	1.72568
0.29	1.01744	0.58914	0.55767	0.79	1.17707	1.41433	1.24166	1.29	1.65643	2.29886	1.72955
0.3	1.01823	0.59187	0.56040	0.8	1.17943	1.41927	1.24340	1.3	1.66518	2.29990	1.73341
0.31	1.01902	0.59460	0.56313	0.81	1.18179	1.42421	1.24514	1.31	1.67394	2.30094	1.73726
0.32	1.01981	0.59733	0.56586	0.82	1.18415	1.42915	1.24688	1.32	1.68271	2.30198	1.74110
0.33	1.02060	0.59999	0.56859	0.83	1.18651	1.43409	1.24862	1.33	1.69149	2.30302	1.74494
0.34	1.02139	0.60266	0.57132	0.84	1.18887	1.43903	1.25036	1.34	1.70028	2.30406	1.74877
0.35	1.02218	0.60533	0.57405	0.85	1.19123	1.44397	1.25210	1.35	1.70908	2.30510	1.75259
0.36	1.02297	0.60800	0.57678	0.86	1.19359	1.44891	1.25384	1.36	1.71789	2.30614	1.75640
0.37	1.02376	0.61067	0.57951	0.87	1.19595	1.45385	1.25558	1.37	1.72671	2.30718	1.76020
0.38	1.02455	0.61334	0.58224	0.88	1.19831	1.45879	1.25732	1.38	1.73554	2.30822	1.76399
0.39	1.02534	0.61601	0.58497	0.89	1.20067	1.46373	1.25906	1.39	1.74438	2.30926	1.76777
0.4	1.02613	0.61868	0.58770	0.9	1.20303	1.46867	1.26080	1.4	1.75323	2.31030	1.77154
0.41	1.02692	0.62135	0.59043	0.91	1.20539	1.47361	1.26254	1.41	1.76209	2.31134	1.77530
0.42	1.02771	0.62402	0.59316	0.92	1.20775	1.47855	1.26428	1.42	1.77096	2.31238	1.77905
0.43	1.02850	0.62669	0.59589	0.93	1.21011	1.48349	1.26602	1.43	1.77983	2.31342	1.78279
0.44	1.02929	0.62936	0.59862	0.94	1.21247	1.48843	1.26776	1.44	1.78871	2.31446	1.78652
0.45	1.03008	0.63203	0.60135	0.95	1.21483	1.49337	1.26950	1.45	1.79760	2.31550	1.79024
0.46	1.03087	0.63470	0.60408	0.96	1.21719	1.49831	1.27124	1.46	1.80650	2.31654	1.79395
0.47	1.03166	0.63737	0.60681	0.97	1.21955	1.50325	1.27298	1.47	1.81541	2.31758	1.79765
0.48	1.03245	0.64004	0.60954	0.98	1.22191	1.50819	1.27472	1.48	1.82433	2.31862	1.80134
0.49	1.03324	0.64271	0.61227	0.99	1.22427	1.51313	1.27646	1.49	1.83326	2.31966	1.80502
0.5	1.03403	0.64538	0.61500	1.0	1.22663	1.51807	1.27820	1.5	1.84221	2.32070	1.80869
0.51	1.03482	0.64805	0.61773	1.01	1.22899	1.52301	1.28000	1.51	1.85117	2.32174	1.81235
0.52	1.03561	0.65072	0.62046	1.02	1.23135	1.52795	1.28180	1.52	1.86014	2.32278	1.81600
0.53	1.03640	0.65339	0.62319	1.03	1.23371	1.53289	1.28360	1.53	1.86912	2.32382	1.81964
0.54	1.03719	0.65606	0.62592	1.04	1.23607	1.53783	1.28540	1.54	1.87811	2.32486	1.82327
0.55	1.03798	0.65873	0.62865	1.05	1.23843	1.54277	1.28720	1.55	1.88711	2.32590	1.82689
0.56	1.03877	0.66140	0.63138	1.06	1.24079	1.54771	1.28900	1.56	1.89612	2.32694	1.83050
0.57	1.03956	0.66407	0.63411	1.07	1.24315	1.55265	1.29080	1.57	1.90514	2.32798	1.83410
0.58	1.04035	0.66674	0.63684	1.08	1.24551	1.55759	1.29260	1.58	1.91417	2.32902	1.83769
0.59	1.04114	0.66941	0.63957	1.09	1.24787	1.56253	1.29440	1.59	1.92321	2.33006	1.84127
0.6	1.04193	0.67208	0.64230	1.1	1.25023	1.56747	1.29620	1.6	1.93226	2.33110	1.84484
0.61	1.04272	0.67475	0.64503	1.11	1.25259	1.57241	1.29800	1.61	1.94132	2.33214	1.84840
0.62	1.04351	0.67742	0.64776	1.12	1.25495	1.57735	1.29980	1.62	1.95039	2.33318	1.85195
0.63	1.04430	0.68009	0.65049	1.13	1.25731	1.58229	1.30160	1.63	1.95947	2.33422	1.85549
0.64	1.04509	0.68276	0.65322	1.14	1.25967	1.58723	1.30340	1.64	1.96856	2.33526	1.85902
0.65	1.04588	0.68543	0.65595	1.15	1.26203	1.59217	1.30520	1.65	1.97766	2.33630	1.86254
0.66	1.04667	0.68810	0.65868	1.16	1.26439	1.59711	1.30700	1.66	1.98677	2.33734	1.86605
0.67	1.04746	0.69077	0.66141	1.17	1.26675	1.60205	1.30880	1.67	1.99589	2.33838	1.86955
0.68	1.04825	0.69344	0.66414	1.18	1.26911	1.60699	1.31060	1.68	2.00502	2.33942	1.87304
0.69	1.04904	0.69611	0.66687	1.19	1.27147	1.61193	1.31240	1.69	2.01416	2.34046	1.87652
0.7	1.04983	0.69878	0.66960	1.2	1.27383	1.61687	1.31420	1.7	2.02331	2.34150	1.87999
0.71	1.05062	0.70145	0.67233	1.21	1.27619	1.62181	1.31600	1.71	2.03247	2.34254	1.88345
0.72	1.05141	0.70412	0.67506	1.22	1.27855	1.62675	1.31780	1.72	2.04164	2.34358	1.88690
0.73	1.05220	0.70679	0.67779	1.23	1.28091	1.63169	1.31960	1.73	2.05082	2.34462	1.89034
0.74	1.05299	0.70946	0.68052	1.24	1.28327	1.63663	1.32140	1.74	2.06001	2.34566	1.89377
0.75	1.05378	0.71213	0.68325	1.25	1.28563	1.64157	1.32320	1.75	2.06921	2.34670	1.89719
0.76	1.05457	0.71480	0.68598	1.26	1.28799	1.64651	1.32500	1.76	2.07842	2.34774	1.90060
0.77	1.05536	0.71747	0.68871	1.27	1.29035	1.65145	1.32680	1.77	2.08764	2.34878	1.90399
0.78	1.05615	0.72014	0.69144	1.28	1.29271	1.65639	1.32860	1.78	2.09687	2.34982	1.90737
0.79	1.05694	0.72281	0.69417	1.29	1.29507	1.66133	1.33040	1.79	2.10611	2.35086	1.91074
0.8	1.05773	0.72548	0.69690	1.3	1.29743	1.66627	1.33220	1.8	2.11536	2.35190	1.91410
0.81	1.05852	0.72815	0.69963	1.31	1.29979	1.67121	1.33400	1.81	2.12462	2.35294	1.91745
0.82	1.05931	0.73082	0.70236	1.32	1.30215	1.67615	1.33580	1.82	2.13389	2.35398	1.92079
0.83	1.06010	0.73349	0.70509	1.33	1.30451	1.68109	1.33760	1.83	2.14317	2.35502	1.92412
0.84	1.06089	0.73616	0.70782	1.34	1.30687	1.68603	1.33940	1.84	2.15246	2.35606	1.92744
0.85	1.06168	0.73883	0.71055	1.35	1.30923	1.69097	1.34120	1.85	2.16176	2.35710	1.93075
0.86	1.06247	0.74150	0.71328	1.36	1.31159	1.69591	1.34300	1.86	2.17107	2.35814	1.9340

$\alpha = 2/3$

x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$	x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$	x	$F_{2/3}(x)$	$H_{1/3}(x)$	$T_{2/3}(x)$
1.50	1.99554	3.65447	1.83039	6.0	1.01265	5.78325	1.93118	6.0	1.997115	257.13820	1.97836
1.51	1.99577	3.65472	1.83082	6.1	1.01265	5.78325	1.93118	6.1	1.997115	257.13820	1.97836
1.52	1.99599	3.65496	1.83124	6.2	1.01265	5.78325	1.93118	6.2	1.997115	257.13820	1.97836
1.53	1.99621	3.65519	1.83166	6.3	1.01265	5.78325	1.93118	6.3	1.997115	257.13820	1.97836
1.54	1.99643	3.65542	1.83208	6.4	1.01265	5.78325	1.93118	6.4	1.997115	257.13820	1.97836
1.55	1.99665	3.65565	1.83250	6.5	1.01265	5.78325	1.93118	6.5	1.997115	257.13820	1.97836
1.56	1.99687	3.65588	1.83292	6.6	1.01265	5.78325	1.93118	6.6	1.997115	257.13820	1.97836
1.57	1.99709	3.65611	1.83334	6.7	1.01265	5.78325	1.93118	6.7	1.997115	257.13820	1.97836
1.58	1.99731	3.65634	1.83376	6.8	1.01265	5.78325	1.93118	6.8	1.997115	257.13820	1.97836
1.59	1.99753	3.65657	1.83418	6.9	1.01265	5.78325	1.93118	6.9	1.997115	257.13820	1.97836
1.60	1.99775	3.65680	1.83460	7.0	1.01265	5.78325	1.93118	7.0	1.997115	257.13820	1.97836
1.61	1.99797	3.65703	1.83502	7.1	1.01265	5.78325	1.93118	7.1	1.997115	257.13820	1.97836
1.62	1.99819	3.65726	1.83544	7.2	1.01265	5.78325	1.93118	7.2	1.997115	257.13820	1.97836
1.63	1.99841	3.65749	1.83586	7.3	1.01265	5.78325	1.93118	7.3	1.997115	257.13820	1.97836
1.64	1.99863	3.65772	1.83628	7.4	1.01265	5.78325	1.93118	7.4	1.997115	257.13820	1.97836
1.65	1.99885	3.65795	1.83670	7.5	1.01265	5.78325	1.93118	7.5	1.997115	257.13820	1.97836
1.66	1.99907	3.65818	1.83712	7.6	1.01265	5.78325	1.93118	7.6	1.997115	257.13820	1.97836
1.67	1.99929	3.65841	1.83754	7.7	1.01265	5.78325	1.93118	7.7	1.997115	257.13820	1.97836
1.68	1.99951	3.65864	1.83796	7.8	1.01265	5.78325	1.93118	7.8	1.997115	257.13820	1.97836
1.69	1.99973	3.65887	1.83838	7.9	1.01265	5.78325	1.93118	7.9	1.997115	257.13820	1.97836
1.70	1.99995	3.65910	1.83880	8.0	1.01265	5.78325	1.93118	8.0	1.997115	257.13820	1.97836
1.71	2.00017	3.65933	1.83922	8.1	1.01265	5.78325	1.93118	8.1	1.997115	257.13820	1.97836
1.72	2.00039	3.65956	1.83964	8.2	1.01265	5.78325	1.93118	8.2	1.997115	257.13820	1.97836
1.73	2.00061	3.65979	1.84006	8.3	1.01265	5.78325	1.93118	8.3	1.997115	257.13820	1.97836
1.74	2.00083	3.66002	1.84048	8.4	1.01265	5.78325	1.93118	8.4	1.997115	257.13820	1.97836
1.75	2.00105	3.66025	1.84090	8.5	1.01265	5.78325	1.93118	8.5	1.997115	257.13820	1.97836
1.76	2.00127	3.66048	1.84132	8.6	1.01265	5.78325	1.93118	8.6	1.997115	257.13820	1.97836
1.77	2.00149	3.66071	1.84174	8.7	1.01265	5.78325	1.93118	8.7	1.997115	257.13820	1.97836
1.78	2.00171	3.66094	1.84216	8.8	1.01265	5.78325	1.93118	8.8	1.997115	257.13820	1.97836
1.79	2.00193	3.66117	1.84258	8.9	1.01265	5.78325	1.93118	8.9	1.997115	257.13820	1.97836
1.80	2.00215	3.66140	1.84300	9.0	1.01265	5.78325	1.93118	9.0	1.997115	257.13820	1.97836
1.81	2.00237	3.66163	1.84342	9.1	1.01265	5.78325	1.93118	9.1	1.997115	257.13820	1.97836
1.82	2.00259	3.66186	1.84384	9.2	1.01265	5.78325	1.93118	9.2	1.997115	257.13820	1.97836
1.83	2.00281	3.66209	1.84426	9.3	1.01265	5.78325	1.93118	9.3	1.997115	257.13820	1.97836
1.84	2.00303	3.66232	1.84468	9.4	1.01265	5.78325	1.93118	9.4	1.997115	257.13820	1.97836
1.85	2.00325	3.66255	1.84510	9.5	1.01265	5.78325	1.93118	9.5	1.997115	257.13820	1.97836
1.86	2.00347	3.66278	1.84552	9.6	1.01265	5.78325	1.93118	9.6	1.997115	257.13820	1.97836
1.87	2.00369	3.66301	1.84594	9.7	1.01265	5.78325	1.93118	9.7	1.997115	257.13820	1.97836
1.88	2.00391	3.66324	1.84636	9.8	1.01265	5.78325	1.93118	9.8	1.997115	257.13820	1.97836
1.89	2.00413	3.66347	1.84678	9.9	1.01265	5.78325	1.93118	9.9	1.997115	257.13820	1.97836
1.90	2.00435	3.66370	1.84720	10.0	1.01265	5.78325	1.93118	10.0	1.997115	257.13820	1.97836
1.91	2.00457	3.66393	1.84762								
1.92	2.00479	3.66416	1.84804								
1.93	2.00501	3.66439	1.84846								
1.94	2.00523	3.66462	1.84888								
1.95	2.00545	3.66485	1.84930								
1.96	2.00567	3.66508	1.84972								
1.97	2.00589	3.66531	1.85014								
1.98	2.00611	3.66554	1.85056								
1.99	2.00633	3.66577	1.85098								
2.00	2.00655	3.66600	1.85140								

TABLE 3B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 2/3$ and x from 1.50 to 10.0.

x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$	x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$	x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$
0.0000	1.00000	0.00047	0.00047	0.50	1.25631	0.17209	0.13746	1.00	2.19278	0.54199	0.25747
0.0010	1.00010	0.00050	0.00050	0.51	1.25693	0.17205	0.13745	1.01	2.19283	0.54199	0.25746
0.0020	1.00020	0.00053	0.00053	0.52	1.25755	0.17200	0.13743	1.02	2.19288	0.54199	0.25745
0.0030	1.00030	0.00057	0.00057	0.53	1.25817	0.17195	0.13740	1.03	2.19293	0.54199	0.25744
0.0040	1.00040	0.00060	0.00060	0.54	1.25879	0.17190	0.13737	1.04	2.19298	0.54199	0.25743
0.0050	1.00050	0.00064	0.00064	0.55	1.25941	0.17185	0.13734	1.05	2.19303	0.54199	0.25742
0.0060	1.00060	0.00068	0.00068	0.56	1.26003	0.17180	0.13731	1.06	2.19308	0.54199	0.25741
0.0070	1.00070	0.00072	0.00072	0.57	1.26065	0.17175	0.13728	1.07	2.19313	0.54199	0.25740
0.0080	1.00080	0.00076	0.00076	0.58	1.26127	0.17170	0.13725	1.08	2.19318	0.54199	0.25739
0.0090	1.00090	0.00080	0.00080	0.59	1.26189	0.17165	0.13722	1.09	2.19323	0.54199	0.25738
0.0100	1.00100	0.00084	0.00084	0.60	1.26251	0.17160	0.13719	1.10	2.19328	0.54199	0.25737
0.0110	1.00110	0.00088	0.00088	0.61	1.26313	0.17155	0.13716	1.11	2.19333	0.54199	0.25736
0.0120	1.00120	0.00092	0.00092	0.62	1.26375	0.17150	0.13713	1.12	2.19338	0.54199	0.25735
0.0130	1.00130	0.00096	0.00096	0.63	1.26437	0.17145	0.13710	1.13	2.19343	0.54199	0.25734
0.0140	1.00140	0.00100	0.00100	0.64	1.26499	0.17140	0.13707	1.14	2.19348	0.54199	0.25733
0.0150	1.00150	0.00104	0.00104	0.65	1.26561	0.17135	0.13704	1.15	2.19353	0.54199	0.25732
0.0160	1.00160	0.00108	0.00108	0.66	1.26623	0.17130	0.13701	1.16	2.19358	0.54199	0.25731
0.0170	1.00170	0.00112	0.00112	0.67	1.26685	0.17125	0.13698	1.17	2.19363	0.54199	0.25730
0.0180	1.00180	0.00116	0.00116	0.68	1.26747	0.17120	0.13695	1.18	2.19368	0.54199	0.25729
0.0190	1.00190	0.00120	0.00120	0.69	1.26809	0.17115	0.13692	1.19	2.19373	0.54199	0.25728
0.0200	1.00200	0.00124	0.00124	0.70	1.26871	0.17110	0.13689	1.20	2.19378	0.54199	0.25727
0.0210	1.00210	0.00128	0.00128	0.71	1.26933	0.17105	0.13686	1.21	2.19383	0.54199	0.25726
0.0220	1.00220	0.00132	0.00132	0.72	1.26995	0.17100	0.13683	1.22	2.19388	0.54199	0.25725
0.0230	1.00230	0.00136	0.00136	0.73	1.27057	0.17095	0.13680	1.23	2.19393	0.54199	0.25724
0.0240	1.00240	0.00140	0.00140	0.74	1.27119	0.17090	0.13677	1.24	2.19398	0.54199	0.25723
0.0250	1.00250	0.00144	0.00144	0.75	1.27181	0.17085	0.13674	1.25	2.19403	0.54199	0.25722
0.0260	1.00260	0.00148	0.00148	0.76	1.27243	0.17080	0.13671	1.26	2.19408	0.54199	0.25721
0.0270	1.00270	0.00152	0.00152	0.77	1.27305	0.17075	0.13668	1.27	2.19413	0.54199	0.25720
0.0280	1.00280	0.00156	0.00156	0.78	1.27367	0.17070	0.13665	1.28	2.19418	0.54199	0.25719
0.0290	1.00290	0.00160	0.00160	0.79	1.27429	0.17065	0.13662	1.29	2.19423	0.54199	0.25718
0.0300	1.00300	0.00164	0.00164	0.80	1.27491	0.17060	0.13659	1.30	2.19428	0.54199	0.25717
0.0310	1.00310	0.00168	0.00168	0.81	1.27553	0.17055	0.13656	1.31	2.19433	0.54199	0.25716
0.0320	1.00320	0.00172	0.00172	0.82	1.27615	0.17050	0.13653	1.32	2.19438	0.54199	0.25715
0.0330	1.00330	0.00176	0.00176	0.83	1.27677	0.17045	0.13650	1.33	2.19443	0.54199	0.25714
0.0340	1.00340	0.00180	0.00180	0.84	1.27739	0.17040	0.13647	1.34	2.19448	0.54199	0.25713
0.0350	1.00350	0.00184	0.00184	0.85	1.27801	0.17035	0.13644	1.35	2.19453	0.54199	0.25712
0.0360	1.00360	0.00188	0.00188	0.86	1.27863	0.17030	0.13641	1.36	2.19458	0.54199	0.25711
0.0370	1.00370	0.00192	0.00192	0.87	1.27925	0.17025	0.13638	1.37	2.19463	0.54199	0.25710
0.0380	1.00380	0.00196	0.00196	0.88	1.27987	0.17020	0.13635	1.38	2.19468	0.54199	0.25709
0.0390	1.00390	0.00200	0.00200	0.89	1.28049	0.17015	0.13632	1.39	2.19473	0.54199	0.25708
0.0400	1.00400	0.00204	0.00204	0.90	1.28111	0.17010	0.13629	1.40	2.19478	0.54199	0.25707
0.0410	1.00410	0.00208	0.00208	0.91	1.28173	0.17005	0.13626	1.41	2.19483	0.54199	0.25706
0.0420	1.00420	0.00212	0.00212	0.92	1.28235	0.17000	0.13623	1.42	2.19488	0.54199	0.25705
0.0430	1.00430	0.00216	0.00216	0.93	1.28297	0.16995	0.13620	1.43	2.19493	0.54199	0.25704
0.0440	1.00440	0.00220	0.00220	0.94	1.28359	0.16990	0.13617	1.44	2.19498	0.54199	0.25703
0.0450	1.00450	0.00224	0.00224	0.95	1.28421	0.16985	0.13614	1.45	2.19503	0.54199	0.25702
0.0460	1.00460	0.00228	0.00228	0.96	1.28483	0.16980	0.13611	1.46	2.19508	0.54199	0.25701
0.0470	1.00470	0.00232	0.00232	0.97	1.28545	0.16975	0.13608	1.47	2.19513	0.54199	0.25700
0.0480	1.00480	0.00236	0.00236	0.98	1.28607	0.16970	0.13605	1.48	2.19518	0.54199	0.25699
0.0490	1.00490	0.00240	0.00240	0.99	1.28669	0.16965	0.13602	1.49	2.19523	0.54199	0.25698
0.0500	1.00500	0.00244	0.00244	1.00	1.28731	0.16960	0.13599	1.50	2.19528	0.54199	0.25697
0.0510	1.00510	0.00248	0.00248								
0.0520	1.00520	0.00252	0.00252								
0.0530	1.00530	0.00256	0.00256								
0.0540	1.00540	0.00260	0.00260								
0.0550	1.00550	0.00264	0.00264								
0.0560	1.00560	0.00268	0.00268								
0.0570	1.00570	0.00272	0.00272								
0.0580	1.00580	0.00276	0.00276								
0.0590	1.00590	0.00280	0.00280								
0.0600	1.00600	0.00284	0.00284								
0.0610	1.00610	0.00288	0.00288								
0.0620	1.00620	0.00292	0.00292								
0.0630	1.00630	0.00296	0.00296								
0.0640	1.00640	0.00300	0.00300								
0.0650	1.00650	0.00304	0.00304								
0.0660	1.00660	0.00308	0.00308								
0.0670	1.00670	0.00312	0.00312								
0.0680	1.00680	0.00316	0.00316								
0.0690	1.00690	0.00320	0.00320								
0.0700	1.00700	0.00324	0.00324								
0.0710	1.00710	0.00328	0.00328								
0.0720	1.00720	0.00332	0.00332								
0.0730	1.00730	0.00336	0.00336								
0.0740	1.00740	0.00340	0.00340								
0.0750	1.00750	0.00344	0.00344								
0.0760	1.00760	0.00348	0.00348								
0.0770	1.00770	0.00352	0.00352								
0.0780	1.00780	0.00356	0.00356								
0.0790	1.00790	0.00360	0.00360								
0.0800	1.00800	0.00364	0.00364								
0.0810	1.00810	0.00368	0.00368								
0.0820	1.00820	0.00372	0.00372								
0.0830	1.00830	0.00376	0.00376								
0.0840	1.00840	0.00380	0.00380								
0.0850	1.00850	0.00384	0.00384								
0.0860	1.00860	0.00388	0.00388								
0.0870	1.00870	0.00392	0.00392								
0.0880	1.00880	0.00396	0.00396								
0.0890	1.00890	0.00400	0.00400								
0.0900	1.00900	0.00404	0.00404								
0.0910	1.00910	0.00408	0.00408								
0.0920	1.00920	0.00412	0.00412								
0.0930	1.00930	0.00416	0.00416								
0.0940	1.00940	0.00420	0.00420								
0.0950	1.00950	0.00424	0.00424								
0.0960	1.00960	0.00428	0.00428								
0.0970	1.00970	0.00432	0.00432								
0.0980	1.00980	0.00436	0.00436								
0.0990	1.00990	0.00440	0.00440								
0.1000	1.01000	0.00444	0.00444								

TABLE 4A. Lanchester-Clifford-Schlöfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for $\alpha = 1/4$ and x from 0.00 to 1.50.

x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$	x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$	x	$F_{1/4}(x)$	$H_{3/4}(x)$	$T_{1/4}(x)$
1.50	3.30031	1.17433	0.30901	2.0	9.75616	2.26675	0.37770	6.0	527.67626	178.34720	0.33799
1.51	3.30953	1.17969	0.30960	2.1	7.70085	2.59835	0.37962	6.1	585.47759	198.0419	0.33799
1.52	3.31966	1.18522	0.31018	2.2	7.20088	2.86267	0.38118	6.2	650.47799	219.85313	0.33799
1.53	3.33059	1.19091	0.31075	2.3	6.91919	3.09243	0.38245	6.3	722.12168	244.06809	0.33799
1.54	3.34277	1.19681	0.31131	2.4	6.74661	3.26473	0.38348	6.4	801.59208	270.92829	0.33799
1.55	3.35550	1.20288	0.31186	2.5	6.67085	3.40113	0.38431	6.5	889.73967	300.72132	0.33799
1.56	3.36887	1.20915	0.31239	2.6	6.59112	3.51771	0.38500	6.6	987.50692	333.76568	0.33799
1.57	3.38287	1.21562	0.31294	2.7	6.50875	3.61007	0.38555	6.7	1095.53831	370.44339	0.33799
1.58	3.39750	1.22229	0.31349	2.8	6.42488	3.68866	0.38600	6.8	1216.49138	411.03607	0.33799
1.59	3.41277	1.22917	0.31404	2.9	6.33988	3.74786	0.38637	6.9	1349.54844	456.13200	0.33799
1.60	3.42865	1.23624	0.31459	3.0	6.25351	3.7992	0.38667	7.0	1497.43105	506.11678	0.33799
1.61	3.44513	1.24350	0.31514	3.1	6.16572	3.84318	0.38691	7.1	1661.41366	561.53928	0.33799
1.62	3.46220	1.25094	0.31569	3.2	6.07652	3.88028	0.38717	7.2	1843.24219	623.95529	0.33799
1.63	3.47987	1.25856	0.31624	3.3	5.98582	3.91103	0.38740	7.3	2044.87933	691.16333	0.33799
1.64	3.49814	1.26635	0.31679	3.4	5.89363	3.93604	0.38768	7.4	2268.37739	766.68645	0.33799
1.65	3.51699	1.27431	0.31734	3.5	5.80000	3.96219	0.38791	7.5	2516.74022	850.44792	0.33799
1.66	3.53642	1.28244	0.31789	3.6	5.70497	3.98947	0.38809	7.6	2790.99753	943.30954	0.33799
1.67	3.55642	1.29074	0.31844	3.7	5.60861	4.01790	0.38826	7.7	3095.23215	1046.25608	0.33799
1.68	3.57699	1.29921	0.31899	3.8	5.51093	4.04747	0.38842	7.8	3433.43381	1160.37849	0.33799
1.69	3.59814	1.30784	0.31954	3.9	5.41200	4.07804	0.38857	7.9	3807.47665	1286.88542	0.33799
1.70	3.61987	1.31663	0.32009	4.0	5.31187	4.10964	0.38871	8.0	4222.37283	1427.11584	0.33799
1.71	3.64219	1.32558	0.32064	4.1	5.21050	4.14230	0.38885	8.1	4682.61100	1581.5206	0.33799
1.72	3.66500	1.33469	0.32119	4.2	5.10787	4.17604	0.38898	8.2	5192.89274	1750.39729	0.33799
1.73	3.68837	1.34396	0.32174	4.3	4.99399	4.21086	0.38911	8.3	5763.59735	1934.9170	0.33799
1.74	3.71230	1.35339	0.32229	4.4	4.87882	4.24676	0.38924	8.4	6395.26842	2135.44170	0.33799
1.75	3.73677	1.36297	0.32284	4.5	4.76235	4.28376	0.38937	8.5	7077.16850	2392.00581	0.33799
1.76	3.76179	1.37270	0.32339	4.6	4.64466	4.32186	0.38949	8.6	7800.30050	2691.96407	0.33799
1.77	3.78736	1.38258	0.32394	4.7	4.52577	4.36106	0.38961	8.7	8566.67335	2940.0690	0.33799
1.78	3.81349	1.39261	0.32449	4.8	4.40566	4.40136	0.38973	8.8	9378.26842	3259.31970	0.33799
1.79	3.84017	1.40279	0.32504	4.9	4.28431	4.44276	0.38985	8.9	10236.03241	3613.11455	0.33799
1.80	3.86740	1.41312	0.32559	5.0	4.16172	4.48526	0.38997	9.0	11249.28315	4005.16529	0.33799
1.81	3.89513	1.42360	0.32614	5.1	4.03787	4.52886	0.39009	9.1	12435.23354	4439.59636	0.33799
1.82	3.92336	1.43423	0.32669	5.2	3.91277	4.57356	0.39021	9.2	13815.46902	4920.97585	0.33799
1.83	3.95209	1.44500	0.32724	5.3	3.78642	4.61936	0.39033	9.3	15413.68846	5455.36306	0.33799
1.84	3.98132	1.45591	0.32779	5.4	3.65883	4.66626	0.39045	9.4	17266.26020	6045.36129	0.33799
1.85	4.01105	1.46696	0.32834	5.5	3.53000	4.71426	0.39057	9.5	19423.64472	6700.17618	0.33799
1.86	4.04128	1.47815	0.32889	5.6	3.40000	4.76336	0.39069	9.6	21923.37333	7428.6036	0.33799
1.87	4.07191	1.48948	0.32944	5.7	3.26883	4.81356	0.39081	9.7	24348.37283	8228.48506	0.33799
1.88	4.10304	1.50094	0.32999	5.8	3.13642	4.86486	0.39093	9.8	26683.17337	9133.01918	0.33799
1.89	4.13467	1.51253	0.33054	5.9	3.00377	4.91726	0.39105	9.9	29002.19553	10106.61719	0.33799
1.90	4.16680	1.52426	0.33109	6.0	2.87087	4.97076	0.39117	10.0	31336.02562	11199.61611	0.33799
1.91	4.19943	1.53613	0.33164								
1.92	4.23256	1.54814	0.33219								
1.93	4.26619	1.56029	0.33274								
1.94	4.30032	1.57258	0.33329								
1.95	4.33495	1.58501	0.33384								
1.96	4.37008	1.59758	0.33439								
1.97	4.40571	1.61029	0.33494								
1.98	4.44184	1.62314	0.33549								
1.99	4.47847	1.63613	0.33604								
2.00	4.51560	1.64926	0.33659								

TABLE 4B. Lanchester-Clifford-Schlöfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 1/4$ and x from 1.50 to 10.0.

x	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$	x	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$	x	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$
0.0	1.00000	0.02685	0.026884	0.50	1.04893	2.10140	1.33707	1.00	1.35788	3.26340	2.23322
0.01	1.00003	0.02685	0.026884	0.51	1.04932	2.10140	1.33707	1.01	1.35788	3.26340	2.23322
0.02	1.00003	0.02685	0.026884	0.52	1.04971	2.10140	1.33707	1.02	1.35788	3.26340	2.23322
0.03	1.00003	0.02685	0.026884	0.53	1.05010	2.10140	1.33707	1.03	1.35788	3.26340	2.23322
0.04	1.00003	0.02685	0.026884	0.54	1.05049	2.10140	1.33707	1.04	1.35788	3.26340	2.23322
0.05	1.00081	0.02777	0.02777	0.55	1.05088	2.10140	1.33707	1.05	1.35788	3.26340	2.23322
0.06	1.00103	0.02832	0.02832	0.56	1.05127	2.10140	1.33707	1.06	1.35788	3.26340	2.23322
0.07	1.00126	0.02887	0.02887	0.57	1.05166	2.10140	1.33707	1.07	1.35788	3.26340	2.23322
0.08	1.00210	0.02942	0.02942	0.58	1.05205	2.10140	1.33707	1.08	1.35788	3.26340	2.23322
0.09	1.00344	0.03034	0.03034	0.59	1.05244	2.10140	1.33707	1.09	1.35788	3.26340	2.23322
0.10	1.00444	0.03126	0.03126	0.60	1.05283	2.10140	1.33707	1.10	1.35788	3.26340	2.23322
0.11	1.00544	0.03218	0.03218	0.61	1.05322	2.10140	1.33707	1.11	1.35788	3.26340	2.23322
0.12	1.00644	0.03310	0.03310	0.62	1.05361	2.10140	1.33707	1.12	1.35788	3.26340	2.23322
0.13	1.00744	0.03402	0.03402	0.63	1.05400	2.10140	1.33707	1.13	1.35788	3.26340	2.23322
0.14	1.00844	0.03494	0.03494	0.64	1.05439	2.10140	1.33707	1.14	1.35788	3.26340	2.23322
0.15	1.00944	0.03586	0.03586	0.65	1.05478	2.10140	1.33707	1.15	1.35788	3.26340	2.23322
0.16	1.01044	0.03678	0.03678	0.66	1.05517	2.10140	1.33707	1.16	1.35788	3.26340	2.23322
0.17	1.01144	0.03770	0.03770	0.67	1.05556	2.10140	1.33707	1.17	1.35788	3.26340	2.23322
0.18	1.01244	0.03862	0.03862	0.68	1.05595	2.10140	1.33707	1.18	1.35788	3.26340	2.23322
0.19	1.01344	0.03954	0.03954	0.69	1.05634	2.10140	1.33707	1.19	1.35788	3.26340	2.23322
0.20	1.01444	0.04046	0.04046	0.70	1.05673	2.10140	1.33707	1.20	1.35788	3.26340	2.23322
0.21	1.01544	0.04138	0.04138	0.71	1.05712	2.10140	1.33707	1.21	1.35788	3.26340	2.23322
0.22	1.01644	0.04230	0.04230	0.72	1.05751	2.10140	1.33707	1.22	1.35788	3.26340	2.23322
0.23	1.01744	0.04322	0.04322	0.73	1.05790	2.10140	1.33707	1.23	1.35788	3.26340	2.23322
0.24	1.01844	0.04414	0.04414	0.74	1.05829	2.10140	1.33707	1.24	1.35788	3.26340	2.23322
0.25	1.01944	0.04506	0.04506	0.75	1.05868	2.10140	1.33707	1.25	1.35788	3.26340	2.23322
0.26	1.02044	0.04598	0.04598	0.76	1.05907	2.10140	1.33707	1.26	1.35788	3.26340	2.23322
0.27	1.02144	0.04690	0.04690	0.77	1.05946	2.10140	1.33707	1.27	1.35788	3.26340	2.23322
0.28	1.02244	0.04782	0.04782	0.78	1.05985	2.10140	1.33707	1.28	1.35788	3.26340	2.23322
0.29	1.02344	0.04874	0.04874	0.79	1.06024	2.10140	1.33707	1.29	1.35788	3.26340	2.23322
0.30	1.02444	0.04966	0.04966	0.80	1.06063	2.10140	1.33707	1.30	1.35788	3.26340	2.23322
0.31	1.02544	0.05058	0.05058	0.81	1.06102	2.10140	1.33707	1.31	1.35788	3.26340	2.23322
0.32	1.02644	0.05150	0.05150	0.82	1.06141	2.10140	1.33707	1.32	1.35788	3.26340	2.23322
0.33	1.02744	0.05242	0.05242	0.83	1.06180	2.10140	1.33707	1.33	1.35788	3.26340	2.23322
0.34	1.02844	0.05334	0.05334	0.84	1.06219	2.10140	1.33707	1.34	1.35788	3.26340	2.23322
0.35	1.02944	0.05426	0.05426	0.85	1.06258	2.10140	1.33707	1.35	1.35788	3.26340	2.23322
0.36	1.03044	0.05518	0.05518	0.86	1.06297	2.10140	1.33707	1.36	1.35788	3.26340	2.23322
0.37	1.03144	0.05610	0.05610	0.87	1.06336	2.10140	1.33707	1.37	1.35788	3.26340	2.23322
0.38	1.03244	0.05702	0.05702	0.88	1.06375	2.10140	1.33707	1.38	1.35788	3.26340	2.23322
0.39	1.03344	0.05794	0.05794	0.89	1.06414	2.10140	1.33707	1.39	1.35788	3.26340	2.23322
0.40	1.03444	0.05886	0.05886	0.90	1.06453	2.10140	1.33707	1.40	1.35788	3.26340	2.23322
0.41	1.03544	0.05978	0.05978	0.91	1.06492	2.10140	1.33707	1.41	1.35788	3.26340	2.23322
0.42	1.03644	0.06070	0.06070	0.92	1.06531	2.10140	1.33707	1.42	1.35788	3.26340	2.23322
0.43	1.03744	0.06162	0.06162	0.93	1.06570	2.10140	1.33707	1.43	1.35788	3.26340	2.23322
0.44	1.03844	0.06254	0.06254	0.94	1.06609	2.10140	1.33707	1.44	1.35788	3.26340	2.23322
0.45	1.03944	0.06346	0.06346	0.95	1.06648	2.10140	1.33707	1.45	1.35788	3.26340	2.23322
0.46	1.04044	0.06438	0.06438	0.96	1.06687	2.10140	1.33707	1.46	1.35788	3.26340	2.23322
0.47	1.04144	0.06530	0.06530	0.97	1.06726	2.10140	1.33707	1.47	1.35788	3.26340	2.23322
0.48	1.04244	0.06622	0.06622	0.98	1.06765	2.10140	1.33707	1.48	1.35788	3.26340	2.23322
0.49	1.04344	0.06714	0.06714	0.99	1.06804	2.10140	1.33707	1.49	1.35788	3.26340	2.23322
0.50	1.04444	0.06806	0.06806	1.00	1.06843	2.10140	1.33707	1.50	1.35788	3.26340	2.23322

TABLE 5A. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 3/4$ and x from 0.00 to 1.50.

$\alpha = 3/4$

x	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$	x	$F_{3/4}(x)$	$H_{1/4}(x)$	$T_{3/4}(x)$
1.50	1.87507	5.22942	2.78799	2.76367	7.28850	2.89054	6.0	1.7180972	318.97126	2.95867
1.51	1.89270	5.27350	2.78623	2.79970	8.70554	2.90477	6.1	1.8161917	350.95316	2.95867
1.52	1.90948	5.31795	2.78441	2.81694	9.49340	2.91815	6.2	1.9352772	386.17215	2.95866
1.53	1.92648	5.36279	2.78259	2.83461	10.30432	2.93132	6.3	1.45.63173	424.95717	2.95866
1.54	1.94366	5.40801	2.78061	2.85277	11.13048	2.94438	6.4	1.56.36900	467.67305	2.95866
1.55	1.96098	5.45353	2.77859	2.87129	11.97177	2.95734	6.5	1.71.96977	514.71843	2.95867
1.56	1.97843	5.49937	2.77653	2.89015	12.82835	2.97020	6.6	1.93.48319	566.53511	2.95867
1.57	1.99599	5.54552	2.77443	2.90926	13.70022	2.98297	6.7	2.18.77365	623.60946	2.95867
1.58	2.01366	5.59203	2.77229	2.92861	14.58738	2.99564	6.8	2.45.92336	686.47762	2.95867
1.59	2.03142	5.63883	2.77011	2.94819	15.48982	2.99820	6.9	2.75.42908	755.47306	2.95867
1.60	2.04927	5.68597	2.76790	2.96799	16.40867	2.99969	7.0	2.11.21402	832.01907	2.95867
1.61	2.06721	5.73346	2.76565	2.98797	17.34394	2.99999	7.1	2.40.41993	917.06433	2.95867
1.62	2.08524	5.78130	2.76337	2.99814	18.29466	2.99999	7.2	2.70.91444	1008.65470	2.95867
1.63	2.10336	5.82949	2.76105	3.00845	19.26082	2.99999	7.3	3.02.32549	1107.66420	2.95867
1.64	2.12156	5.87803	2.75870	3.01888	20.24242	2.99999	7.4	3.35.37666	1213.05550	2.95867
1.65	2.13984	5.92692	2.75632	3.02944	21.23946	2.99999	7.5	3.69.23428	1325.88978	2.95867
1.66	2.15819	5.97615	2.75391	3.04012	22.25191	2.99999	7.6	4.04.31884	1445.33670	2.95867
1.67	2.17661	6.02572	2.75147	3.05091	23.27976	2.99999	7.7	4.40.62825	1571.96608	2.95867
1.68	2.19510	6.07563	2.74900	3.06181	24.32302	2.99999	7.8	4.78.69774	1705.92656	2.95867
1.69	2.21366	6.12588	2.74650	3.07282	25.38168	2.99999	7.9	5.18.86974	1847.92656	2.95867
1.70	2.23229	6.17646	2.74397	3.08394	26.45574	2.99999	8.0	5.60.23428	2000.00000	2.95867
1.71	2.25098	6.22737	2.74141	3.09517	27.54520	2.99999	8.1	6.03.31884	2163.33670	2.95867
1.72	2.26973	6.27861	2.73882	3.10651	28.65006	2.99999	8.2	6.48.18884	2338.00000	2.95867
1.73	2.28853	6.33018	2.73620	3.11796	29.77032	2.99999	8.3	6.94.31884	2524.33670	2.95867
1.74	2.30738	6.38208	2.73355	3.12951	30.90608	2.99999	8.4	7.41.62825	2722.92656	2.95867
1.75	2.32628	6.43431	2.73087	3.14116	32.05734	2.99999	8.5	7.90.23428	2934.00000	2.95867
1.76	2.34523	6.48687	2.72817	3.15291	33.22410	2.99999	8.6	8.40.31884	3158.33670	2.95867
1.77	2.36423	6.53976	2.72544	3.16476	34.40636	2.99999	8.7	8.91.62825	3395.92656	2.95867
1.78	2.38328	6.59298	2.72269	3.17671	35.60512	2.99999	8.8	9.44.31884	3647.00000	2.95867
1.79	2.40238	6.64653	2.71992	3.18876	36.82038	2.99999	8.9	9.98.62825	3912.33670	2.95867
1.80	2.42153	6.70041	2.71713	3.20091	38.05214	2.99999	9.0	10.54.31884	4192.00000	2.95867
1.81	2.44073	6.75462	2.71431	3.21316	39.30040	2.99999	9.1	11.11.62825	4486.33670	2.95867
1.82	2.46000	6.80917	2.71147	3.22551	40.56516	2.99999	9.2	11.70.31884	4795.92656	2.95867
1.83	2.47933	6.86406	2.70861	3.23796	41.84642	2.99999	9.3	12.30.62825	5120.00000	2.95867
1.84	2.49873	6.91929	2.70573	3.25051	43.15418	2.99999	9.4	12.92.31884	5469.33670	2.95867
1.85	2.51819	6.97485	2.70283	3.26316	44.48844	2.99999	9.5	13.56.62825	5844.00000	2.95867
1.86	2.53771	7.03074	2.69991	3.27591	45.84920	2.99999	9.6	14.23.31884	6235.92656	2.95867
1.87	2.55729	7.08696	2.69697	3.28876	47.23646	2.99999	9.7	14.92.62825	6645.00000	2.95867
1.88	2.57693	7.14351	2.69401	3.30171	48.65022	2.99999	9.8	15.64.31884	7072.33670	2.95867
1.89	2.59663	7.20039	2.69103	3.31476	50.09048	2.99999	9.9	16.39.62825	7517.92656	2.95867
1.90	2.61639	7.25760	2.68803	3.32791	51.55724	2.99999	10.0	17.17.31884	7982.00000	2.95867
1.91	2.63621	7.31513	2.68500	3.34116	53.05050	2.99999				
1.92	2.65609	7.37298	2.68195	3.35451	54.57026	2.99999				
1.93	2.67603	7.43115	2.67888	3.36796	56.11652	2.99999				
1.94	2.69603	7.48964	2.67579	3.38151	57.68928	2.99999				
1.95	2.71609	7.54845	2.67267	3.39516	59.28854	2.99999				
1.96	2.73621	7.60758	2.66953	3.40891	60.91430	2.99999				
1.97	2.75639	7.66703	2.66637	3.42276	62.56656	2.99999				
1.98	2.77663	7.72680	2.66318	3.43671	64.24532	2.99999				
1.99	2.79693	7.78689	2.65997	3.45076	65.95058	2.99999				
2.00	2.81729	7.84730	2.65673	3.46491	67.68234	2.99999				

TABLE 5B. Lanchester-Clifford-Schlöfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for $\alpha = 3/4$ and x from 1.50 to 10.0.

$\alpha = 1/5$

x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$	x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$	x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$
0.0	1.00000	0.00000	0.00000	0.5	1.32072	0.40800	0.16661	1.0	2.39524	0.47223	0.17793
0.01	1.00013	0.00026	0.00005	0.51	1.32493	0.41553	0.16909	1.01	2.41590	0.47403	0.17913
0.02	1.00049	0.00079	0.00019	0.52	1.32914	0.42307	0.17150	1.02	2.43711	0.47583	0.18033
0.03	1.00113	0.00151	0.00041	0.53	1.33335	0.43061	0.17392	1.03	2.45832	0.47763	0.18153
0.04	1.00200	0.00236	0.00089	0.54	1.33756	0.43815	0.17634	1.04	2.47953	0.47943	0.18273
0.05	1.00313	0.00348	0.00159	0.55	1.34177	0.44569	0.17876	1.05	2.50074	0.48123	0.18393
0.06	1.00450	0.00496	0.00259	0.56	1.34598	0.45323	0.18118	1.06	2.52195	0.48303	0.18513
0.07	1.00601	0.00686	0.00399	0.57	1.35019	0.46077	0.18360	1.07	2.54316	0.48483	0.18633
0.08	1.00767	0.00925	0.00589	0.58	1.35440	0.46831	0.18602	1.08	2.56437	0.48663	0.18753
0.09	1.00948	0.01214	0.00839	0.59	1.35861	0.47585	0.18844	1.09	2.58558	0.48843	0.18873
0.1	1.01143	0.01563	0.01149	0.6	1.36282	0.48339	0.19086	1.1	2.60679	0.49023	0.18993
0.11	1.01353	0.01972	0.01519	0.61	1.36703	0.49093	0.19328	1.11	2.62800	0.49203	0.19113
0.12	1.01578	0.02441	0.01949	0.62	1.37124	0.49847	0.19570	1.12	2.64921	0.49383	0.19233
0.13	1.01818	0.02970	0.02429	0.63	1.37545	0.50601	0.19812	1.13	2.67042	0.49563	0.19353
0.14	1.02073	0.03559	0.02949	0.64	1.37966	0.51355	0.20054	1.14	2.69163	0.49743	0.19473
0.15	1.02343	0.04208	0.03519	0.65	1.38387	0.52109	0.20296	1.15	2.71284	0.49923	0.19593
0.16	1.02628	0.04917	0.04149	0.66	1.38808	0.52863	0.20538	1.16	2.73405	0.50103	0.19713
0.17	1.02928	0.05686	0.04829	0.67	1.39229	0.53617	0.20780	1.17	2.75526	0.50283	0.19833
0.18	1.03243	0.06515	0.05549	0.68	1.39650	0.54371	0.21022	1.18	2.77647	0.50463	0.19953
0.19	1.03573	0.07404	0.06319	0.69	1.40071	0.55125	0.21264	1.19	2.79768	0.50643	0.20073
0.2	1.03918	0.08353	0.07149	0.7	1.40492	0.55879	0.21506	1.2	2.81889	0.50823	0.20193
0.21	1.04278	0.09362	0.08029	0.71	1.40913	0.56633	0.21748	1.21	2.84010	0.51003	0.20313
0.22	1.04653	0.10431	0.08949	0.72	1.41334	0.57387	0.21990	1.22	2.86131	0.51183	0.20433
0.23	1.05043	0.11560	0.09919	0.73	1.41755	0.58141	0.22232	1.23	2.88252	0.51363	0.20553
0.24	1.05448	0.12749	0.10939	0.74	1.42176	0.58895	0.22474	1.24	2.90373	0.51543	0.20673
0.25	1.05868	0.14008	0.12009	0.75	1.42597	0.59649	0.22716	1.25	2.92494	0.51723	0.20793
0.26	1.06303	0.15337	0.13129	0.76	1.43018	0.60403	0.22958	1.26	2.94615	0.51903	0.20913
0.27	1.06753	0.16736	0.14299	0.77	1.43439	0.61157	0.23200	1.27	2.96736	0.52083	0.21033
0.28	1.07218	0.18205	0.15519	0.78	1.43860	0.61911	0.23442	1.28	2.98857	0.52263	0.21153
0.29	1.07698	0.19744	0.16789	0.79	1.44281	0.62665	0.23684	1.29	3.00978	0.52443	0.21273
0.3	1.08193	0.21353	0.18109	0.8	1.44702	0.63419	0.23926	1.3	3.03099	0.52623	0.21393
0.31	1.08703	0.23032	0.19479	0.81	1.45123	0.64173	0.24168	1.31	3.05220	0.52803	0.21513
0.32	1.09228	0.24781	0.20899	0.82	1.45544	0.64927	0.24410	1.32	3.07341	0.52983	0.21633
0.33	1.09768	0.26590	0.22369	0.83	1.45965	0.65681	0.24652	1.33	3.09462	0.53163	0.21753
0.34	1.10323	0.28459	0.23889	0.84	1.46386	0.66435	0.24894	1.34	3.11583	0.53343	0.21873
0.35	1.10893	0.30388	0.25449	0.85	1.46807	0.67189	0.25136	1.35	3.13704	0.53523	0.21993
0.36	1.11478	0.32377	0.27049	0.86	1.47228	0.67943	0.25378	1.36	3.15825	0.53703	0.22113
0.37	1.12078	0.34426	0.28689	0.87	1.47649	0.68697	0.25620	1.37	3.17946	0.53883	0.22233
0.38	1.12693	0.36535	0.30369	0.88	1.48070	0.69451	0.25862	1.38	3.20067	0.54063	0.22353
0.39	1.13323	0.38704	0.32089	0.89	1.48491	0.70205	0.26104	1.39	3.22188	0.54243	0.22473
0.4	1.13968	0.40933	0.33849	0.9	1.48912	0.70959	0.26346	1.4	3.24309	0.54423	0.22593
0.41	1.14628	0.43222	0.35649	0.91	1.49333	0.71713	0.26588	1.41	3.26430	0.54603	0.22713
0.42	1.15303	0.45571	0.37489	0.92	1.49754	0.72467	0.26830	1.42	3.28551	0.54783	0.22833
0.43	1.15993	0.47980	0.39369	0.93	1.50175	0.73221	0.27072	1.43	3.30672	0.54963	0.22953
0.44	1.16708	0.50449	0.41289	0.94	1.50596	0.73975	0.27314	1.44	3.32793	0.55143	0.23073
0.45	1.17438	0.52978	0.43249	0.95	1.51017	0.74729	0.27556	1.45	3.34914	0.55323	0.23193
0.46	1.18183	0.55567	0.45249	0.96	1.51438	0.75483	0.27798	1.46	3.37035	0.55503	0.23313
0.47	1.18943	0.58216	0.47289	0.97	1.51859	0.76237	0.28040	1.47	3.39156	0.55683	0.23433
0.48	1.19718	0.60925	0.49369	0.98	1.52280	0.76991	0.28282	1.48	3.41277	0.55863	0.23553
0.49	1.20508	0.63694	0.51489	0.99	1.52701	0.77745	0.28524	1.49	3.43398	0.56043	0.23673
0.5	1.21313	0.66523	0.53649	1.0	1.53122	0.78499	0.28766	1.5	3.45519	0.56223	0.23793

TABLE 6A. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 1/5$ and x from 0.00 to 1.50.

x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$	x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$	x	$F_{1/5}(x)$	$H_{4/5}(x)$	$T_{1/5}(x)$
1.50	4.53040	1.06142	0.23423	2.0	8.42789	2.07992	0.24688	6.0	700.89071	177.74325	0.25360
1.51	4.58820	1.07582	0.23469	2.1	9.50223	2.35595	0.24619	6.1	778.96261	197.54277	0.25360
1.52	4.64609	1.09240	0.23509	2.2	10.71144	2.67702	0.24517	6.2	865.64062	219.52377	0.25360
1.53	4.70388	1.11091	0.23548	2.3	12.06779	3.01177	0.25001	6.3	961.86701	243.92611	0.25360
1.54	4.76157	1.13036	0.23586	2.4	13.57220	3.40328	0.25068	6.4	1068.68667	271.01608	0.25360
1.55	4.81919	1.15015	0.23623	2.5	15.23339	3.83405	0.25121	6.5	1181.28832	301.08512	0.25360
1.56	4.87671	1.17062	0.23659	2.6	17.05312	4.30498	0.25167	6.6	1309.66788	334.56147	0.25360
1.57	4.93416	1.19246	0.23695	2.7	19.03347	4.81613	0.25205	6.7	1454.07779	371.52059	0.25360
1.58	5.00155	1.21569	0.23731	2.8	21.17602	5.36713	0.25236	6.8	1616.07125	412.50591	0.25360
1.59	5.06867	1.24030	0.23767	2.9	23.49274	5.95816	0.25266	6.9	1797.23911	458.23991	0.25360
1.60	5.13551	1.26639	0.23803	3.0	26.00000	6.58905	0.25291	7.0	2000.58906	508.86695	0.25360
1.61	5.20207	1.29391	0.23839	3.1	28.69774	7.26072	0.25316	7.1	2221.11298	565.04537	0.25360
1.62	5.26836	1.32291	0.23875	3.2	31.48706	7.97222	0.25341	7.2	2474.91797	627.37937	0.25360
1.63	5.33439	1.35341	0.23911	3.3	34.36896	8.72432	0.25366	7.3	2746.63101	696.54039	0.25360
1.64	5.40016	1.38546	0.23947	3.4	37.34448	9.51686	0.25391	7.4	3040.21213	773.27112	0.25360
1.65	5.46567	1.41911	0.23983	3.5	40.41472	10.35016	0.25416	7.5	3384.87750	858.39852	0.25360
1.66	5.53092	1.45441	0.24019	3.6	43.58076	11.22469	0.25441	7.6	3751.28135	952.83443	0.25360
1.67	5.59591	1.49141	0.24055	3.7	46.84360	12.14083	0.25466	7.7	4170.34888	1057.59271	0.25360
1.68	5.66064	1.53016	0.24091	3.8	50.20432	13.09899	0.25491	7.8	4620.58851	1173.78691	0.25360
1.69	5.72511	1.57061	0.24127	3.9	53.66392	14.09948	0.25516	7.9	5136.86869	1302.69030	0.25360
1.70	5.78932	1.61381	0.24163	4.0	57.22340	15.14316	0.25541	8.0	5700.54986	1445.65407	0.25360
1.71	5.85329	1.65981	0.24199	4.1	60.88376	16.23000	0.25566	8.1	6311.24772	1604.21698	0.25360
1.72	5.91702	1.70861	0.24235	4.2	64.64608	17.36048	0.25591	8.2	6970.07311	1780.40731	0.25360
1.73	5.98051	1.76016	0.24271	4.3	68.51136	18.53516	0.25616	8.3	7700.31605	1975.10239	0.25360
1.74	6.04376	1.81446	0.24307	4.4	72.48064	19.75468	0.25641	8.4	8541.16934	2191.38448	0.25360
1.75	6.10677	1.87151	0.24339	4.5	76.55496	21.01871	0.25666	8.5	9586.93047	2431.22887	0.25360
1.76	6.16954	1.93136	0.24371	4.6	80.73536	22.32770	0.25691	8.6	10833.67462	2697.18887	0.25360
1.77	6.23207	1.99401	0.24403	4.7	85.02288	23.68148	0.25716	8.7	12300.55352	2992.09998	0.25360
1.78	6.29436	2.05946	0.24435	4.8	89.41856	25.08048	0.25741	8.8	13998.0108	3319.10107	0.25360
1.79	6.35641	2.12771	0.24467	4.9	93.92352	26.52516	0.25766	8.9	14911.73379	3681.67111	0.25360
1.80	6.41824	2.19886	0.24499	5.0	98.53888	28.01608	0.25791	9.0	16102.87904	4083.66516	0.25360
1.81	6.47986	2.27291	0.24531	5.1	103.26544	29.55392	0.25816	9.1	17500.72710	4523.27722	0.25360
1.82	6.54127	2.35006	0.24563	5.2	108.10416	31.13968	0.25841	9.2	19108.08871	5017.36412	0.25360
1.83	6.60248	2.43031	0.24595	5.3	113.05504	32.77376	0.25866	9.3	20940.50854	5571.54152	0.25360
1.84	6.66349	2.51366	0.24627	5.4	118.11912	34.45664	0.25891	9.4	22991.97769	6178.54152	0.25360
1.85	6.72430	2.60011	0.24659	5.5	123.29648	36.18912	0.25916	9.5	25270.67695	6851.74096	0.25360
1.86	6.78491	2.68976	0.24691	5.6	128.58816	37.97136	0.25941	9.6	27789.76485	7557.99697	0.25360
1.87	6.84532	2.78261	0.24723	5.7	133.99424	39.80384	0.25966	9.7	30557.34468	8425.21055	0.25360
1.88	6.90563	2.87876	0.24755	5.8	139.51584	41.68672	0.25991	9.8	33683.33470	9342.14050	0.25360
1.89	6.96584	2.97811	0.24787	5.9	145.15296	43.61984	0.26016	9.9	37200.05146	10358.48612	0.25360
1.90	7.02595	3.08066	0.24819	6.0	150.90560	45.60336	0.26041	10.0	40446.05146	11484.99634	0.25360
1.91	7.08596	3.18641	0.24851								
1.92	7.14587	3.29536	0.24883								
1.93	7.20568	3.40751	0.24915								
1.94	7.26529	3.52286	0.24947								
1.95	7.32470	3.64141	0.24979								
1.96	7.38391	3.76316	0.25011								
1.97	7.44292	3.88811	0.25043								
1.98	7.50173	4.01626	0.25075								
1.99	7.56034	4.14761	0.25107								
2.00	7.61875	4.28216	0.25139								

TABLE 6B. Lanchester-Clifford-Schlöfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 1/5$ and x from 1.50 to 10.0.

$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$	x	$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$	x	$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$
0.00000	0.0289	0.0289	0.00000	1.9777	0.9329	0.9329	1.00000	1.93278	0.8439	0.8439
0.00009	0.0289	0.0289	0.00009	1.9777	0.9329	0.9329	1.00009	1.93278	0.8439	0.8439
0.00018	0.0289	0.0289	0.00018	1.9777	0.9329	0.9329	1.00018	1.93278	0.8439	0.8439
0.00027	0.0289	0.0289	0.00027	1.9777	0.9329	0.9329	1.00027	1.93278	0.8439	0.8439
0.00036	0.0289	0.0289	0.00036	1.9777	0.9329	0.9329	1.00036	1.93278	0.8439	0.8439
0.00045	0.0289	0.0289	0.00045	1.9777	0.9329	0.9329	1.00045	1.93278	0.8439	0.8439
0.00054	0.0289	0.0289	0.00054	1.9777	0.9329	0.9329	1.00054	1.93278	0.8439	0.8439
0.00063	0.0289	0.0289	0.00063	1.9777	0.9329	0.9329	1.00063	1.93278	0.8439	0.8439
0.00072	0.0289	0.0289	0.00072	1.9777	0.9329	0.9329	1.00072	1.93278	0.8439	0.8439
0.00081	0.0289	0.0289	0.00081	1.9777	0.9329	0.9329	1.00081	1.93278	0.8439	0.8439
0.00090	0.0289	0.0289	0.00090	1.9777	0.9329	0.9329	1.00090	1.93278	0.8439	0.8439
0.00099	0.0289	0.0289	0.00099	1.9777	0.9329	0.9329	1.00099	1.93278	0.8439	0.8439
0.00108	0.0289	0.0289	0.00108	1.9777	0.9329	0.9329	1.00108	1.93278	0.8439	0.8439
0.00117	0.0289	0.0289	0.00117	1.9777	0.9329	0.9329	1.00117	1.93278	0.8439	0.8439
0.00126	0.0289	0.0289	0.00126	1.9777	0.9329	0.9329	1.00126	1.93278	0.8439	0.8439
0.00135	0.0289	0.0289	0.00135	1.9777	0.9329	0.9329	1.00135	1.93278	0.8439	0.8439
0.00144	0.0289	0.0289	0.00144	1.9777	0.9329	0.9329	1.00144	1.93278	0.8439	0.8439
0.00153	0.0289	0.0289	0.00153	1.9777	0.9329	0.9329	1.00153	1.93278	0.8439	0.8439
0.00162	0.0289	0.0289	0.00162	1.9777	0.9329	0.9329	1.00162	1.93278	0.8439	0.8439
0.00171	0.0289	0.0289	0.00171	1.9777	0.9329	0.9329	1.00171	1.93278	0.8439	0.8439
0.00180	0.0289	0.0289	0.00180	1.9777	0.9329	0.9329	1.00180	1.93278	0.8439	0.8439
0.00189	0.0289	0.0289	0.00189	1.9777	0.9329	0.9329	1.00189	1.93278	0.8439	0.8439
0.00198	0.0289	0.0289	0.00198	1.9777	0.9329	0.9329	1.00198	1.93278	0.8439	0.8439
0.00207	0.0289	0.0289	0.00207	1.9777	0.9329	0.9329	1.00207	1.93278	0.8439	0.8439
0.00216	0.0289	0.0289	0.00216	1.9777	0.9329	0.9329	1.00216	1.93278	0.8439	0.8439
0.00225	0.0289	0.0289	0.00225	1.9777	0.9329	0.9329	1.00225	1.93278	0.8439	0.8439
0.00234	0.0289	0.0289	0.00234	1.9777	0.9329	0.9329	1.00234	1.93278	0.8439	0.8439
0.00243	0.0289	0.0289	0.00243	1.9777	0.9329	0.9329	1.00243	1.93278	0.8439	0.8439
0.00252	0.0289	0.0289	0.00252	1.9777	0.9329	0.9329	1.00252	1.93278	0.8439	0.8439
0.00261	0.0289	0.0289	0.00261	1.9777	0.9329	0.9329	1.00261	1.93278	0.8439	0.8439
0.00270	0.0289	0.0289	0.00270	1.9777	0.9329	0.9329	1.00270	1.93278	0.8439	0.8439
0.00279	0.0289	0.0289	0.00279	1.9777	0.9329	0.9329	1.00279	1.93278	0.8439	0.8439
0.00288	0.0289	0.0289	0.00288	1.9777	0.9329	0.9329	1.00288	1.93278	0.8439	0.8439
0.00297	0.0289	0.0289	0.00297	1.9777	0.9329	0.9329	1.00297	1.93278	0.8439	0.8439
0.00306	0.0289	0.0289	0.00306	1.9777	0.9329	0.9329	1.00306	1.93278	0.8439	0.8439
0.00315	0.0289	0.0289	0.00315	1.9777	0.9329	0.9329	1.00315	1.93278	0.8439	0.8439
0.00324	0.0289	0.0289	0.00324	1.9777	0.9329	0.9329	1.00324	1.93278	0.8439	0.8439
0.00333	0.0289	0.0289	0.00333	1.9777	0.9329	0.9329	1.00333	1.93278	0.8439	0.8439
0.00342	0.0289	0.0289	0.00342	1.9777	0.9329	0.9329	1.00342	1.93278	0.8439	0.8439
0.00351	0.0289	0.0289	0.00351	1.9777	0.9329	0.9329	1.00351	1.93278	0.8439	0.8439
0.00360	0.0289	0.0289	0.00360	1.9777	0.9329	0.9329	1.00360	1.93278	0.8439	0.8439
0.00369	0.0289	0.0289	0.00369	1.9777	0.9329	0.9329	1.00369	1.93278	0.8439	0.8439
0.00378	0.0289	0.0289	0.00378	1.9777	0.9329	0.9329	1.00378	1.93278	0.8439	0.8439
0.00387	0.0289	0.0289	0.00387	1.9777	0.9329	0.9329	1.00387	1.93278	0.8439	0.8439
0.00396	0.0289	0.0289	0.00396	1.9777	0.9329	0.9329	1.00396	1.93278	0.8439	0.8439
0.00405	0.0289	0.0289	0.00405	1.9777	0.9329	0.9329	1.00405	1.93278	0.8439	0.8439
0.00414	0.0289	0.0289	0.00414	1.9777	0.9329	0.9329	1.00414	1.93278	0.8439	0.8439
0.00423	0.0289	0.0289	0.00423	1.9777	0.9329	0.9329	1.00423	1.93278	0.8439	0.8439
0.00432	0.0289	0.0289	0.00432	1.9777	0.9329	0.9329	1.00432	1.93278	0.8439	0.8439
0.00441	0.0289	0.0289	0.00441	1.9777	0.9329	0.9329	1.00441	1.93278	0.8439	0.8439
0.00450	0.0289	0.0289	0.00450	1.9777	0.9329	0.9329	1.00450	1.93278	0.8439	0.8439
0.00459	0.0289	0.0289	0.00459	1.9777	0.9329	0.9329	1.00459	1.93278	0.8439	0.8439
0.00468	0.0289	0.0289	0.00468	1.9777	0.9329	0.9329	1.00468	1.93278	0.8439	0.8439
0.00477	0.0289	0.0289	0.00477	1.9777	0.9329	0.9329	1.00477	1.93278	0.8439	0.8439
0.00486	0.0289	0.0289	0.00486	1.9777	0.9329	0.9329	1.00486	1.93278	0.8439	0.8439
0.00495	0.0289	0.0289	0.00495	1.9777	0.9329	0.9329	1.00495	1.93278	0.8439	0.8439
0.00504	0.0289	0.0289	0.00504	1.9777	0.9329	0.9329	1.00504	1.93278	0.8439	0.8439
0.00513	0.0289	0.0289	0.00513	1.9777	0.9329	0.9329	1.00513	1.93278	0.8439	0.8439
0.00522	0.0289	0.0289	0.00522	1.9777	0.9329	0.9329	1.00522	1.93278	0.8439	0.8439
0.00531	0.0289	0.0289	0.00531	1.9777	0.9329	0.9329	1.00531	1.93278	0.8439	0.8439
0.00540	0.0289	0.0289	0.00540	1.9777	0.9329	0.9329	1.00540	1.93278	0.8439	0.8439
0.00549	0.0289	0.0289	0.00549	1.9777	0.9329	0.9329	1.00549	1.93278	0.8439	0.8439
0.00558	0.0289	0.0289	0.00558	1.9777	0.9329	0.9329	1.00558	1.93278	0.8439	0.8439
0.00567	0.0289	0.0289	0.00567	1.9777	0.9329	0.9329	1.00567	1.93278	0.8439	0.8439
0.00576	0.0289	0.0289	0.00576	1.9777	0.9329	0.9329	1.00576	1.93278	0.8439	0.8439
0.00585	0.0289	0.0289	0.00585	1.9777	0.9329	0.9329	1.00585	1.93278	0.8439	0.8439
0.00594	0.0289	0.0289	0.00594	1.9777	0.9329	0.9329	1.00594	1.93278	0.8439	0.8439
0.00603	0.0289	0.0289	0.00603	1.9777	0.9329	0.9329	1.00603	1.93278	0.8439	0.8439
0.00612	0.0289	0.0289	0.00612	1.9777	0.9329	0.9329	1.00612	1.93278	0.8439	0.8439
0.00621	0.0289	0.0289	0.00621	1.9777	0.9329	0.9329	1.00621	1.93278	0.8439	0.8439
0.00630	0.0289	0.0289	0.00630	1.9777	0.9329	0.9329	1.00630	1.93278	0.8439	0.8439
0.00639	0.0289	0.0289	0.00639	1.9777	0.9329	0.9329	1.00639	1.93278	0.8439	0.8439
0.00648	0.0289	0.0289	0.00648	1.9777	0.9329	0.9329	1.00648	1.93278	0.8439	0.8439
0.00657	0.0289	0.0289	0.00657	1.9777	0.9329	0.9329	1.00657	1.93278	0.8439	0.8439
0.00666	0.0289	0.0289	0.00666	1.9777	0.9329	0.9329	1.00666	1.93278	0.8439	0.8439
0.00675	0.0289	0.0289	0.00675	1.9777	0.9329	0.9329	1.00675	1.93278	0.8439	0.8439
0.00684	0.0289	0.0289	0.00684	1.9777	0.9329	0.9329	1.00684	1.93278	0.8439	0.8439
0.00693	0.0289	0.0289	0.00693	1.9777	0.9329	0.9329	1.00693	1.93278	0.8439	0.8439
0.00702	0.0289	0.0289	0.00702	1.9777	0.9329	0.9329	1.00702	1.93278	0.8439	0.8439
0.00711	0.0289	0.0289	0.00711	1.9777	0.9329	0.9329	1.00711	1.93278	0.8439	0.8439
0.00720	0.0289	0.0289	0.00720	1.9777	0.9329	0.9329	1.00720	1.93278	0.8439	0.8439
0.00729	0.0289	0.0289	0.00729	1.9777	0.9329	0.9329	1.00729	1.93278	0.8439	0.8439
0.00738	0.0289	0.0289	0.00738	1.9777	0.9329	0.9329	1.00738	1.93278	0.8439	0.8439
0.00747	0.0289	0.0289	0.00747	1.9777	0.9329	0.9329	1.00747	1.93278	0.8439	0.8439
0.00756	0.0289	0.0289	0.00756	1.9777	0.9329	0.9329	1.00756	1.93278	0.8439	0.8439
0.00765	0.0289	0.0289	0.00765	1.9777	0.9329	0.9329	1.00765	1.93278	0.8439	0.8439
0.00774	0.0289	0.0289	0.00774	1.9777	0.9329	0.9329	1.00774	1.93278	0.8439	0.8439
0.00783	0.0289	0.0289	0.00783	1.9777	0.9329	0.9329	1.00783	1.93278	0.8439	0.8439
0.00792	0.0289	0.0289	0.00792	1.9777	0.9329	0.9329	1.00792	1.93278	0.8439	0.8439
0.00801	0.0289	0.0289	0.00801	1.9777	0.9329	0.9329	1.00801	1.93278	0.8439	0.8439
0.00810	0.0289	0.0289	0.00810	1.9777	0.9329	0.9329	1.00810	1.93278	0.8439	0.8439
0.00819	0.0289	0.0289	0.00819	1.9777	0.9329	0.9329	1.00819	1.93278	0.8439	0.8439
0.00828	0.0289	0.0289	0.00828	1.9777	0.9329	0.9329	1.00828	1.93278	0.8439	0.8439
0.00837	0.0289	0.0289	0.00837	1.9777	0.9329	0.9329	1.00837	1.93278	0.8439	0.8439
0.00846	0.0289	0.0289	0.00846	1.9777	0.9329	0.9329	1.00846	1.93		

TABLE 7A. Lanchester-Clifford-Schl\"afli Functions $F_i(x)$, $H_{1-\alpha}(x)$, and

$\Gamma_\alpha(x)$ for $\alpha = 2/5$ and x from 0.00 to 1.50.

α	$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$	x	$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$	x	$F_{2/5}(x)$	$H_{3/5}(x)$	$T_{2/5}(x)$
1.00	2.71176	1.64228	0.60561	2.0	4.50188	2.94825	0.64692	6.0	2.78.92057	187.25497	0.67136
1.01	2.71313	1.64234	0.60689	2.1	4.51218	3.27101	0.65135	6.1	308.81162	207.32397	0.67136
1.02	2.71481	1.64239	0.60813	2.2	4.52286	3.60495	0.65588	6.2	341.91671	229.54871	0.67136
1.03	2.71681	1.64246	0.60936	2.3	4.53444	4.06495	0.65986	6.3	378.95625	254.14613	0.67136
1.04	2.71915	1.64253	0.61056	2.4	4.54681	4.53.771	0.66400	6.4	419.06687	281.35829	0.67136
1.05	2.72175	1.64258	0.61174	2.5	4.56013	5.04780	0.66819	6.5	463.91827	311.68146	0.67136
1.06	2.72460	1.64263	0.61289	2.6	4.57439	5.57171	0.67238	6.6	513.61264	347.81159	0.67136
1.07	2.72769	1.64268	0.61403	2.7	4.58961	6.11983	0.67695	6.7	568.51856	389.71529	0.67136
1.08	2.73102	1.64273	0.61516	2.8	4.60578	6.70323	0.68165	6.8	639.36749	422.54724	0.67136
1.09	2.73459	1.64278	0.61628	2.9	4.62291	7.33293	0.68645	6.9	727.84582	467.73468	0.67136
1.10	2.73840	1.64282	0.61739	3.0	4.64099	8.01994	0.69136	7.0	835.61756	517.74129	0.67136
1.11	2.74243	1.64286	0.61849	3.1	4.65913	8.76573	0.69644	7.1	964.60886	573.08038	0.67136
1.12	2.74668	1.64290	0.61959	3.2	4.67733	9.57195	0.70174	7.2	1118.1869	634.31861	0.67136
1.13	2.75115	1.64294	0.62068	3.3	4.69559	10.44044	0.70717	7.3	1304.74977	702.08474	0.67136
1.14	2.75584	1.64298	0.62176	3.4	4.71391	11.37404	0.71283	7.4	1527.446.2	777.07339	0.67136
1.15	2.76075	1.64302	0.62283	3.5	4.73229	12.37799	0.71869	7.5	1791.02725	860.05207	0.67136
1.16	2.76588	1.64306	0.62389	3.6	4.75073	13.4598	0.72474	7.6	2156.85277	951.87152	0.67136
1.17	2.77123	1.64310	0.62494	3.7	4.76923	14.6246	0.73100	7.7	2653.89273	1053.89122	0.67136
1.18	2.77679	1.64314	0.62598	3.8	4.78779	15.8786	0.73747	7.8	3302.2811	1190.2811	0.67136
1.19	2.78256	1.64318	0.62701	3.9	4.80641	17.3294	0.74417	7.9	4135.97175	1351.87152	0.67136
1.20	2.78854	1.64322	0.62804	4.0	4.82509	18.9846	0.75117	8.0	5202.43699	1580.22198	0.67136
1.21	2.79473	1.64326	0.62906	4.1	4.84383	20.8517	0.75847	8.1	6557.71718	1804.72261	0.67136
1.22	2.80113	1.64330	0.63008	4.2	4.86263	22.9386	0.76607	8.2	8262.43669	2041.44573	0.67136
1.23	2.80774	1.64334	0.63109	4.3	4.88149	25.3530	0.77397	8.3	10392.64379	2369.16724	0.67136
1.24	2.81456	1.64338	0.63209	4.4	4.90041	28.1075	0.78227	8.4	13105.76091	2822.18712	0.67136
1.25	2.82159	1.64342	0.63308	4.5	4.91939	31.2122	0.79097	8.5	16582.88225	3401.56328	0.67136
1.26	2.82883	1.64346	0.63406	4.6	4.93843	34.6849	0.79997	8.6	21000.64949	4210.64949	0.67136
1.27	2.83628	1.64350	0.63503	4.7	4.95753	38.5444	0.80927	8.7	26622.61247	5352.61247	0.67136
1.28	2.84394	1.64354	0.63599	4.8	4.97669	42.8049	0.81887	8.8	33709.64379	6892.67224	0.67136
1.29	2.85181	1.64358	0.63694	4.9	4.99591	47.4849	0.82877	8.9	43741.88925	9001.56328	0.67136
1.30	2.85989	1.64362	0.63788	5.0	5.01519	52.6049	0.83897	9.0	58155.55521	11992.93895	0.67136
1.31	2.86818	1.64366	0.63881	5.1	5.03453	58.1849	0.84947	9.1	78543.71763	16149.49861	0.67136
1.32	2.87668	1.64370	0.63973	5.2	5.05393	64.3449	0.86027	9.2	10762.76091	21492.54861	0.67136
1.33	2.88539	1.64374	0.64064	5.3	5.07339	71.1049	0.87137	9.3	14892.51354	28892.54861	0.67136
1.34	2.89431	1.64378	0.64154	5.4	5.09291	78.5849	0.88277	9.4	20622.61247	39392.54861	0.67136
1.35	2.90344	1.64382	0.64243	5.5	5.11249	86.8849	0.89447	9.5	28522.61247	5592.54861	0.67136
1.36	2.91278	1.64386	0.64331	5.6	5.13213	96.0049	0.90647	9.6	39392.54861	8182.54861	0.67136
1.37	2.92233	1.64390	0.64418	5.7	5.15183	106.1449	0.91877	9.7	54522.61247	11322.54861	0.67136
1.38	2.93208	1.64394	0.64504	5.8	5.17159	117.3049	0.93137	9.8	75522.61247	15522.54861	0.67136
1.39	2.94203	1.64398	0.64589	5.9	5.19141	129.5849	0.94427	9.9	104522.61247	21322.54861	0.67136
1.40	2.95218	1.64402	0.64673	6.0	5.21129	143.0849	0.95747	10.0	144522.61247	29322.54861	0.67136
2.00	4.52641	2.92825	0.64692								

TABLE 7B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for $\alpha = 2/5$ and x from 1.50 to 10.0.

x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$	x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$	x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$
0.0	1.00000	0.0	0.0	0.50	1.10622	0.86199	0.71922	1.00	1.43028	1.70597	1.17030
0.01	1.00004	0.03607	0.03607	0.51	1.11060	0.87131	0.72899	1.01	1.46004	1.72536	1.18172
0.02	1.00008	0.06280	0.06279	0.52	1.11519	0.88054	0.73894	1.02	1.48980	1.74489	1.19326
0.03	1.00017	0.08887	0.08884	0.53	1.11993	0.88963	0.74903	1.03	1.51955	1.76456	1.20491
0.04	1.00194	0.10716	0.10705	0.54	1.12485	0.89857	0.75924	1.04	1.54909	1.78436	1.21668
0.05	1.00400	0.12713	0.12695	0.55	1.12995	0.90737	0.76956	1.05	1.57837	1.80431	1.22856
0.06	1.00627	0.14833	0.14798	0.56	1.13523	0.91602	0.77999	1.06	1.60731	1.82440	1.24056
0.07	1.00875	0.17023	0.16977	0.57	1.14069	0.92452	0.79053	1.07	1.63598	1.84463	1.25268
0.08	1.01138	0.19297	0.19237	0.58	1.14633	0.93287	0.80118	1.08	1.66438	1.86500	1.26493
0.09	1.01413	0.21648	0.21577	0.59	1.15215	0.94107	0.81193	1.09	1.69251	1.88553	1.27731
0.10	1.01699	0.24078	0.23997	0.60	1.15815	0.94912	0.82277	1.10	1.72037	1.90623	1.28981
0.11	1.02004	0.26583	0.26492	0.61	1.16433	0.95702	0.83370	1.11	1.74796	1.92706	1.30241
0.12	1.02327	0.29159	0.29058	0.62	1.17069	0.96477	0.84471	1.12	1.77528	1.94801	1.31511
0.13	1.02667	0.31799	0.31688	0.63	1.17723	0.97237	0.85579	1.13	1.80233	1.96907	1.32791
0.14	1.03021	0.34507	0.34386	0.64	1.18395	0.97982	0.86693	1.14	1.82912	1.99024	1.34081
0.15	1.03388	0.37277	0.37146	0.65	1.19085	0.98712	0.87813	1.15	1.85565	2.01151	1.35381
0.16	1.03767	0.40103	0.40002	0.66	1.19793	0.99427	0.88938	1.16	1.88192	2.03288	1.36691
0.17	1.04157	0.42979	0.42868	0.67	1.20518	1.00127	0.90067	1.17	1.90793	2.05435	1.38011
0.18	1.04557	0.45900	0.45779	0.68	1.21259	1.00812	0.91199	1.18	1.93368	2.07591	1.39341
0.19	1.04967	0.48861	0.48730	0.69	1.22015	1.01482	0.92333	1.19	1.95917	2.09756	1.40681
0.20	1.05386	0.51857	0.51716	0.70	1.22786	1.02137	0.93468	1.20	1.98440	2.11930	1.42031
0.21	1.05813	0.54883	0.54732	0.71	1.23572	1.02777	0.94603	1.21	2.00937	2.14113	1.43381
0.22	1.06247	0.57934	0.57773	0.72	1.24373	1.03402	0.95738	1.22	2.03408	2.16305	1.44731
0.23	1.06687	0.61005	0.60834	0.73	1.25188	1.04012	0.96873	1.23	2.05853	2.18506	1.46081
0.24	1.07133	0.64092	0.63911	0.74	1.25999	1.04607	0.97998	1.24	2.08272	2.20716	1.47431
0.25	1.07584	0.67191	0.66999	0.75	1.26815	1.05187	0.99113	1.25	2.10665	2.22935	1.48781
0.26	1.08040	0.70307	0.70105	0.76	1.27636	1.05752	1.00218	1.26	2.13032	2.25163	1.50131
0.27	1.08500	0.73435	0.73223	0.77	1.28462	1.06302	1.01313	1.27	2.15373	2.27400	1.51481
0.28	1.08964	0.76571	0.76349	0.78	1.29293	1.06837	1.02408	1.28	2.17688	2.29646	1.52831
0.29	1.09432	0.79719	0.79487	0.79	1.30129	1.07357	1.03493	1.29	2.19977	2.31900	1.54181
0.30	1.09903	0.82874	0.82631	0.80	1.30970	1.07862	1.04568	1.30	2.22240	2.34162	1.55531
0.31	1.10377	0.86032	0.85779	0.81	1.31815	1.08352	1.05633	1.31	2.24477	2.36431	1.56881
0.32	1.10853	0.89199	0.88935	0.82	1.32664	1.08827	1.06698	1.32	2.26688	2.38706	1.58231
0.33	1.11331	0.92371	0.92097	0.83	1.33517	1.09287	1.07753	1.33	2.28873	2.40987	1.59581
0.34	1.11811	0.95544	0.95260	0.84	1.34374	1.09732	1.08798	1.34	2.31032	2.43273	1.60931
0.35	1.12292	0.98714	0.98420	0.85	1.35234	1.10162	1.09833	1.35	2.33165	2.45564	1.62281
0.36	1.12774	1.01887	1.01583	0.86	1.36097	1.10577	1.10858	1.36	2.35272	2.47860	1.63631
0.37	1.13257	1.05059	1.04745	0.87	1.36963	1.10977	1.11873	1.37	2.37353	2.50161	1.64981
0.38	1.13741	1.08231	1.07907	0.88	1.37831	1.11362	1.12878	1.38	2.39408	2.52466	1.66331
0.39	1.14226	1.11400	1.11066	0.89	1.38699	1.11732	1.13873	1.39	2.41437	2.54775	1.67681
0.40	1.14711	1.14564	1.14220	0.90	1.39568	1.12087	1.14858	1.40	2.43440	2.57088	1.69031
0.41	1.15196	1.17723	1.17369	0.91	1.40437	1.12427	1.15833	1.41	2.45417	2.59404	1.70381
0.42	1.15681	1.20882	1.20517	0.92	1.41306	1.12752	1.16798	1.42	2.47368	2.61723	1.71731
0.43	1.16166	1.24037	1.23662	0.93	1.42175	1.13062	1.17753	1.43	2.49293	2.64045	1.73081
0.44	1.16651	1.27187	1.26802	0.94	1.43044	1.13357	1.18698	1.44	2.51192	2.66370	1.74431
0.45	1.17136	1.30332	1.30007	0.95	1.43913	1.13642	1.19633	1.45	2.53065	2.68698	1.75781
0.46	1.17621	1.33472	1.33147	0.96	1.44782	1.13917	1.20558	1.46	2.54912	2.71029	1.77131
0.47	1.18106	1.36607	1.36272	0.97	1.45651	1.14182	1.21473	1.47	2.56733	2.73363	1.78481
0.48	1.18591	1.39737	1.39392	0.98	1.46520	1.14437	1.22378	1.48	2.58528	2.75699	1.79831
0.49	1.19076	1.42862	1.42507	0.99	1.47389	1.14682	1.23273	1.49	2.60297	2.78036	1.81181
0.50	1.19561	1.45982	1.45617	1.00	1.48258	1.14917	1.24158	1.50	2.62040	2.80373	1.82531

TABLE 8A. Lanchester-Clifford-Schläfli Functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ for $\alpha = 3/5$ and x from 0.00 to 1.50.

$\alpha = 3/5$

x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$	x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$	x	$F_{3/5}(x)$	$H_{2/5}(x)$	$T_{3/5}(x)$
1.50	2.11455	2.88285	1.36227	2.0	3.25912	4.69836	1.64099	6.0	153.13773	228.05212	1.48949
1.51	2.14982	2.94590	1.37625	2.1	3.30626	4.70949	1.64951	6.1	168.90493	251.58219	1.48950
1.52	2.18775	3.01690	1.39109	2.2	3.35340	4.72063	1.65803	6.2	186.33813	277.54946	1.48949
1.53	2.22856	3.09715	1.40719	2.3	3.40053	4.73176	1.66711	6.3	205.57712	306.20625	1.48950
1.54	2.27276	3.18797	1.42441	2.4	3.44767	4.74289	1.67671	6.4	226.80937	337.83198	1.48950
1.55	2.32042	3.28959	1.44285	2.5	3.49480	4.75402	1.68683	6.5	250.24213	372.74922	1.48950
1.56	2.37177	3.40255	1.46255	2.6	3.54194	4.76515	1.69745	6.6	276.40208	414.15539	1.48950
1.57	2.42713	3.52737	1.48357	2.7	3.58907	4.77628	1.70859	6.7	304.44699	463.60777	1.48950
1.58	2.48699	3.66454	1.50594	2.8	3.63620	4.78741	1.72021	6.8	334.44699	522.48477	1.48950
1.59	2.55175	3.81459	1.52967	2.9	3.68333	4.79854	1.73233	6.9	366.44699	592.48477	1.48950
1.60	2.62191	3.97897	1.55481	3.0	3.73046	4.80967	1.74495	7.0	409.24931	699.63759	1.48950
1.61	2.69797	4.15822	1.58145	3.1	3.77759	4.82080	1.75809	7.1	451.64444	776.44699	1.48950
1.62	2.77953	4.35297	1.60969	3.2	3.82472	4.83193	1.77173	7.2	498.34511	841.31311	1.48950
1.63	2.86719	4.56382	1.63954	3.3	3.87185	4.84306	1.78588	7.3	549.94699	919.22533	1.48950
1.64	2.96055	4.79147	1.67109	3.4	3.91898	4.85419	1.79952	7.4	606.94699	994.06134	1.48950
1.65	3.06021	5.03652	1.70444	3.5	3.96611	4.86532	1.81366	7.5	669.32494	997.70714	1.48950
1.66	3.16687	5.29957	1.73969	3.6	4.01324	4.87645	1.82839	7.6	739.22222	1071.07587	1.48950
1.67	3.28123	5.58162	1.77694	3.7	4.06037	4.88758	1.84362	7.7	815.82711	1215.18071	1.48950
1.68	3.40409	5.88337	1.81639	3.8	4.10750	4.89871	1.85935	7.8	900.38709	1341.13066	1.48950
1.69	3.53625	6.20652	1.86184	3.9	4.15463	4.90984	1.87558	7.9	993.35032	1480.16606	1.48950
1.70	3.67851	6.55197	1.90929	4.0	4.20176	4.92097	1.89231	8.0	1096.77089	1633.66526	1.48950
1.71	3.83177	6.92052	1.95974	4.1	4.24889	4.93210	1.90954	8.1	1210.51996	1803.07095	1.48950
1.72	3.99693	7.31317	2.01319	4.2	4.29602	4.94323	1.92727	8.2	1336.68310	1990.19235	1.48950
1.73	4.17499	7.73082	2.06974	4.3	4.34315	4.95436	1.94550	8.3	1474.69908	2196.51164	1.48950
1.74	4.36605	8.17447	2.12939	4.4	4.39028	4.96549	1.96427	8.4	1627.72303	2444.50162	1.48950
1.75	4.57111	8.64412	2.19214	4.5	4.43741	4.97662	1.98354	8.5	1796.65455	2676.12602	1.48950
1.76	4.79117	9.13977	2.25899	4.6	4.48454	4.98775	1.99937	8.6	1983.14952	2933.91126	1.48950
1.77	5.02723	9.66142	2.32994	4.7	4.53167	4.99888	2.01560	8.7	2189.03832	3200.90733	1.48950
1.78	5.28029	10.20907	2.40599	4.8	4.57880	5.00997	2.03233	8.8	2416.33389	3599.44166	1.48950
1.79	5.55135	10.78272	2.48714	4.9	4.62593	5.02106	2.04956	8.9	2664.72158	3972.91466	1.48950
1.80	5.84041	11.38337	2.57239	5.0	4.67306	5.03215	2.06729	9.0	2944.71108	4335.66473	1.48950
1.81	6.14847	12.01102	2.66164	5.1	4.72019	5.04324	2.08552	9.1	3267.85095	4694.15386	1.48950
1.82	6.47653	12.66667	2.75489	5.2	4.76732	5.05433	2.10425	9.2	3635.85095	5054.15386	1.48950
1.83	6.82459	13.35032	2.85214	5.3	4.81445	5.06542	2.12348	9.3	4049.85095	5420.15386	1.48950
1.84	7.19265	14.06297	2.95339	5.4	4.86158	5.07651	2.14321	9.4	4511.85095	5794.15386	1.48950
1.85	7.58071	14.80562	3.05864	5.5	4.90871	5.08760	2.16344	9.5	5023.85095	6176.15386	1.48950
1.86	7.98877	15.57827	3.16789	5.6	4.95584	5.09869	2.18417	9.6	5597.85095	6566.15386	1.48950
1.87	8.41683	16.38092	3.28114	5.7	5.00297	5.10978	2.20540	9.7	6233.85095	6964.15386	1.48950
1.88	8.86489	17.21357	3.39839	5.8	5.05010	5.12087	2.22713	9.8	6933.85095	7370.15386	1.48950
1.89	9.33295	18.07622	3.51964	5.9	5.09723	5.13196	2.24936	9.9	7699.85095	7784.15386	1.48950
1.90	9.82101	18.96887	3.64489	6.0	5.14436	5.14305	2.27209	10.0	7915.12075	11789.61318	1.48950
1.91	10.32907	19.89252	3.77414								
1.92	10.85713	20.84717	3.90739								
1.93	11.40519	21.83282	4.04464								
1.94	11.97325	22.84947	4.18589								
1.95	12.56131	23.89712	4.33114								
1.96	13.16937	24.97577	4.48039								
1.97	13.79743	26.08542	4.63364								
1.98	14.44549	27.22607	4.79089								
1.99	15.11355	28.39772	4.95214								
2.00	15.80161	29.60037	5.11739								

TABLE 8B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and $T_{\alpha}(x)$ for $\alpha = 3/5$ and x from 1.50 to 10.0.

x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$
0.01	1.00000	0.00000	0.00000	0.50	1.07949	3.02345	2.80081	1.00	1.3486	4.02477	3.46461	1.00	1.3486	4.02477	3.46461	1.00	1.3486	4.02477	3.46461	1.00	1.3486	4.02477	3.46461
0.02	1.00003	0.00057	0.00259	0.51	1.08610	3.05773	2.82335	1.01	1.35206	4.04914	3.47805	1.01	1.35206	4.04914	3.47805	1.01	1.35206	4.04914	3.47805	1.01	1.35206	4.04914	3.47805
0.03	1.00013	0.00153	0.00719	0.52	1.09291	3.08690	2.83555	1.02	1.35580	4.07331	3.49133	1.02	1.35580	4.07331	3.49133	1.02	1.35580	4.07331	3.49133	1.02	1.35580	4.07331	3.49133
0.04	1.00029	0.00259	0.01454	0.53	1.09954	3.11424	2.84803	1.03	1.35942	4.09736	3.50422	1.03	1.35942	4.09736	3.50422	1.03	1.35942	4.09736	3.50422	1.03	1.35942	4.09736	3.50422
0.05	1.00078	1.14386	1.14297	0.54	1.10654	3.14791	2.86113	1.04	1.36296	4.12121	3.51719	1.04	1.36296	4.12121	3.51719	1.04	1.36296	4.12121	3.51719	1.04	1.36296	4.12121	3.51719
0.06	1.00113	1.13030	1.12929	0.55	1.11337	3.17691	2.87409	1.05	1.36636	4.14491	3.53007	1.05	1.36636	4.14491	3.53007	1.05	1.36636	4.14491	3.53007	1.05	1.36636	4.14491	3.53007
0.07	1.00153	1.11817	1.11781	0.56	1.11999	3.20520	2.88686	1.06	1.36969	4.16836	3.54286	1.06	1.36969	4.16836	3.54286	1.06	1.36969	4.16836	3.54286	1.06	1.36969	4.16836	3.54286
0.08	1.00203	1.10743	1.10707	0.57	1.12649	3.23269	2.89949	1.07	1.37296	4.19156	3.55557	1.07	1.37296	4.19156	3.55557	1.07	1.37296	4.19156	3.55557	1.07	1.37296	4.19156	3.55557
0.09	1.00253	1.09812	1.09680	0.58	1.13287	3.25934	2.91199	1.08	1.37619	4.21456	3.56827	1.08	1.37619	4.21456	3.56827	1.08	1.37619	4.21456	3.56827	1.08	1.37619	4.21456	3.56827
0.10	1.00313	1.08997	1.08860	0.59	1.13913	3.28526	2.92436	1.09	1.37936	4.23736	3.58097	1.09	1.37936	4.23736	3.58097	1.09	1.37936	4.23736	3.58097	1.09	1.37936	4.23736	3.58097
0.11	1.00380	1.08287	1.08144	0.60	1.14527	3.31046	2.93661	1.10	1.38249	4.26006	3.59367	1.10	1.38249	4.26006	3.59367	1.10	1.38249	4.26006	3.59367	1.10	1.38249	4.26006	3.59367
0.12	1.00453	1.07682	1.07533	0.61	1.15129	3.33496	2.94876	1.11	1.38556	4.28266	3.60637	1.11	1.38556	4.28266	3.60637	1.11	1.38556	4.28266	3.60637	1.11	1.38556	4.28266	3.60637
0.13	1.00533	1.07182	1.07027	0.62	1.15719	3.35876	2.96081	1.12	1.38859	4.30516	3.61897	1.12	1.38859	4.30516	3.61897	1.12	1.38859	4.30516	3.61897	1.12	1.38859	4.30516	3.61897
0.14	1.00619	1.06787	1.06625	0.63	1.16297	3.38186	2.97276	1.13	1.39159	4.32756	3.63157	1.13	1.39159	4.32756	3.63157	1.13	1.39159	4.32756	3.63157	1.13	1.39159	4.32756	3.63157
0.15	1.00704	1.06497	1.06329	0.64	1.16863	3.40426	2.98461	1.14	1.39456	4.34986	3.64417	1.14	1.39456	4.34986	3.64417	1.14	1.39456	4.34986	3.64417	1.14	1.39456	4.34986	3.64417
0.16	1.00790	1.06212	1.06037	0.65	1.17417	3.42596	2.99636	1.15	1.39751	4.37206	3.65677	1.15	1.39751	4.37206	3.65677	1.15	1.39751	4.37206	3.65677	1.15	1.39751	4.37206	3.65677
0.17	1.00875	1.05932	1.05752	0.66	1.17959	3.44696	3.00801	1.16	1.40044	4.39416	3.66937	1.16	1.40044	4.39416	3.66937	1.16	1.40044	4.39416	3.66937	1.16	1.40044	4.39416	3.66937
0.18	1.00959	1.05657	1.05472	0.67	1.18489	3.46726	3.01956	1.17	1.40336	4.41616	3.68197	1.17	1.40336	4.41616	3.68197	1.17	1.40336	4.41616	3.68197	1.17	1.40336	4.41616	3.68197
0.19	1.01043	1.05387	1.05197	0.68	1.19007	3.48686	3.03101	1.18	1.40626	4.43806	3.69457	1.18	1.40626	4.43806	3.69457	1.18	1.40626	4.43806	3.69457	1.18	1.40626	4.43806	3.69457
0.20	1.01127	1.05122	1.04927	0.69	1.19513	3.50576	3.04236	1.19	1.40914	4.45986	3.70717	1.19	1.40914	4.45986	3.70717	1.19	1.40914	4.45986	3.70717	1.19	1.40914	4.45986	3.70717
0.21	1.01211	1.04862	1.04657	0.70	1.19999	3.52396	3.05361	1.20	1.41201	4.48156	3.71977	1.20	1.41201	4.48156	3.71977	1.20	1.41201	4.48156	3.71977	1.20	1.41201	4.48156	3.71977
0.22	1.01295	1.04607	1.04397	0.71	1.20473	3.54146	3.06476	1.21	1.41486	4.50316	3.73237	1.21	1.41486	4.50316	3.73237	1.21	1.41486	4.50316	3.73237	1.21	1.41486	4.50316	3.73237
0.23	1.01379	1.04357	1.04142	0.72	1.20935	3.55826	3.07581	1.22	1.41769	4.52466	3.74497	1.22	1.41769	4.52466	3.74497	1.22	1.41769	4.52466	3.74497	1.22	1.41769	4.52466	3.74497
0.24	1.01463	1.04112	1.03892	0.73	1.21387	3.57436	3.08676	1.23	1.42051	4.54606	3.75757	1.23	1.42051	4.54606	3.75757	1.23	1.42051	4.54606	3.75757	1.23	1.42051	4.54606	3.75757
0.25	1.01547	1.03872	1.03652	0.74	1.21829	3.58976	3.09761	1.24	1.42331	4.56736	3.77017	1.24	1.42331	4.56736	3.77017	1.24	1.42331	4.56736	3.77017	1.24	1.42331	4.56736	3.77017
0.26	1.01631	1.03637	1.03412	0.75	1.22261	3.60446	3.10836	1.25	1.42611	4.58856	3.78277	1.25	1.42611	4.58856	3.78277	1.25	1.42611	4.58856	3.78277	1.25	1.42611	4.58856	3.78277
0.27	1.01715	1.03407	1.03177	0.76	1.22683	3.61846	3.11891	1.26	1.42891	4.60966	3.79537	1.26	1.42891	4.60966	3.79537	1.26	1.42891	4.60966	3.79537	1.26	1.42891	4.60966	3.79537
0.28	1.01799	1.03182	1.02947	0.77	1.23095	3.63176	3.12936	1.27	1.43169	4.63066	3.80797	1.27	1.43169	4.63066	3.80797	1.27	1.43169	4.63066	3.80797	1.27	1.43169	4.63066	3.80797
0.29	1.01883	1.02962	1.02722	0.78	1.23497	3.64436	3.13971	1.28	1.43446	4.65156	3.82057	1.28	1.43446	4.65156	3.82057	1.28	1.43446	4.65156	3.82057	1.28	1.43446	4.65156	3.82057
0.30	1.01967	1.02747	1.02497	0.79	1.23889	3.65626	3.14996	1.29	1.43723	4.67236	3.83317	1.29	1.43723	4.67236	3.83317	1.29	1.43723	4.67236	3.83317	1.29	1.43723	4.67236	3.83317
0.31	1.02051	1.02532	1.02272	0.80	1.24271	3.66746	3.16011	1.30	1.44001	4.69306	3.84577	1.30	1.44001	4.69306	3.84577	1.30	1.44001	4.69306	3.84577	1.30	1.44001	4.69306	3.84577
0.32	1.02135	1.02317	1.02047	0.81	1.24643	3.67796	3.17016	1.31	1.44279	4.71366	3.85837	1.31	1.44279	4.71366	3.85837	1.31	1.44279	4.71366	3.85837	1.31	1.44279	4.71366	3.85837
0.33	1.02219	1.02102	1.01822	0.82	1.25005	3.68776	3.18011	1.32	1.44556	4.73416	3.87097	1.32	1.44556	4.73416	3.87097	1.32	1.44556	4.73416	3.87097	1.32	1.44556	4.73416	3.87097
0.34	1.02303	1.01887	1.01697	0.83	1.25357	3.69686	3.19006	1.33	1.44833	4.75456	3.88357	1.33	1.44833	4.75456	3.88357	1.33	1.44833	4.75456	3.88357	1.33	1.44833	4.75456	3.88357
0.35	1.02387	1.01672	1.01472	0.84	1.25699	3.70526	3.20001	1.34	1.45109	4.77486	3.89617	1.34	1.45109	4.77486	3.89617	1.34	1.45109	4.77486	3.89617	1.34	1.45109	4.77486	3.89617
0.36	1.02471	1.01457	1.01252	0.85	1.26031	3.71286	3.20976	1.35	1.45386	4.79506	3.90877	1.35	1.45386	4.79506	3.90877	1.35	1.45386	4.79506	3.90877	1.35	1.45386	4.79506	3.90877
0.37	1.02555	1.01242	1.01032	0.86	1.26353	3.72036	3.21931	1.36	1.45663	4.81516	3.92137	1.36	1.45663	4.81516	3.92137	1.36	1.45663	4.81516	3.92137	1.36	1.45663	4.81516	3.92137
0.38	1.02639	1.01027	1.00812	0.87	1.26665	3.72766	3.22876	1.37	1.45939	4.83516	3.93397	1.37	1.45939	4.83516	3.93397	1.37	1.45939	4.83516	3.93397	1.37	1.45939	4.83516	3.93397
0.39	1.02723	1.00812	1.00592	0.88	1.26967	3.73476	3.23801	1.38	1.46216	4.85506	3.94657	1.38	1.46216	4.85506	3.94657	1.38	1.46216	4.85506	3.94657	1.38	1.46216	4.85506	3.94657
0.40	1.02807	1.00597	1.00372	0.89	1.27259	3.74166	3.24716	1.39	1.46493	4.87486	3.95917	1.39	1.46493	4.87486	3.95917	1.39	1.46493	4.87486	3.95917	1.39	1.46493	4.87486	3.95917
0.41	1.02891	1.00382	1.00147	0.90	1.27541	3.74836	3.25611	1.40	1.46770	4.89456	3.97177	1.40	1.46770	4.89456	3.97177	1.40	1.46770	4.89456	3.97177	1.40	1.46770	4.89456	3.97177
0.42	1.02975	1.00167	1.00002	0.91	1.27813	3.75486	3.26496	1.41	1.47047	4.91416	3.98437	1.41	1.47047	4.91416	3.98437	1.41	1.47047	4.91416	3.98437	1.41	1.47047	4.91416	3.98437
0.43	1.03059	1.00002	0.99837	0.92	1.28085	3.76116	3.27371	1.42	1.47323	4.93366	3.99697	1.42	1.47323	4.93366	3.99697	1.42	1.47323	4.93366	3.99697	1.42	1.47323	4.93366	3.99697
0.44	1.03143	0.99837	0.99672	0.93	1.28347	3.76726	3.28236	1.43	1.47599	4.95306	4.00957	1.43	1.47599	4.95306	4.00957	1.43	1.47599	4.953					

$\alpha = 4/5$

x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$	x	$F_{4/5}(x)$	$H_{1/5}(x)$	$T_{4/5}(x)$
1.50	1.82062	6.82973	3.75077	2.0	3.66859	10.21838	3.66859	6.0	97.15298	383.09540	3.94323
1.51	1.83333	6.88281	3.75432	2.1	3.88162	11.10058	3.88162	6.1	106.80157	421.14242	3.94323
1.52	1.84612	6.93736	3.75781	2.2	3.89244	11.70747	3.89244	6.2	117.10411	463.01142	3.94323
1.53	1.85906	6.99238	3.76126	2.3	3.90119	12.14780	3.90119	6.3	129.10452	509.08890	3.94323
1.54	1.87214	7.04789	3.76461	2.4	3.90874	12.41289	3.90874	6.4	141.19648	559.80068	3.94323
1.55	1.88536	7.10388	3.76791	2.5	3.91593	12.56492	3.91593	6.5	156.11948	615.45817	3.94324
1.56	1.89872	7.16037	3.77116	2.6	3.92287	12.64982	3.92287	6.6	176.16933	687.05126	3.94324
1.57	1.91221	7.21736	3.77435	2.7	3.92956	12.67476	3.92956	6.7	191.18629	775.18629	3.94324
1.58	1.92581	7.27485	3.77751	2.8	3.93601	12.64982	3.93601	6.8	209.17920	881.18629	3.94324
1.59	1.93953	7.33282	3.78062	2.9	3.94223	12.56492	3.94223	6.9	229.15056	991.28804	3.94324
1.60	1.95338	7.39134	3.78367	3.0	3.94834	12.41289	3.94834	7.0	251.13891	1109.28804	3.94324
1.61	1.96733	7.45037	3.78667	3.1	3.95435	12.14780	3.95435	7.1	276.15768	1230.15768	3.94324
1.62	1.98138	7.50990	3.78962	3.2	3.96026	11.70747	3.96026	7.2	304.17141	1359.17141	3.94324
1.63	1.99553	7.56993	3.79253	3.3	3.96607	11.10058	3.96607	7.3	334.18491	1487.18491	3.94324
1.64	2.01000	7.63046	3.79540	3.4	3.97179	10.21838	3.97179	7.4	368.19741	1614.19741	3.94324
1.65	2.02500	7.69159	3.79823	3.5	3.97744	9.04347	3.97744	7.5	405.20935	1739.20935	3.94324
1.66	2.04066	7.75332	3.80102	3.6	3.98297	8.04347	3.98297	7.6	446.21751	1862.21751	3.94324
1.67	2.05699	7.81565	3.80377	3.7	3.98838	7.16037	3.98838	7.7	491.17519	1983.17519	3.94324
1.68	2.07399	7.87854	3.80647	3.8	3.99367	6.45037	3.99367	7.8	540.18255	2102.18255	3.94324
1.69	2.09166	7.94192	3.80912	3.9	3.99884	5.88281	3.99884	7.9	595.08601	2219.08601	3.94324
1.70	2.10999	8.00581	3.81171	4.0	4.00389	5.41289	4.00389	8.0	655.09836	2334.09836	3.94325
1.71	2.12899	8.07020	3.81426	4.1	4.00874	5.01838	4.00874	8.1	721.13419	2457.13419	3.94325
1.72	2.14866	8.13509	3.81677	4.2	4.01349	4.67485	4.01349	8.2	793.19031	2588.19031	3.94325
1.73	2.16899	8.20040	3.81923	4.3	4.01804	4.36606	4.01804	8.3	871.26741	2727.26741	3.94325
1.74	2.18999	8.26611	3.82164	4.4	4.02249	4.08281	4.02249	8.4	955.36481	2874.36481	3.94325
1.75	2.21166	8.33222	3.82400	4.5	4.02674	3.82281	4.02674	8.5	1045.48281	3029.48281	3.94325
1.76	2.23399	8.39873	3.82631	4.6	4.03089	3.57485	4.03089	8.6	1141.62031	3192.62031	3.94325
1.77	2.25699	8.46564	3.82857	4.7	4.03494	3.33281	4.03494	8.7	1243.77741	3363.77741	3.94325
1.78	2.28066	8.53295	3.83078	4.8	4.03889	3.09485	4.03889	8.8	1351.95481	3542.95481	3.94325
1.79	2.30499	8.60066	3.83294	4.9	4.04274	2.86037	4.04274	8.9	1466.15281	3729.15281	3.94325
1.80	2.32999	8.66877	3.83505	5.0	4.04649	2.62881	4.04649	9.0	1586.38031	3922.38031	3.94325
1.81	2.35566	8.73728	3.83711	5.1	4.05014	2.40037	4.05014	9.1	1712.63741	4123.63741	3.94325
1.82	2.38199	8.80619	3.83912	5.2	4.05369	2.17485	4.05369	9.2	1844.92481	4333.92481	3.94325
1.83	2.40899	8.87550	3.84108	5.3	4.05714	1.95281	4.05714	9.3	1983.24281	4552.24281	3.94325
1.84	2.43666	8.94521	3.84299	5.4	4.06049	1.73485	4.06049	9.4	2127.59031	4778.59031	3.94325
1.85	2.46499	9.01532	3.84485	5.5	4.06374	1.52037	4.06374	9.5	2277.96741	5012.96741	3.94325
1.86	2.49399	9.08583	3.84666	5.6	4.06689	1.30981	4.06689	9.6	2434.38481	5255.38481	3.94325
1.87	2.52366	9.15674	3.84842	5.7	4.06994	1.10281	4.06994	9.7	2596.84281	5505.84281	3.94325
1.88	2.55399	9.22805	3.85013	5.8	4.07289	0.90037	4.07289	9.8	2765.34031	5764.34031	3.94325
1.89	2.58499	9.29976	3.85179	5.9	4.07574	0.70281	4.07574	9.9	2939.87741	6030.87741	3.94325
1.90	2.61666	9.37187	3.85340	6.0	4.07849	0.51037	4.07849	10.0	3120.45481	6304.45481	3.94325
1.91	2.64899	9.44438	3.85496								
1.92	2.68199	9.51729	3.85647								
1.93	2.71566	9.59060	3.85794								
1.94	2.75000	9.66431	3.85936								
1.95	2.78499	9.73842	3.86073								
1.96	2.82066	9.81293	3.86205								
1.97	2.85699	9.88784	3.86332								
1.98	2.89399	9.96315	3.86454								
1.99	2.93166	10.03886	3.86571								
2.00	2.96999	10.11497	3.86683								

TABLE 9B. Lanchester-Clifford-Schläfli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 4/5$ and x from 1.50 to 10.0.

x	$F_{3/7}(x)$	$H_{4/7}(x)$	$T_{3/7}(x)$	x	$F_3(x)$	$H_4(x)$	$T_3(x)$	x	$F_3(x)$	$H_{4/7}(x)$	$T_{3/7}(x)$
0.0	1.00000	0.00000	0.00000	0.50	1.14905	0.37335	0.34972	1.00	1.63616	0.92366	0.56526
0.01	1.00006	0.00040	0.00410	0.51	1.15555	0.37250	0.35125	1.01	1.65007	0.93077	0.56626
0.02	1.00023	0.00096	0.00966	0.52	1.16211	0.37171	0.35285	1.02	1.66416	0.93799	0.56726
0.03	1.00053	0.00141	0.01406	0.53	1.16874	0.37099	0.35437	1.03	1.67844	0.94519	0.56826
0.04	1.00093	0.00200	0.02000	0.54	1.17543	0.37033	0.35597	1.04	1.69291	0.95241	0.56926
0.05	1.00140	0.00258	0.02580	0.55	1.18218	0.36974	0.35759	1.05	1.70756	0.95964	0.57026
0.06	1.00197	0.00319	0.03197	0.56	1.18897	0.36921	0.35923	1.06	1.72245	0.96689	0.57126
0.07	1.00260	0.00384	0.03846	0.57	1.19581	0.36871	0.36089	1.07	1.73759	0.97414	0.57226
0.08	1.00329	0.00454	0.04545	0.58	1.20270	0.36824	0.36257	1.08	1.75298	0.98139	0.57326
0.09	1.00404	0.00529	0.05293	0.59	1.20964	0.36780	0.36427	1.09	1.76861	0.98864	0.57426
0.10	1.00484	0.00609	0.06092	0.60	1.21663	0.36738	0.36599	1.10	1.78448	0.99589	0.57526
0.11	1.00569	0.00694	0.06943	0.61	1.22367	0.36698	0.36773	1.11	1.80060	1.00314	0.57626
0.12	1.00659	0.00784	0.07842	0.62	1.23076	0.36659	0.36949	1.12	1.81696	1.01039	0.57726
0.13	1.00754	0.00879	0.08791	0.63	1.23790	0.36622	0.37127	1.13	1.83357	1.01764	0.57826
0.14	1.00854	0.00979	0.09790	0.64	1.24509	0.36587	0.37307	1.14	1.85043	1.02489	0.57926
0.15	1.00959	0.01084	0.10843	0.65	1.25233	0.36554	0.37489	1.15	1.86754	1.03214	0.58026
0.16	1.01069	0.01194	0.11943	0.66	1.25962	0.36522	0.37673	1.16	1.88490	1.03939	0.58126
0.17	1.01184	0.01309	0.13093	0.67	1.26696	0.36491	0.37859	1.17	1.90241	1.04664	0.58226
0.18	1.01304	0.01429	0.14293	0.68	1.27435	0.36461	0.38047	1.18	1.92007	1.05389	0.58326
0.19	1.01429	0.01554	0.15543	0.69	1.28179	0.36432	0.38237	1.19	1.93788	1.06114	0.58426
0.20	1.01559	0.01684	0.16843	0.70	1.28928	0.36404	0.38429	1.20	1.95584	1.06839	0.58526
0.21	1.01694	0.01819	0.18193	0.71	1.29682	0.36377	0.38623	1.21	1.97395	1.07564	0.58626
0.22	1.01834	0.01959	0.19593	0.72	1.30441	0.36351	0.38819	1.22	1.99221	1.08289	0.58726
0.23	1.01979	0.02104	0.21043	0.73	1.31205	0.36326	0.39017	1.23	2.01062	1.09014	0.58826
0.24	1.02129	0.02254	0.22543	0.74	1.31974	0.36302	0.39217	1.24	2.02918	1.09739	0.58926
0.25	1.02284	0.02409	0.24093	0.75	1.32748	0.36279	0.39419	1.25	2.04789	1.10464	0.59026
0.26	1.02439	0.02569	0.25693	0.76	1.33527	0.36257	0.39623	1.26	2.06675	1.11189	0.59126
0.27	1.02599	0.02729	0.27293	0.77	1.34311	0.36236	0.39829	1.27	2.08576	1.11914	0.59226
0.28	1.02759	0.02894	0.28943	0.78	1.35100	0.36216	0.40037	1.28	2.10492	1.12639	0.59326
0.29	1.02924	0.03064	0.30643	0.79	1.35894	0.36197	0.40247	1.29	2.12423	1.13364	0.59426
0.30	1.03094	0.03239	0.32393	0.80	1.36693	0.36179	0.40459	1.30	2.14369	1.14089	0.59526
0.31	1.03269	0.03419	0.34193	0.81	1.37497	0.36162	0.40673	1.31	2.16330	1.14814	0.59626
0.32	1.03444	0.03599	0.35993	0.82	1.38306	0.36146	0.40889	1.32	2.18306	1.15539	0.59726
0.33	1.03624	0.03779	0.37793	0.83	1.39120	0.36131	0.41107	1.33	2.20297	1.16264	0.59826
0.34	1.03809	0.03959	0.39593	0.84	1.39939	0.36117	0.41327	1.34	2.22303	1.16989	0.59926
0.35	1.03994	0.04139	0.41393	0.85	1.40763	0.36104	0.41549	1.35	2.24325	1.17714	0.60026
0.36	1.04179	0.04319	0.43193	0.86	1.41592	0.36092	0.41773	1.36	2.26362	1.18439	0.60126
0.37	1.04364	0.04499	0.44993	0.87	1.42426	0.36081	0.41999	1.37	2.28415	1.19164	0.60226
0.38	1.04549	0.04679	0.46793	0.88	1.43265	0.36071	0.42227	1.38	2.30483	1.19889	0.60326
0.39	1.04734	0.04859	0.48593	0.89	1.44109	0.36062	0.42457	1.39	2.32566	1.20614	0.60426
0.40	1.04919	0.05039	0.50393	0.90	1.44958	0.36054	0.42689	1.40	2.34664	1.21339	0.60526
0.41	1.05104	0.05219	0.52193	0.91	1.45812	0.36047	0.42923	1.41	2.36777	1.22064	0.60626
0.42	1.05289	0.05399	0.53993	0.92	1.46671	0.36041	0.43159	1.42	2.38905	1.22789	0.60726
0.43	1.05474	0.05579	0.55793	0.93	1.47535	0.36036	0.43397	1.43	2.41048	1.23514	0.60826
0.44	1.05659	0.05759	0.57593	0.94	1.48404	0.36032	0.43637	1.44	2.43206	1.24239	0.60926
0.45	1.05844	0.05939	0.59393	0.95	1.49278	0.36029	0.43879	1.45	2.45379	1.24964	0.61026
0.46	1.06029	0.06119	0.61193	0.96	1.50157	0.36027	0.44123	1.46	2.47566	1.25689	0.61126
0.47	1.06214	0.06299	0.62993	0.97	1.51041	0.36026	0.44369	1.47	2.49767	1.26414	0.61226
0.48	1.06399	0.06479	0.64793	0.98	1.51930	0.36026	0.44617	1.48	2.51982	1.27139	0.61326
0.49	1.06584	0.06659	0.66593	0.99	1.52824	0.36027	0.44867	1.49	2.54212	1.27864	0.61426
0.50	1.06769	0.06839	0.68393	1.00	1.53723	0.36029	0.45119	1.50	2.56457	1.28589	0.61526

TABLE 10A. Lanchester-Clifford-Schlöfli Functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ for $\alpha = 3/7$ and x from 0.00 to 1.50.

x	$T_{3/7}(x)$	$H_{4/7}(x)$	$T_{3/7}(x)$	x	$F_{3/7}(x)$	$H_{4/7}(x)$	$T_{3/7}(x)$
1.50	3.57169	1.76254	0.68007	6.0	252.71048	3.10153	0.72624
1.51	3.57170	1.76250	0.68149	6.1	279.69327	3.57228	0.73123
1.52	3.57173	1.80466	0.68283	6.2	309.47366	3.85017	0.73531
1.53	3.57168	1.84752	0.68454	6.3	337.95369	4.08429	0.73869
1.54	3.57169	1.89094	0.68654	6.4	378.95865	4.26410	0.74142
1.55	3.57145	1.93427	0.68893	6.5	419.97650	5.29460	0.74367
1.56	3.57205	1.97741	0.69101	6.6	463.99635	5.58123	0.74514
1.57	3.57059	1.95547	0.69344	6.7	508.99955	6.74103	0.74679
1.58	3.57064	1.95515	0.69601	6.8	558.99955	7.04824	0.74824
1.59	3.57064	1.95515	0.69877	6.9	608.99955	8.04824	0.74924
1.60	3.57064	1.95515	0.70149	7.0	658.99955	8.94824	0.75011
1.61	3.57064	1.95515	0.70427	7.1	708.99955	9.84824	0.75119
1.62	3.57064	1.95515	0.70701	7.2	758.99955	10.74824	0.75208
1.63	3.57064	1.95515	0.70977	7.3	808.99955	11.64824	0.75279
1.64	3.57064	1.95515	0.71249	7.4	858.99955	12.54824	0.75336
1.65	3.57064	1.95515	0.71517	7.5	908.99955	13.44824	0.75384
1.66	3.57064	1.95515	0.71781	7.6	958.99955	14.34824	0.75424
1.67	3.57064	1.95515	0.72041	7.7	1008.99955	15.24824	0.75454
1.68	3.57064	1.95515	0.72297	7.8	1058.99955	16.14824	0.75479
1.69	3.57064	1.95515	0.72549	7.9	1108.99955	17.04824	0.75499
1.70	3.57064	1.95515	0.72797	8.0	1158.99955	17.94824	0.75514
1.71	3.57064	1.95515	0.73041	8.1	1208.99955	18.84824	0.75524
1.72	3.57064	1.95515	0.73281	8.2	1258.99955	19.74824	0.75534
1.73	3.57064	1.95515	0.73517	8.3	1308.99955	20.64824	0.75544
1.74	3.57064	1.95515	0.73749	8.4	1358.99955	21.54824	0.75554
1.75	3.57064	1.95515	0.73977	8.5	1408.99955	22.44824	0.75564
1.76	3.57064	1.95515	0.74201	8.6	1458.99955	23.34824	0.75574
1.77	3.57064	1.95515	0.74421	8.7	1508.99955	24.24824	0.75584
1.78	3.57064	1.95515	0.74637	8.8	1558.99955	25.14824	0.75594
1.79	3.57064	1.95515	0.74849	8.9	1608.99955	26.04824	0.75604
1.80	3.57064	1.95515	0.75057	9.0	1658.99955	26.94824	0.75614
1.81	3.57064	1.95515	0.75261	9.1	1708.99955	27.84824	0.75624
1.82	3.57064	1.95515	0.75461	9.2	1758.99955	28.74824	0.75634
1.83	3.57064	1.95515	0.75657	9.3	1808.99955	29.64824	0.75644
1.84	3.57064	1.95515	0.75849	9.4	1858.99955	30.54824	0.75654
1.85	3.57064	1.95515	0.76037	9.5	1908.99955	31.44824	0.75664
1.86	3.57064	1.95515	0.76221	9.6	1958.99955	32.34824	0.75674
1.87	3.57064	1.95515	0.76401	9.7	2008.99955	33.24824	0.75684
1.88	3.57064	1.95515	0.76577	9.8	2058.99955	34.14824	0.75694
1.89	3.57064	1.95515	0.76749	9.9	2108.99955	35.04824	0.75704
1.90	3.57064	1.95515	0.76917	10.0	2158.99955	35.94824	0.75714
1.91	3.57064	1.95515	0.77081				
1.92	3.57064	1.95515	0.77241				
1.93	3.57064	1.95515	0.77397				
1.94	3.57064	1.95515	0.77549				
1.95	3.57064	1.95515	0.77697				
1.96	3.57064	1.95515	0.77841				
1.97	3.57064	1.95515	0.77981				
1.98	3.57064	1.95515	0.78117				
1.99	3.57064	1.95515	0.78249				
2.00	3.57064	1.95515	0.78377				

TABLE 10B. Lanchester-Clifford-Schlafli Functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and $T_\alpha(x)$ for $\alpha = 3/7$ and x from 1.50 to 10.0.

x	$F_{4/7}(x)$	$F_{3/7}(x)$	$T_{4/7}(x)$	x	$F_{4/7}(x)$	$H_{3/7}(x)$	$T_{4/7}(x)$	x	$F_{4/7}(x)$	$H_{3/7}(x)$	$T_{4/7}(x)$
0.0	1.00000	0.02487	0.0	0.50	1.11157	0.74260	0.69077	1.00	1.47375	1.5541	1.05277
0.01	1.00004	0.02497	0.02487	0.51	1.11177	0.74663	0.69188	1.01	1.47375	1.5541	1.05277
0.02	1.00018	0.04393	0.04394	0.52	1.11207	0.75069	0.69298	1.02	1.47375	1.5541	1.05277
0.03	1.00039	0.06378	0.06379	0.53	1.11256	0.75483	0.69415	1.03	1.47375	1.5541	1.05277
0.04	1.00070	0.08463	0.08467	0.54	1.11326	0.75903	0.69538	1.04	1.47375	1.5541	1.05277
0.05	1.00109	0.09885	0.09874	0.55	1.11426	0.76334	0.69666	1.05	1.47375	1.5541	1.05277
0.06	1.00158	0.11559	0.11547	0.56	1.11546	0.76776	0.69800	1.06	1.47375	1.5541	1.05277
0.07	1.00214	0.13495	0.13467	0.57	1.11686	0.77230	0.69939	1.07	1.47375	1.5541	1.05277
0.08	1.00280	0.15795	0.15758	0.58	1.11846	0.77696	0.70083	1.08	1.47375	1.5541	1.05277
0.09	1.00358	0.18476	0.18431	0.59	1.12026	0.78174	0.70232	1.09	1.47375	1.5541	1.05277
0.10	1.00438	0.21546	0.21494	0.60	1.12226	0.78664	0.70386	1.10	1.47375	1.5541	1.05277
0.11	1.00530	0.24998	0.24940	0.61	1.12446	0.79166	0.70545	1.11	1.47375	1.5541	1.05277
0.12	1.00631	0.28848	0.28784	0.62	1.12686	0.79680	0.70709	1.12	1.47375	1.5541	1.05277
0.13	1.00740	0.33080	0.33014	0.63	1.12946	0.80206	0.70878	1.13	1.47375	1.5541	1.05277
0.14	1.00859	0.37706	0.37635	0.64	1.13226	0.80744	0.71052	1.14	1.47375	1.5541	1.05277
0.15	1.00986	0.42736	0.42660	0.65	1.13526	0.81294	0.71231	1.15	1.47375	1.5541	1.05277
0.16	1.01127	0.48168	0.48092	0.66	1.13846	0.81856	0.71415	1.16	1.47375	1.5541	1.05277
0.17	1.01281	0.53998	0.53924	0.67	1.14186	0.82430	0.71603	1.17	1.47375	1.5541	1.05277
0.18	1.01448	0.60226	0.60154	0.68	1.14546	0.83016	0.71795	1.18	1.47375	1.5541	1.05277
0.19	1.01628	0.66852	0.66782	0.69	1.14926	0.83614	0.71991	1.19	1.47375	1.5541	1.05277
0.20	1.01820	0.73876	0.73808	0.70	1.15326	0.84224	0.72191	1.20	1.47375	1.5541	1.05277
0.21	1.02024	0.81298	0.81232	0.71	1.15746	0.84846	0.72395	1.21	1.47375	1.5541	1.05277
0.22	1.02240	0.89118	0.89054	0.72	1.16186	0.85480	0.72603	1.22	1.47375	1.5541	1.05277
0.23	1.02468	0.97336	0.97274	0.73	1.16646	0.86126	0.72815	1.23	1.47375	1.5541	1.05277
0.24	1.02708	1.05952	1.05892	0.74	1.17126	0.86784	0.73031	1.24	1.47375	1.5541	1.05277
0.25	1.02960	1.14966	1.14908	0.75	1.17626	0.87454	0.73251	1.25	1.47375	1.5541	1.05277
0.26	1.03224	1.24378	1.24322	0.76	1.18146	0.88136	0.73475	1.26	1.47375	1.5541	1.05277
0.27	1.03500	1.34188	1.34134	0.77	1.18686	0.88830	0.73703	1.27	1.47375	1.5541	1.05277
0.28	1.03788	1.44396	1.44344	0.78	1.19246	0.89536	0.73935	1.28	1.47375	1.5541	1.05277
0.29	1.04088	1.54998	1.54948	0.79	1.19826	0.90254	0.74171	1.29	1.47375	1.5541	1.05277
0.30	1.04398	1.66092	1.66044	0.80	1.20426	0.90984	0.74411	1.30	1.47375	1.5541	1.05277
0.31	1.04718	1.77676	1.77630	0.81	1.21046	0.91726	0.74655	1.31	1.47375	1.5541	1.05277
0.32	1.05048	1.89748	1.89704	0.82	1.21686	0.92482	0.74903	1.32	1.47375	1.5541	1.05277
0.33	1.05388	2.02298	2.02256	0.83	1.22346	0.93252	0.75155	1.33	1.47375	1.5541	1.05277
0.34	1.05738	2.15326	2.15286	0.84	1.23026	0.94036	0.75411	1.34	1.47375	1.5541	1.05277
0.35	1.06098	2.28842	2.28804	0.85	1.23726	0.94834	0.75671	1.35	1.47375	1.5541	1.05277
0.36	1.06468	2.42846	2.42810	0.86	1.24446	0.95646	0.75935	1.36	1.47375	1.5541	1.05277
0.37	1.06848	2.57348	2.57314	0.87	1.25186	0.96472	0.76203	1.37	1.47375	1.5541	1.05277
0.38	1.07238	2.72348	2.72316	0.88	1.25946	0.97312	0.76475	1.38	1.47375	1.5541	1.05277
0.39	1.07638	2.87846	2.87816	0.89	1.26726	0.98166	0.76751	1.39	1.47375	1.5541	1.05277
0.40	1.08048	3.03842	3.03814	0.90	1.27526	0.99034	0.77031	1.40	1.47375	1.5541	1.05277
0.41	1.08468	3.20336	3.20310	0.91	1.28346	0.99916	0.77315	1.41	1.47375	1.5541	1.05277
0.42	1.08898	3.37326	3.37302	0.92	1.29186	1.00814	0.77603	1.42	1.47375	1.5541	1.05277
0.43	1.09338	3.54812	3.54788	0.93	1.30046	1.01726	0.77895	1.43	1.47375	1.5541	1.05277
0.44	1.09788	3.72796	3.72774	0.94	1.30926	1.02652	0.78191	1.44	1.47375	1.5541	1.05277
0.45	1.10248	3.91276	3.91256	0.95	1.31826	1.03592	0.78491	1.45	1.47375	1.5541	1.05277
0.46	1.10718	4.10252	4.10234	0.96	1.32746	1.04546	0.78795	1.46	1.47375	1.5541	1.05277
0.47	1.11198	4.29726	4.29710	0.97	1.33686	1.05514	0.79103	1.47	1.47375	1.5541	1.05277
0.48	1.11688	4.49696	4.49682	0.98	1.34646	1.06496	0.79415	1.48	1.47375	1.5541	1.05277
0.49	1.12188	4.70162	4.70150	0.99	1.35626	1.07492	0.79731	1.49	1.47375	1.5541	1.05277
0.50	1.12698	4.91122	4.91112	1.00	1.36626	1.08502	0.80051	1.50	1.47375	1.5541	1.05277

TABLE 11A. Lanchester-Clifford-Schlafli Functions $F_\alpha(x)$, $H_{1-\alpha}(x)$, and

$T_\alpha(x)$ for $\alpha = 4/7$ and x from 0.00 to 1.50.

x	$F_{4/7}(x)$	$H_{3/7}(x)$	$T_{4/7}(x)$	x	$F_{4/7}(x)$	$H_{3/7}(x)$	$T_{4/7}(x)$	x	$F_{4/7}(x)$	$H_{3/7}(x)$	$T_{4/7}(x)$
1.50	2.17392	2.62923	1.20944	2.0	3.5828	4.3755	1.28168	6.0	164.99174	218.86467	1.32653
1.51	2.17233	2.62923	1.21167	2.1	3.71706	4.48548	1.28962	6.1	182.10837	241.57070	1.32653
1.52	2.17073	2.62923	1.21390	2.2	3.85120	4.59538	1.29679	6.2	201.80329	266.97827	1.32653
1.53	2.16913	2.62923	1.21613	2.3	4.01350	4.71021	1.30395	6.3	221.80159	294.97430	1.32653
1.54	2.16753	2.62923	1.21836	2.4	4.17580	4.82504	1.31111	6.4	244.40225	324.86946	1.32653
1.55	2.16593	2.62923	1.22059	2.5	5.40141	7.07432	1.30972	5	270.33290	358.60439	1.32653
1.56	2.16433	2.62923	1.22282	2.6	5.94665	7.79848	1.31733	5.1	298.41064	395.80337	1.32653
1.57	2.16273	2.62923	1.22505	2.7	6.53623	8.59651	1.32521	5.2	329.41064	436.97335	1.32653
1.58	2.16113	2.62923	1.22728	2.8	7.19391	9.47618	1.33309	5.3	363.63818	481.37748	1.32653
1.59	2.15953	2.62923	1.22951	2.9	7.92006	10.44590	1.34097	5.4	401.42949	533.55097	1.32653
1.60	2.15793	2.62923	1.23174	3.0	8.72171	11.51518	1.34885	7.0	443.15614	581.86102	1.32653
1.61	2.15633	2.62923	1.23397	3.1	9.59843	12.69435	1.35673	7.1	489.25887	646.97766	1.32653
1.62	2.15473	2.62923	1.23620	3.2	10.55835	13.98486	1.36461	7.2	540.09925	719.97133	1.32653
1.63	2.15313	2.62923	1.23843	3.3	11.60148	15.38793	1.37249	7.3	595.70116	799.97426	1.32653
1.64	2.15153	2.62923	1.24066	3.4	12.72891	16.91517	1.38037	7.4	656.69212	879.97719	1.32653
1.65	2.14993	2.62923	1.24289	3.5	13.94170	18.57235	1.38825	7.5	726.17774	964.09527	1.32653
1.66	2.14833	2.62923	1.24512	3.6	15.24085	20.36353	1.39613	7.6	802.39977	1066.41005	1.32653
1.67	2.14673	2.62923	1.24735	3.7	16.62720	22.29271	1.40401	7.7	885.90216	1177.91944	1.32653
1.68	2.14513	2.62923	1.24958	3.8	18.10185	24.37289	1.41189	7.8	978.10839	1299.44215	1.32653
1.69	2.14353	2.62923	1.25181	3.9	19.66570	26.61097	1.41977	7.9	1079.92661	1433.55915	1.32653
1.70	2.14193	2.62923	1.25404	4.0	21.31905	29.01616	1.42765	8.0	1192.35862	1581.70466	1.32653
1.71	2.14033	2.62923	1.25627	4.1	23.06240	31.59416	1.43553	8.1	1326.40024	1746.94024	1.32653
1.72	2.13873	2.62923	1.25850	4.2	24.89575	34.34266	1.44341	8.2	1482.26881	1928.26881	1.32653
1.73	2.13713	2.62923	1.26073	4.3	26.81910	37.26591	1.45129	8.3	1660.10284	2128.10284	1.32653
1.74	2.13553	2.62923	1.26296	4.4	28.83245	40.37719	1.45917	8.4	1861.88200	2350.18200	1.32653
1.75	2.13393	2.62923	1.26519	4.5	30.93580	43.67238	1.46705	8.5	2098.62244	2595.77281	1.32653
1.76	2.13233	2.62923	1.26742	4.6	33.12915	47.15257	1.47493	8.6	2372.32288	2868.25017	1.32653
1.77	2.13073	2.62923	1.26965	4.7	35.41250	50.81976	1.48281	8.7	2685.99732	3168.71279	1.32653
1.78	2.12913	2.62923	1.27188	4.8	37.78585	54.67495	1.49069	8.8	3040.66176	3508.96225	1.32653
1.79	2.12753	2.62923	1.27411	4.9	40.24920	58.71814	1.49857	8.9	3438.31620	3898.99625	1.32653
1.80	2.12593	2.62923	1.27634	5.0	42.80255	62.94933	1.50645	9.0	3881.97064	4261.24747	1.32653
1.81	2.12433	2.62923	1.27857	5.1	45.44590	67.36852	1.51433	9.1	4374.72508	4705.40498	1.32653
1.82	2.12273	2.62923	1.28080	5.2	48.17925	71.97671	1.52221	9.2	4927.57952	5196.06282	1.32653
1.83	2.12113	2.62923	1.28303	5.3	50.99260	76.77390	1.53009	9.3	5541.53396	5731.85318	1.32653
1.84	2.11953	2.62923	1.28526	5.4	53.89595	81.76009	1.53797	9.4	6227.58840	6336.19435	1.32653
1.85	2.11793	2.62923	1.28749	5.5	56.88930	86.93528	1.54585	9.5	6996.74284	6996.74284	1.32653
1.86	2.11633	2.62923	1.28972	5.6	59.97265	92.39947	1.55373	9.6	7861.99728	7726.77579	1.32653
1.87	2.11473	2.62923	1.29195	5.7	63.14599	98.15266	1.56161	9.7	8834.35172	8532.74759	1.32653
1.88	2.11313	2.62923	1.29418	5.8	66.40934	104.19485	1.56949	9.8	9924.80616	9422.93229	1.32653
1.89	2.11153	2.62923	1.29641	5.9	69.76269	110.52704	1.57737	9.9	11144.44810	10405.93299	1.32653
1.90	2.10993	2.62923	1.29864	6.0	73.20594	117.15923	1.58525	10.0	8662.91020	11491.65041	1.32653
1.91	2.10833	2.62923	1.30087								
1.92	2.10673	2.62923	1.30310								
1.93	2.10513	2.62923	1.30533								
1.94	2.10353	2.62923	1.30756								
1.95	2.10193	2.62923	1.30979								
1.96	2.10033	2.62923	1.31202								
1.97	2.09873	2.62923	1.31425								
1.98	2.09713	2.62923	1.31648								
1.99	2.09553	2.62923	1.31871								
2.00	2.09393	2.62923	1.32094								

TABLE 11B. Lanchester-Clifford-Schlafli Functions $F_{\alpha}(x)$, $H_{1-\alpha}(x)$, and

$T_{\alpha}(x)$ for $\alpha = 4/7$ and x from 1.50 to 10.0.

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